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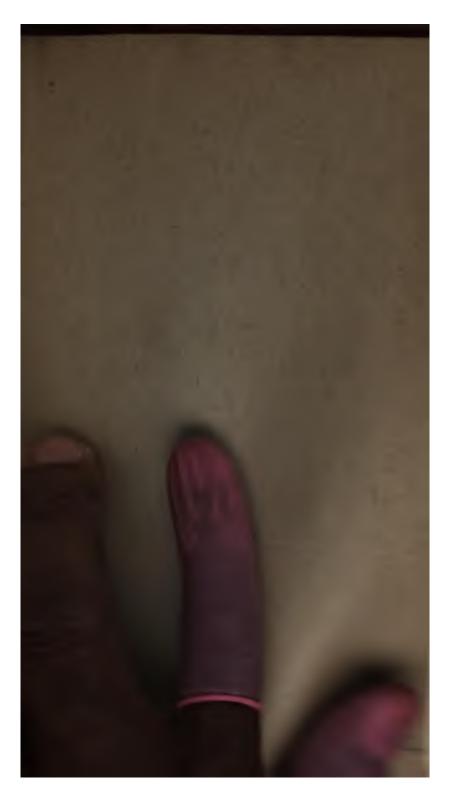
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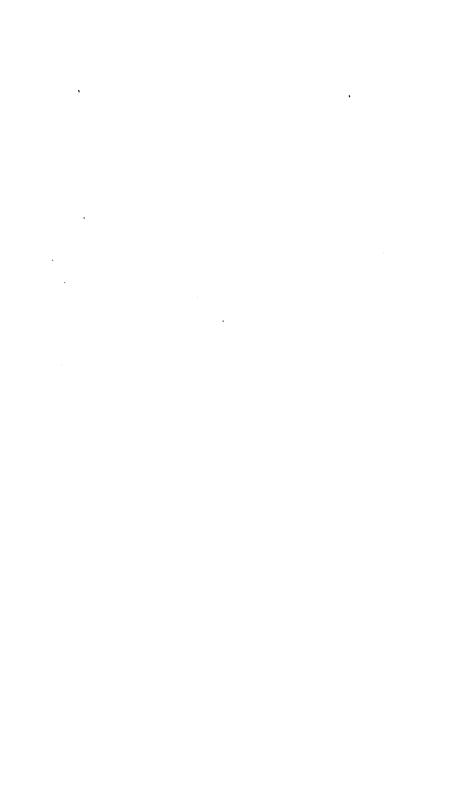


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# By THOMAS HODSON.

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IN TWO VOLUMES.
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In each of the other fubjects. I have retained those parts which appeared to me the most effective, and reject of the superfluous; as sling myself of the labours of others on each of the subjects; though I have not quoted every author; as that would be effected with more difficulty than might be at sirft expected, and partake of a preciseness unnecessary in the present work.

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Middle Temple,

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## CHAP. I.

## OF ENGLISH GRAMMAR.

#### SECT. I.

#### OF THE DIVISION AND SOUND OF LETTERS

IN the early ages of antiquity, before alphabets were invented, mankind, fensible of their want of some means of recording historical events and scientifical discoveries, had recourse to various arts for these purposes; the first of which was painting. That partiality for pictures, so evident in all ages and countries, afforded our ancients a method of perpetuating their transactions. To commemorate that one man had killed another, they painted the figure of a dead many with another man standing over him, having an hostile weapon in his hand. On the first discovery of America, this was the only kind of writing used by the Mexicans.

The first improvement made by our ancestors in the art of writing (if it might then be called an art) was by the introduction of hieroglyphical characters. These consisted of

certain fymbols, which were made to repressit fible objects, to which, in fome particular, fucility to sols were furnoied to bear force retemblance. An eye whiche fymbol of knowledge; a curcle, of eternity, as having the her beginning nor did. The figures of animals were alter thuch emplayed in this kind of writing, on account of fome quality with which they were improfed to be endowed, and in which they refembled the object figuited. Thus, imprudence was represented by a fly; wildom by an ant; and victory by a bawk. These hieroglyphics flourished most in ancient legypt (as did all other learning at that time), where the knowledge of thefe characters was reduced into a regular art; and many specimens of them are still extant in relies of Egyptian anti-Hieroglyphica, though an improvement upon the former mode of writing, was a very imperfect one, and often contufed and perplexed its most skilful professors.

In a few forceding ages, hieroglyphics gave place to fumple arbitrary marks, which were introduced to reprefent objects, without having the least refemblance or affinity to the objects repretented. The Chinese fill use characters of. this nature: they have no alphabet of letters, but every fingle mark or character fignifies one perfect idea or object. The number of their characters are therefore great :-- near a feventy thousand. To be perfectly acquainted with them?': conflitutes the bufinels of a whole life; which must be aninformantable obffacle to the improvement of frience. Ours common figures, 1, 2, 3, 4, &c., afford us an example of Ship. .. fort of writing; where each figure or character conveys the idea of the number for which it thinds as clearly and intelligibly in the words themselves, one, two, three, &c. . But when sparks or characters come to be used for all our items. in exclusion to an alphabet of letters, they then, from their number, become inconvenient.

The next improvement in the art of writing was by the povention of tigns or marks, which flood, not directly for the objects themselves, but for the words or names whichly

they were diffinguished. This was an alphabet of fyllable. An alphabet of this kind is still in use in Athiopia, and some countries of India.

But the noble and fublime diknovery of an alphabet of letters superfeded every other improvement in this art. Who was the first in this invention is uncertain. An alphabet of letters was, however, brought into Greece by Cadmus, the Phrenician, who was cotemporary with king David. This alphabet consisted of only fixteen letters: the rest were added afterwards, as signs for proper sounds were found to be wanting. The Phrenician, Hebrew, Greek, and Roman alphabets are so much alike in the figures and names of the letters, as plainly to evince they were originally derived from the same.

By the use of the alphabet, we are now, therefore, enabled to express our ideas with the same elearness and precision, as in conversation.

The English alphabet confish of twenty-six letters, A, a; B, b; C, c; D, d; E, c; F, f; G, g; H, h; l, i; J, j; K, k; L, l; M, m; N, n; O, o; P, p; Q, q; R, r; S, f; s; T, t; U, u; V, v; W, w; X, x; Y, y; Z, z: and is divided into vowels and conforants, mutes and temi-vowels.

The names of the twenty-fix letters are as follow: a, bec, cee, dee, e, ef, gee, aitch, i, ja, ka, el, em, en, o, pee, cue, ar, efs, tee, u, vee, double u, ex, v, zad.

The vowels are fix in number, viz. a, c, i, c, x, y; all the refl are conforants.

The mutes are those letters which are begun, when they are spelled, by a consonant: as, h, bec; c, cre; d, dee, &c.; those which are begun with a vowel are called simi-vowels: as, l, el; m, en; e, en; r, ar; s, efs. &c.; l, m, n, r, are also called liquids.

When two vowels meet together, they are called a diphthong; of these there are thirteen, viz. ai, ei, ei, ei, ui, au, eu, eu, ee, ee, ee, ee, ee, and ie.

When three vowels meet, they are called a triphthong: as in the word beauty.

With regard to the found of these double vowels, there are so rules, that can be given, which will hold good in all cases, as words are sounded according to the caprice or affectation of the age, or the speakers: a knowledge of them must, therefore, be acquired by experience and observation.

And concerning the found of fingle letters, the following rules are all that can fafely be depended upon.

C is pronounced hard like k, before a, o, n; and fost like s, before o, i, and v.

G is also sounded hard before a, o, u; sometimes hard, and sometimes soft, before i and y; and generally soft before o.

E is mostly filent at the end of a word; but in that case it lengthens the foregoing vowel; as, bid, bide; and that sometimes in the middle of a word; as ungrateful. But sometimes it only softens a preceding g, as in ledge, judge.

H is only an aspiration of the breath, and sometimes at the beginning of a word is not sounded at all: as, an bear, an bear, man.

W is either a vowel or a diphthong: its proper found is the same as a in the Italian, on in the French, or so in the English. Sometimes it is not founded at all after o, sometimes like an.

X is a double confonant, composed of a hard c or k, and s; and at the beginning of a word mostly sounded like x.

Y has exactly the same sound as i; and is only a substitute for it at the end of a word, or before i: as, cry, flying. It is a perfect vowel: and when used as a consonant at the beginning of a word, it answers to the ancient Saxon i: as, year, iw; young, iong.

Z is a double confonant; it founds as much coarser and thicker than s, as w does than f.

J and w, though confounded by fome old writers with i and u, are entirely different letters; the former having the found of a foft g, and the latter that of a coarser f. The former is called ja, and the latter vee.

#### SECT. 11.

#### OF SYLLABLES.

A SYLLABLE is a constituent part of a word, or a whole word; it consists of one or more letters, and is formed by a single impulse of the voice.

Spelling is the art of rightly naming the letters fingly that constitute a word, and dividing them into syllables.

The art of spelling perfectly is not to be acquired (particularly in the English) but by practice: but a few rules for the dividing of syllables may possibly be of service.

- 1. A fyllable in the beginning, or middle, of a word ends in a vowel, except fuch vowel be followed by x, or two or more conforants: as in re-li-gi-on.
- s. When two or more confoundts follow a vowe!, which is pronounced thort, they must be separated; and one, at least, always belongs to the preceding syllable: as in ab-flinence.
- 3. When two or more confonants follow a vowel, which is pronounced long, they fometimes belong to the following syllable: as, di-gress.
- 4. A particle, though placed immediately before a vowel, is feldom divided: as, un-e-qual.
- 5. A mute with a liquid following are feldom divided; but a liquid or a mute, with a mute following, are mostly divided.
  - 6. When le or re follow a mute they are never divided.

These are the fundamental rules for the dividing of syllables; but some grammarians recommend them to be diwided as they are sounded in a just pronunciation.

#### SECT. III.

#### OF THE NINL PARTS OF SPEECH.

WHEN mankind had arrived at fome perfection in the art
of writing, they foon discovered the property of reducing
Language

language into different forms of words; or, as they are commonly called, parts of speech.

In English we have nine forms of words, or parts of speech.

- The Article—placed before nouns to help to determine their fignification: as, a man, the man.
- 2. The Substantive, or noun—which is the name of any object whatever, of which we have any idea: 28, a man, a borfe, a spirit, grief, love.
- 3. The PRONOUN—used as a substitute for the noun: as, be, she, it.
- 4. The Adjective—added to the noun to denote its quality: as, an bonest man, a white horse, an evil spirit.
- 5. The VER 1—which fignifies a flate of existence, acting or suffering: 25, state centinels slept, the enemy entered, and the fort was taken."
- 6. The Adver B—used to qualify or enforce the meaning of other words. It is added sometimes to a verb: as, he reads well. Sometimes to an adjective: as, "an exceeding high mountain." Sometimes to another adverb: as, "most divinely fair."
- 7. The Preposition—placed between words to connect them together: as, "the path to fame lies through the road to danger."
- 8. The Conjunction—used to connect sentences, as prepositions connect words: as, "fear God and honour the King."
- 9. The INTERJECTION—used to express the surprise or affection of the speaker: as, O! alas!

These are the nine parts of speech in the English tongue; every word in which is reducible to one of these parts.

The ARTICLE is placed before substantives to shew how far their signification extends.

There are in English only two articles; a and the. A is called the indefinite, and the the definite article.

The indefinite article a is changed into an when the next word begins with a vowel, or a filent b before the vowel; except such vowel be y or w. This article, as its name imports, is used in an indefinite and undetermined sense: as, a

man, means one man, without determining who in particular; leaving that to be explained, if necessary, by the other pares of the sentence.

This article can, therefore, be joined to substantives in the singular number only, except it come before the adjectives few and many: as, a few days, a (great) many men; or before the complete numerical adjectives, a dozen, a livre, an bundred, a thousand, a million, a myriad: as, a dozen pound, a spore of eggs, an bundred men, &c.

The definite article the determines which particular thing is meant, or of many which they are: this is therefore employed both with fingular and plural nouns: as, 40 the flork in the beavers."

It is also used sometimes before adverbs in the comparative and superlative degrees; as, the more, the better, the least of all.)

The SUBSTANTIVE is the name of any object whatever of which we have any idea.

There are two forts of substantives, Proper and Common. Proper names are such as belong to individual objects, whether animate or inanimate; but not to every individual or object of the same fort or species: thus, John is the name of a man, but not the name of every man; Chance may be the name of a dog, but it is not the name of every dog; London the name of a city, but not of every city. These are therefore proper names; but man, dog, and city are common names: for man as the common name of every man; dog, the common name of every dog; and city, the common name of every city.

Proper names have no articles nor plural number, unless by a metaphor: as when a cruel tyrant is called a New; or when a common name is understood, as the (ship) Royal George; or when there are many of the same name, as the twelve Caesars.

There are three attributes belonging to an English noun, viz. number, gender, and case.

The number is either fingular or plural. The fingular number expresses one object: as, a king: the plural, two or more, as, king:

10

Lan

The plural number is mostly formed, in English, by the addition of s or es: as, boy, boys; goat, goats; fox, foxes.

Some change the f into v: as, wife, wives; leaf, leaves.

Some plurals end in en: 22, on, onen; child, children; man men; brother, brethren. In the latter, and some others, the o in the first fyllable is changed into e. This form is the remains of the Teutonic language, and the following of the Saxon; louse, lice; mouse, mice; tooth, teeth.

Some nouns ending in y, change it into i: as, city, cities; gallery, galleries.

Some nouns have no plural: as, corn, gold, pitch, floth, &cc And others no fingular numbers: as, annals, bellows, sciffars, lungs, &cc. The words sheep and deer have no variation o number.

All substantives in English, whether common or proper are considered with relation to gender, as being either of the masculine, seminine, or neuter gender. That is, either of the male or female sex, or neither.

The masculine or seminine genders are applied to the name of animals only, and such whose sex is obvious: as, man Thomas, ox, which are the masculine gender: Mary, woman hen, cow, which are the seminine gender. Those whose sex is not evident, with all inanimate objects, are of the neuter gender: as, oxster, worm, house, tree; except in poetry, and the clegant species of composition, where inanimate objects, and the human passions, are personisted into men and women, and consequently have their genders.

A few substantives are marked by their terminations: as, prince, princess; lion, lioness; aslor, astress.

The chief use of gender is to agree with the pronoun.

In English there are three different cases of the noun: the nonmative, possessive, and objective case.

The nominative case is the simple name of the noun, without relation to other objects: as, " John."

The possessive signifies the relation of possession: as, "John's book," and was formerly written "John's book," and not "John bis book," as is vulgatly written. It may also be expressed by

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: Thou, in all its cases, generally gives place to you, except in a very solemn style, and in addresses to the Deity.

As the personal pronoun is a substitute for the noun, so it has the same nature in grammatical construction, and is capable of forming a sentence without the aid of the substantives as, "I that speak unto thee am be [Christ]." John, iv. 86.

But there are other pronouns, of the nature of adjectives, and, like adjectives, require some substantive to be joined with them, which is either expressed or understood. Those are therefore called Pronominal Adjectives. Of these there are sour forts: possession, and, they, our, your, ber, elvir; and are metirely different words from the possession pronouns, nine, thing, see. In these the substantive is sometimes understood without being expressed: as, "Ashe frame be yours;" whereas, to those the substantive skould be added: as, "soly people shall be my people, and thy God my God." Ruth, i. 16.

The definitives are, this, that, ether, any, fond, one, new, These define, or limit, the meaning of the substantive to which they refer, or are joined. The three first lave the plural number: as, these, these, others. This refers to the latter term or sentence, that to the former: as, "block are definitives, these (mentioned before) are possessive;" other is used in the plural form only, when the substantive belonging to it is not expressed, as is sometimes the case in definitives: other and one have also the possessive case; as, "this is others' property," and "it startles one's apprehension;" one is also used in an indefinite sense, as "one thinks." These are all the variations definitives admit of.

The relatives are, who, which, that. These refer to some substantive or pronoun going before, which is therefore called the antecedent: as, "I am the Lord that maketh all things, that stretcheth forth the heavens alone." Issiah, xliv. 24. They also connect the following and foregoing parts of a sentence together. Who is varied to express the three cases: as, who, vulose, whom; these relatives refer to all the three persons,

persons, whereas the other pronominal adjectives belong only to the third person. Who, which, what, are called interrogatives, when they are used in a question.

Each, every, either, are called diffributives, because they relate to objects or persons taken separately.

Besides the foregoing pronominal adjectives, there are two others: ocun, and felf, in the plural selves. Both of them express emphasis, or opposition, and are joined to the possessives, and so form a compound pronominal adjective: as, my own, thyself, yearselves.

Ourfelf, the plural pronominal adjective, with the fingular substantive, belongs to the regal style.

All fubitantives belong to the third person, except when an address is made to a person, then the substantive is of the second person.

An ADJECTIVE is a word added to a substantive, to express the quality of it, or some other property: as, a good man, an bundred pounds, a burning mountain.

Adjectives have no variation, except the three degrees of comparison: positive, comparative, and superlative.

Most qualities consist of different degrees, or of more or less. Thus, when a quality is simply expressed, without reference to a greater or less degree of the same, it is called the positive degree: as, large, short. When it is expressed with relation to a less degree, it is called the comparative degree: as, larger, shorter. When it is expressed as being of the highest degree in its quality, it is called the superlative: as, largest, shortest.

There are two ways of forming the comparative and superlative degrees; the first is by adding r or er to the positive degree, which forms the comparative; and by adding st or est to the positive, and so forming the superlative degree; as in the last example. Most monosyllables are compared in this manner; and dissyllables ending in y: as, happy; and k, when they are followed by a mute: as, able; or when they are accented on the last syllable: as, genteel. But others, and words of more than two fyllables, feldom admit of these terminations; but are compared according to the following rule.

The fecond method of forming the comparative and superlative degrees of comparison, is by placing the adverbs more or riost before the adjective of the positive degree: as, expevienced, more experienced, mest experienced.

The superlative is, in a few words, formed by adding the adverb most to the end of them: as, neibermest, foremost, appearant, andermost, &cc.

The four following adjectives are irregular in the formation of the degrees of comparison in most languages: good, better, left; had, worse, worse; little, left, least; much or many, more, mest.

Double comparatives and superlatives are improper in grammar: as, the more greater, or the most greates; except the most bigloss, a phrase used in the Pfatas of David, and is properly applicable to the Supreme Being only.

The VERB is a word which fignifies an action, or a flate or condition of being; and is either active, pallive, or neuter.

A verb active expresses an action in its natural order, that is, when the agent is placed first, and the object last; as, " John love his book." Here John is unled the agent, because he performs the action, which is love, and which is the verb; and hook is the object, upon which the action love is exercised.

A verb passive expresses an action, but in an inverted order; that is, when the object is placed first, and the agent last: as, we the book is loved by John." Here may be seen the use of the cases of nouns and pronouns: for when the verb is active, the agent is placed first, and is in the nominative case; 'as, " I love else." When the verb is passive, the object being placed first, must be in the nominative case, and the agent being last must be in the objective case, accompanied with a preposition; and the verb assumes a different form: as, " then are soved by me." Thus an active verb may be transformed into a passive, or a passive verb into an active verb.

A verb neuter expresses a state, or condition, of being, only, and consequently has no object to be acted upon; but an agent only: an I walk, I steep, I decemed, be fell, she arefe. The verb neuter is called also the intransitive verb, and the verb active transitive.

Many verbs are used in English both in an active and neuter tignification; their form demonstrating of which kind they are.

The verb is varied, first, to correspond with the three different persons of the pronoun; secondly, to agree with the number singular or plural; thirdly, to express the three principal gradations of time,—present, past, and suture; lastly, to show the mode or manner in which the action or state of being is expressed.

. In a verb are, therefore, these sour attributes; person, number, time, and mode.

To agree with the three personal pronouns, though of the same number, the verb is varied: as, I love, then loves, be loved or loves.

Also to agree with the two different numbers of the same person: as, thou loves, ye love; he lovesh, they love.

Likewife, to express the different times in which the action is represented: as, I love, I loved, I have loved. To express the different times, other verbs are often used, called auxiliaries, as will be seen hereafter.

The verb is moreover varied according to the different manner of expressing the action or being; which variations are called its modes; of which there are generally reckoned four, besides the participle: the indicative, imperative, subjunctive, and infinitive.

When a circumstance is simply declared, or when a question is asked, the verb employed on these occasions is of the indicative mode: as, I love, he loves, lovest thou? When any thing is commanded, or folicited, or requested to be done, be it to a superior or inserior, the verb employed in the sentence is of the imperative mode: as, love thou, "O Thou

my voice infpire!"—Pope. When any thing is expressed in a doubtful manner, or under a condition, or supposition, or the like; or when it is subjoined as the end or design; or when it is expressed in the form of a wish; it is, in any of these cases, and in many others, the subjunctive mode of the verb: as, if I love, "though he stay me, yet will I put my trust in him." Job, xiii. 15. "Long may be live." The verb in this mode generally depends on some other verb, and has a conjunction before it: as, "Though after my skin, worms destroy this body, yet in my slesh shall I for God." Job, xix. 26.

Here jt must be noted, that when an application is made, of the nature of a request, the verb is of the imperative mode: as, "Lord face me." Matt. xiv. When it is of the nature of a wish, the verb is of the subjunctive mode: as, "O King, live for ever." Dan. iii. When the verb is expressed without any reference to person or number, it is called the infinitive mode: at, to love; and when it is expressed in such a form, that it may be joined to an adjective, it is called the participle, and has somewhat of the nature of an adjective: as, loving, loved.

To express the different times of the verb, in English, it is often necessary to make use of other verbs, called therefore similaries, or helpers; of which there are nine: be, have, do, let, may, must, can, shall, will. The two first are chiefly used for forming the different times of the verb: it is, therefore, necessary to know how to decline them according to person, number, time, and mode.

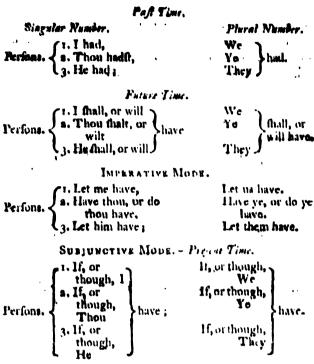
#### TO HAVE.

INDICATIVE MODE. - Present Time.

Perfons.

I. I have,
2. Thou hast,
3. He hath, or has;

Plural Number,
We
Ye
They



Present, To have; Post, To have had.

#### PARTICIPIE.

Profest, Having ;-Ported, Had; . . Post, Having had.

As the plural pronoun you is mostly employed instead of the fingular rhou, it must, therefore, have the plural verb; as, you have, you had, you were; and not you hast, you had, you were; and not you hast, you had, you were; and not you hast, you had, you had, you were; and not you hast, you had, you had, you were; and not you hast, you had, you which the first or third person fingular of the verb; and which error writers of the first eminency have committed.

In the third person singular, present time, indicative mode, the termination of the verb is generally in s, instead of so or etc, in the polite and familiar style: us, he bas, instead of he bash; he boss, for he bossh. But in the very solemn and serious style the termination is in sb.

## TO BE. '

INDICATIVE MODE.—Profes	t Time.
· Singular Number.	Plural Number.
Perfons. { r. I am, a. Thou art, 3. He is ;	Ye They
C3. He is ;	They J
Paft Times .	
Ca. I was,	We Ye were.
Perform { z. 1 was, s. Thou walt, 3. He was;	Ye were.
(3. He was;	They J
Future Time.	•
Persons, { z. I shall, or will, a. Thou shalt, or wilt, } be;	We 7 mall an
Persons, < a. Thou shalt, or wilt, > be ;	Te will be
(3. He fhall, or will,	They J "" ou
Interative Mode.	• •
Cr. Let me be,	Let us be-
Persons. { z. Let me be, z. Let me be, z. Let him be; z. Let him b	Be ye, or do ye be.
(3. Let him be ;	Let them be.
SUBJUNCTIVE MODE Profi	int Lime.
<b>ር</b> ፡፡ 161 - ጋ	If we
Perform. { t. If I a. If thou be;	If we li ye le they
Co. If he J	If they J
Paft Time.	
Perfons. { s. I were, s. Thou wert, s. It's were;	Ye Yere.
remone.	Te > Weller
(3. the weld)	Tiley J
lupinitive Mode.	
Profest, To be;—Past, To ha	ve been.
PARMINIT.	

Profest, Being ;- Perfect, Been ;- Past, Having been.

The

The Variation of the Verb active according to Perfon, Number, Time, and Mode.

## TO LOVE.

# INDICATIVE MODE .- Prefent Time.

Singular Number.  1. 1 love, 2. Thou lovest, 3. He loveth, or loves; Paf Time.	Plural Number. We Ye They
Persons. { t. I loved, a. Thou loveds, g. He loved;	We Ye They loved.
Fature Time.  I. I shall, or will,  Thou shalt, or wilt,  He shall, or will,	
IMPERATIVE MODE	
Persons. {1. Let me love, a. Love thou, or do thou love, 3. Let him love;	Let us love. Love ye, or do ye love. Los them love.
SUBJUNCTIVE MODE.—Pro	fent Tues.
Perfons. { 1. I a. Thou } love;	We Ye They love.
Alfo,	
Perfons. { i. I may a. Thou may } love;	Ye may love; and have loved.
Past Time.	
Persons. { r. I might s. Thou mightest } love;	Ye might love; and have loved.
Ayo,	
Perform:    Solution of the second of the se	Ye could, fhould, or would love; and have loved.
Yor., I. C	J Infi-

# Infinitive Mone. Prefent, To love; — Paft, To have loved.

#### PARTICIPLE.

Prefent, Loving ;- Perfett, Loved ;- P. of. Having loved.

In the plural number of the subjunctive mode, the imperfect and perfect times are put together. The verb in the prefent time, and the auxiliary of the prefent and past imperfect times of this mode, frequently have a future signification; as, "if he arrive (hereafter) we shall do well;" "if he should, or would come (to-morrow), I might, would, could, or should speak to him." The auxiliaries should and would, in the past imperfect, are also used to express the three species of time, praint, past, and future; as, "it is my defire that he should or would come (yesterday)." Therefore, in this mode, the time of the verb is known mostly by the nature of the sentence.

The three grand divitions of time, into prefent, path, and future, are called indefinite, or undeterminate time; but each of these are subdivided into imperfect and perfect time, which subdivition is called definite or determined time.

#### Definite or determined Time.

Attive Vesti,	Puttive Verti Present Impersect.	Neuter Verb
I am (now) loving,	I am loyed,	I am entering.
•	Present Persett.	
I have (now) loved.	I have been loved,	I have entered.
	Puff Impersion.	
I was (then) loving,	I was loved,	I was entering.
	Past Persatt.	
I had (then) loved,	I had been loved,	I had entered.
	Puture Imperfect.	
I finall (then) be lovin	ig, I fiell be loved,	I finali be entering
	Puture Perfett.	_
I hall (then) lieve loved,	I mail have been leved,	. I fh <mark>ail have e</mark> ntered . 11

It is not necessary to give the variations of the definite times, as they are formed only by the proper variations of the auxiliaries, joined to the present or perfect participle.

In the formation of these definite times, the active and neuter verbs are alike; the passive verb differs from the active, only in having the perfect participle inflead of the present in the imperfect times; and having the perfect participle sees in the perfect times.

The pattive verb is formed through all its variations of person, number, time, and mode, by adding the persect, or pattive participle (both which are the same, and in all regular verbs the same as the indefinite patt time active) to the auxiliary verb to be, through all its variations: as, I am look, I shall be look, thou art lovel, &c.; the object is placed before the verb, and is in the nonmative case, and the agent follows the verb, and is in the objective case, are companied with a preposition: as, I am look by lam. Here the pronoun him is the agent, as he performs the action, viz. Issue, and is placed in the objective case; and the personal pronoun I is the object, and is placed first, and is in the nonumative case.

The neuter verb is formed through all its variations like the active verb; but as h does not exprets any action or pattion, but only a date or condition of being, it, contequently, can have no object to be acted upon: it therefore has only an agent, and that always in the nominative cate: as, I am, I among this is in fome influences the neuter verb has a pattive form; thus is in fome verbs which figure a fort of motion, or change of place or condition: as, I am eigen, I now faller, I am ever, I was gone. These verbs partake formwhat of the nature of the pattive verb, though they have still the neuter figurification. The auxiliary am, now, defines the time of the verb.

The two principal auxiliaties have already been declined through all their variations. The auxiliary is loser, through its teveral variations, is placed only before the perfect parti-

ciple; to be is also placed before the present and perfect par ticiple. The other auxiliaries are placed before the verb, o another auxiliary in its original form.

The nature of the other auxiliaries should be just mentioned Do, past time did, expresses the action, or the time of it, witl peculiar force. It is much used in interrogative and negative sentences. It also supplies the place of a verb, and render the repetition of it unnecessary: as, "go and do thou like wife." Let expresses permission, but its chief use is in forming the imperative mode, which it does,

The possibility of performing an action depends upon the power of the agent; and is expressed,

The liberty of performing an action depends upon a free dom from all hindrances; and is expressed,

when 
$$\left\{ \begin{array}{l} ab foliate, \\ conditional, \end{array} \right\}$$
 by the auxiliary  $\left\{ \begin{array}{l} may. \\ might. \end{array} \right.$ 

When the agent expresses the refolution of his own will, to perform an action; it is expressed,

The acceptity of performing an action from some externa abligation, whether it be natural or moral, and what we cal duty; is expressed,

Some of the auxiliaries vary their import according to the person with which they are joined; thus will, in the first person, both singular and plural, promises or threatens; in the second and third persons only foretels: shall, on the contrary in the first only foretels; in the second or third, promises commands, or threatens. But this rule regards explicative

fentences only; for in internigative fentences generally the reverse takes place; thus, I will write, we will write, they fall write, you feelt write; their promite, command, or threaten; but, I feelt write, we feelt write, they will write, yo will write, capiels event only, and fimply foretel. The verb to will is quite a different word from the auxiliary out, and is formed regularly; as, I will, thou willed, he willed or wills.

The auxiliaries could, fooded, would, may, might, are uted in forming the subjunctive made. The auxiliary may has so variation.

When two or more verbs or auxiliaries, or both, are joined together, the first only of them is varied according to perfound number, time, and mode.

Before we proceed to irregular verbs, it may be necessary to lay a few words concerning, what are called, by grammarians, contracted verbs.

Vorbe which and in the other, we the fit in forming the pattime active, and the participle perfect or pattive, often change the degree (which all regular verbs and in, in these torms) into r; are feebed, feebe; paried, parter mand, marer amitting also one of the double contourning thereind, divide; prefled, pref.

Some verbs that out in we believe the contraction, change the we into fo as, because beefly in we, lett.

Most contracted verbs have the entire as well as the contracted form; and the entire form is always to be preferred to the contracted; which latter is only a corruption of the verb, and an error in the rules of grammar, introduced into convertation for the take of a more agreeable found. This is the reation of the contraction of the verb of the fecond perforingular, which was originally written lovedell, turnedell q but is now contracted into lovedel, turnedel, and the third perion, which was formerly lovedel, turnedell, is now in most alylos written loves, turner.

laus-

IRREGULAR VREES are next to be confidered. In all regular verbs the indefinite past time active, and the participle perfect, or passive, are formed by adding to the verb cd, or donly when the verb ends in it as, turn, turned; love, loved. Verbs which vary from this rule are called irregular verbs.

The English language being compounded of the Saxon, and Norman French, must necessarily particle of the nature of both; but the formation of all our verbs is derived from the Saxon.

· All our irregular verbs are monosyllables, except the compounded ones; and are generally the same verbs which are irregular in the flaxon.

There are three classes of irregular verbs. The first class consists of those verbs which are become irregular by consmellon, and either have the present and past time active, and participle perfect, or passive, all exactly alike; or else vary in the formation of the past time, and participle, from the present, by shortening the diphthong, or changing the dist the end of the verb into t. The second class of irregular verbs are those that in the past time and participle end in gbt, and change the vowel or diphthong of the present time into as or as. Irregulars of the third class form the past time by changing the vowel or diphthong of the present; and form the participle, by adding the termination in, with generally the change of the vowel or diphthong.

Irregular Verbs of the First Class, which have the Prefent, Past Time, and Participle alike.

Beat,	heat*,	lift",	read,	flied,	split,
burft,	hit,	light",	rent,	flired,	spread,
eatt,	hurt,	put,	rid,	fliur,	thrust,
seilt,	knit,	quit",	lat,	flit,	wat*.
ÇIII,	lei,	•	•	•	

The verbe marked thus v, introughout the three chaffes of tre-gulars, have the regular see well as the irregular turn, in use.

The two first have also beaten and burflen in the participle; and thus they sometimes belong to the irregulars of the third class. The verb light is pronounced short in the past time and participle; so, I have lit the candle; but the regular form is preservable—lighted. The verb read is also pronounced short in the past time and participle: as, I have red, for read.

The following vary in the form of the past time and participle from the present: lead, led; sweat, swet\*; meet, met; bleed, bled; breed, bred; feed, fed; speed, sped; bend, bent\*g lend, lent; rend, rent; send, sent; spend, spent; build, built\*; geld, gelt; gild, gilt\*; gird, girt; lose, lost. The following are formed by contraction: have, had; make, made; see, sled; shoe, shod. And some change the vowel also: as, sell, sold; tell, told; clothe, clad\*; stand, stood; dare, durst.

## Irregular Verbs of the Second Class.

Bring,	brought.
buy,	bought.
catch,	caught.
fight,	fought.
teach,	taught.
think,	thought.
feck,	fought.
work,	wrought.

# Irregular Verbs of the Third Clafs.

lime. Paft Time.	Participle.
l, tell,	fallen.
ike, awoke,	(awaked).
ake, fortook,	forfaken.
ke, thook,	fhaken.
e, took,	taken.
w, drew,	drawn.
llew,	flain.
gat or got,	gotten.
p, (helped),	holpen .
t. (melted).	molten 🗽
Il. ((welled),	iwollen.
	eaten.
r. bare or bore.	borne.
ak. brake or brok	e. broken.
,	ćleave,
	tell, awoke, ake, forfook, ke, took, took, w, flew, flew, fley, fley, fley, fleyed), t, fmelted), t, fwelled), ate, r, bare or bore,

· as into a or a	fhear,	Past Time. clave or clo fpake or fpc iware or iw tare or tore ware or wo hove", shore,	oke, fpoken, fore, fworn, fore, worn, hoven*, fhorn,
	iteal, tread,	stole, trode,	Rolen or floin. trodden.
	wcave.	wove,	woren.
•	(creep,	crope*,	crept*,
ar into e.	√ freeze,	froze,	frozen.
•	Licetha,	fod,	fedden.
e isto ew.	ice,	ſaw,	feen.
••	bite,	bit	bigten.
Flong into	d chide,	ebid,	chidden.
i fhort.	flide,	hid, slid,	hidden. Aidden.
	abide,	ab <b>ede</b>	no participle.
	climb,	clomb,	(climbed).
	drive,	drove,	driven.
	ride,	rode,	ridden.
	rife,	rofe,	rilen.
i long into o.	fhine,	fhone*,	(shined).
. iong anto or	inrive,	fhrove,	fhriven.
	fmite,	fmote,	fmitten.
	firide,	itrode,	stridden.
	Arive,	itrove*, throve,	Ariven. thriven.
	Cwrite,	wrote,	written.
i long into u.		ftruck,	strucken or stricken.
	cbid,	bade,	bidden.
: Chart into a	J give,	gave,	given.
i short into a.	) fit,	fat,	fitten.
	Cipit,	spat,	spitten.
i short into u.		dug*,	(digged).
ie into ay.	lie,	lay,	lien or lain.
o into e.	hold, <b>do</b> ,	held, did,	holden.
oo into o.	choose,	chose,	done, from detu.
50 ILIC 51	(blow,	blew,	blown.
	crow,	crew,	(crowed).
es into esu.	grow,	grew,	grown.
	know,	knew,	known.
•	throw,	threw,	thrown.
y into ew.	fly,	flew;	flown.
•			The

The following verbs have the participle now formed, without the termination en; except two of them, viz. drunken and bounden; though this was undoubtedly their original form.

Pref	ent Time.	Paft Time.	Participle.
1	Begin,	began,	begun.
	cling,	clang or clueg,	clung.
	drink,	drank.	drunk or drunken.
	fling,	flung,	flung.
	dne,		mung.
	ring,	rang or rung,	rung.
1	Mrink,	firank or farunk	
	fing,	lang or lung,	lung.
	link,	fank or funk,	ſunk.
i fhort into	fling,	flang or flung,	flung.
a or n.	aink,	flun <b>k</b> ,	Nunk.
	spin,	fpan or fpun,	ípun.
l	spring,	forang or forung	, íprung.
•	Ring,	ftung.	flung.
	Amk,	stank or Lunk,	Runk.
	fring,	strung,	Arung.
	ſwim,		
		fwam or fwum,	fwum.
	fwing,	fwung,	iwung.
	wring,	wrung,	wrung.
	Chind,	bound,	bound or bounden.
i long into on.	find,	found,	found.
. Ithis illicon.	grind,	ground,	ground.
	Cwind,	wound,	wound.
a into n.	hang,	hung*,	hong".
🐠 into e.	fhoot,	fhot,	fhot.
i into u.	flick,	Ruck,	fluck.
e into a.	come,	came.	come.
u into a.	run,	ran,	run.
i into •.			
i ilito F.	win,	won,	won.

The following are irregular in the participle only; and even then they do not change the vowel:

Lade,	(laded),	laden.
rive,	(rived),	riven.
fhave,	(Muved).	íhaven.
fhow,	(fhowed),	fbown.
wreath.	(wreathed),	wreathen.
writhe.	(writhed).	writhen.

The following also are irregular in the participle only, which they form in the same manner:

Vol. I. D Bake,

Bake,	hew,	pwe,	hew,	Arew or Arow,
fold,	load,	Iaw,	fow,	wall,
grave,	mow,	fliape,	ftraw,	wax.

These have also the regular as well as the irregular form; and the regular form should always be preferred,

Besides the irregular verbs, there are also others called defective verbs; which are not only irregular in their forms, but also wanting in some of their forms; some have no past time, some no participle, and others neither.

Most of the auxiliary verbs are of this class.

Prefent Time.	Puft Time.	Participle.
Am.	Was,	been.
can, t	could,	no participle.
go,	went,	gone.
may,	might,	no participie.
must,	no past,	no participle.
quoth,	quoth,	no participle.
thall,	should,	no participie.
weet, wit, or wot,	wot,	no participle.
will,	would,	no participle.
wit,	wift,	no participle.

The whole number of verbe in the English language, regular and irregular, simple and compounded, taken together, amount to about 41001 whereof fifty-two are irregulars of the art class, eight irregulars of the second class, and 107 irregulars of the third class, which, with the ten defective verbs, make 177; all the rest are regular verbs, and have the past time active, and participle perfect or passive, formed alike, and ending in d or ed, as was before obscreed. Of the irregular verbs there are not so many as 100, which have different forms for the past time active, and the participle. This has given occasion to introduce a great corruption, by confounding the different forms of the path time and participle with each other, in irregular verba. Thus, the participle is fometimes used for the past time; as, be run, for be run; be drunk, for be drunk; but the past time is very frequently used instead of the participle; as,



I have rode, for I have ridden; I have fet, for fitten; I have get, for getten. This error is frequently committed by our best writers, and the vulgar translation of the Old and New Testament, which is the best standard of the English grammar, is not free from this sault: beld is there often used for belden; is not free from this sault: beld is there often used for belden; bid, sometimes for bidden; and bid, for bidden; and beget is twice used for begetten. This error is, however, an enormous solecism; and the impropriety of it will appear by the abuse of some verbs which have not been so corrupted: as, I have some, for I have some; I have did, for I have done; I have went, for I have gone; which are not a whit more ungrammatical than any other verbs which have the past time, instead of the participle, after the auxiliary have.

In the formation of the present participle, it is to be observed, that if the verb end in a single consonant, following a single vowel, and accented on the last syllable, if it consists of more than one syllable, it doubles the last consonant in forming the present participle; also in every other form of the verb in which a syllable is added: as, cut, cutting; regret, regretting, regretteth, regretted. Verbs which end in e omit the e in the present participle: as, increase, increasing: all other verbs form the present participle by barely adding ing to the verb in its original form: as, turn, turning.

The ADVERB, as its same imports, is added to the verb, and also to the adjective, to express some modification, or other circumstance of the action expressed by the verb, or the quality expressed by the adjective: as, the time, he reads now;—distance, the countries lie wide apart;—relation, they are closely united;—quantity, an exceeding high mountain;—quality, to live soberly;—comparison, they are much alike;—doubt, possibly, perhaps;—assimation, yes, certainly;—negation, no;—demonstration, evidently;—interrogation, how, what;—manner, well, ill;—order, regularly;—place, here, there;—motion, slow, swift.

The adverb in English has no variation, except a few, which have the degrees of comparison; and in these the D 2 degrees degrees of comparison should be furmed by the words more and most: as, right, more right, most right; and not by the terminations or and off, like adjectives: as, right, righter, rightes; though the best writers of the seventeenth century have frequently failen into this error.

Some adverbs, which are derived from irregular adjectives, are also irregular in their degrees of comparison; as the adverb well (which is derived from the adjective good), and has better and bost in the comparative and superlative degrees.

An adverb is fometimes joined to another adverb, to qualify or enforce its meaning: as, very well, mark too large.

PREPOSITIONS are placed between words, to connect them together, and to show the relation between them.

Prepositions originally denote the relation of place, but are now used to denote other relations: as, in, with, through, for, from, by, out, under, to, of, over, &c. Of has the same meaning with from: learn of me, that is, from me: for signifies in the place or stead of another. All the others evidently convey the idea of place, according to the general meaning of the words.

Prepositions are sometimes placed before verbs, and joined to them so as to form but one word; in which case they always after the sense of the verb; as, to stand, signifies a posture—to understand, intends comprehension: uslo, to go, to onigo; so look, to overlook. Sometimes they follow the verb, and are not joined to it; when they no less after the meaning of the verb; as, to give, to give up; to cast, to cast of, to cast down, &cc.

The preposition on is sometimes converted into an a, and that chiefly before the present participle t us, a malking, a going, e.c. which are evidently derived from the phrases. I was on walking, I was on going; that is, employed on that action. Also, twelve a clock, as it is commonly pronounced, but written, twelve o'clock, was originally, twelve on the clock.

CONJUNCTIONS are used to connect sentences together; so as from two or more simple sentences to form one, which is called a compound sentence.

What a simple sentence is has been shewn in page 12. A compound sentence is formed of two or more such simple sentences: 25, "John and Thomas love their book, but Edward is a dunce." This is a compound sentence, formed by uniting the three following simple sentences together, by the conjunctions and and but: John loves his book; Thomas loves his book; Edward is a dunce.

Conjunctions are principally divided into copulative conjunctions, and disjunctive conjunctions. They both serve to connect the sentence; but the disjunctive conjunction expresses an opposition in the sense, as has been seen by the conjunction but. Also the conjunctions or, than, except, unless, although (though), yet, nevertheless, &c. are disjunctives.

INTERJECTIONS, though reckoned one of the parts of speech, are only a kind of natural sounds, thrown into a sentence by the speaker, as the result of his feeling, and to express his own affections: as, O! alas! &c.

When the interjection O is placed before a substantive, it shows that an address is made to that particular person or thing of which the substantive is the name; and the substantive is, in what in Latin is called, the vocative case.

### SECT. IV.

#### OF SYNTAX.

STRIAN is the right ordering and framing of words, in order to form fentences with grammatical propriety. And for this purpose, words are fuld to govern, or agree with each other.

When a word governs another, it canfee that particular word which it governs, to be in fuch a particular number, gender, case, person, time, or mode.

When a word agrees with another, it is in that particular mode, number, case, &c. which is required by the word that governs it. Thus; "And fire shall bring torth a Son, and thou thait call his name letus a for he thall fave his people from their fine."-Matt. i. 21. In this fentence the is a pronoun of the third person, singular, seminine gender, and ought to agree with the subject foregoing, namely, the Virgin Mary 1-diall bring, the future time of the affive verb bring (referring to the time of the birth of the child), the third person, singular number, to agree with the promoun site, and Indicative mode, as it timply declares the event; forth, a preposition added to the verb bring, and which alters its meaning from bring, to bring forth, which figuifies to bear or produce : - a, the indefinite article .- lon, main fulflantive. fingular number, matculine gender, objective cate is - and, a conjunction conflative, connecting the following and force going fentences together; -- then, the pronoun of the fecond perion, fingular, and agent of this fentence; -/hali call, the future time of the active verb call, fecond perion, lingular, being governed by thou, indicative mode, as it only foresteld or declares the name of the child, but does not command it, - bu, a possessive pronoun, third person, singular, materime gender, governed by the noun Son .-- name, a subflantive

CORMINAL.

common, and the object of the lentence;—Jesus, a substantive proper, masculine gender, agreeing with the noun Son, and nominative case;—for, a copulative conjunction;—be, a pronoun, third person, singular, masculine gender, nominative case, being a substante for the noun Jesus, and governed by it, and the agent of this sentence;—shall some, the future time of the active verb (agreeing in time with the other verba in the sentence, which are all suture), third person, singular, governed by the pronoun be, indicative mode;—bis, a possessive pronoun;—people, a piural noun, neuter gender, objective case;—from, a preposition, shewing the relation between the nouns people and sins;—their, a possessive pronominal adjective, and as such joined to the piural noun sins, objective case.

SENTENCES are either fimple or compounded,

A simple sentence hath but one subject, or agent, and one werb in the indicative, imperative, or subjunctive mode; and consists of three parts, if the verb be active; the agent, the attribute, and the object: as was seen page 12.

A compound fentence confifts of two or more simple sentences united together by the aid of conjunctions, as hath been shewn before; or by relatives, as will be seen bereaster.

As language and ftyle is only an affemblage of fentences, too much attention can hardly be bestowed upon their construction. We will therefore take a view of the rules of English Syntax, as they regard the several parts of speech respectively.

The ARTICLE, as hath been feen, if definite, is placed before both the fingular and plural mount as, the man, the men: the indefinite article a is placed before the fingular noun only: as, a man.

The Substantive governs both the pronoun and the verb: for if the substantive be plural, it requires both the pronoun and verb to be plural also; and if singular, they must also be singular: as, "nothing has so much exposed men of learning to contempt and ridicule, as their ignorance of things which are known to all but themselves."—Johnson's Rambier.

Rambler. Example of the fingular: "Senses speaks in the natural and genuine language of a man of honour, when be declares, that were there no God to see or punish vice, be awald not commit it."—Guardian.

There are some nouns called nouns of multitude, which fignify many, and have the pronoun and verb agreeing with them, either in the singular or plural number; but if they convey a plural idea, the verb and pronoun should be plural likewise; if they convey a singular idea, the verb and pronoun should be singular: as, "the essentially of the wicked bave enclosed me."—Psalm xxii. 16. instead of bash enclosed me. "My people is soolish,"—Jer. iv. 23. instead of are feelish.

Two or more fingular nouns, joined by copulative conjunctions, have the verbs, nouns, and pronouns agreeing with them in the plural number: as, "Shakespeare and Milton wave the most eminent peers of the English nation."

But formetims the verb follows in the fingular number, and refers to each of the preceding nouns taken feparately; as, "fand, and fall, and a mass of iron is easier to bear than a man without understanding."

Nouns of number, weight, and measure, are often used in the fingular form, when they are joined to numeral adjectives; though they denote plurality: as, an hundred thousand, instead of thousands; an hundred pound weight; fix foot; forty fathom.

Nouns, whether of the masculine, seminine, or neuter gender, always govern the same gender in the pronoun: as, "I have a friend, who, because be knows his own sidelity and usefulness, is never willing to fink into a companion." "I have a wife, whose beauty first seduced me, and whose wit confirmed ber conquest."—Johnson's Rumbler.

Every noun in the nominative case belongs to some verb, either expressed or understood, except the case absolute, as will be seen hereaster; and when an address is made to a person, called the vocative case. Thus in the answer to this question, Who conquered the Persians?—Alexander: that is, Alexander conquered them.

Every noun in the possessive cale has also some nound belonging to it; as, St. Paul's, that is, St. Paul's Cuibedral; St. James's, St. James's Palace.

The noun has no different form in English for the shjective case, though this case be founded in nature and grashmar: as, " books bun never teach the use of books."

The Pronoun, being a substitute for the noun, must confequently have the same nature, with regard to the govorument and agreement of houns and verbs.

When two or more pronouns of the fingular number are joined together, to make the plural pronoun agree with them in person, the second person is preserved before the third, and the first person before both: as, be and you did as you were commanded; I, then, and he loft our characters by it.

The neuter pronoun it is employed in a threefold sense: -first, it expresses the subject of any discourse: as, it so happened; who is it?—fecondly, the state of any person or thing: as, how is it with you?—thirdly, the thing that is the cause of any event: as, it was I that did it; it is these that corrupt the mind.

PRONOMINAL ADJECTIVES have some substantive belonging to them, either expressed or understood.

The definitives this, that, in the plural thefe, those, must always agree with their fubftantive in number: thus, "By this means thou shalt have no portion on this side the river." Ezra, iv. 16. "I have not wept this forty years." It should be these means; these forty years. Again, "They are these kind of gods which Horace mentions in his alleggrical velsel."-Addison's Dialogues, ii. on Medals. Here it should be these kinds, or this kind.

The relatives who, which, that, have no variation of gender, and therefore must agree with their antecedent in this respect. For every relative must have a noun or pronoun, to which it refers, either expressed or understood; which is therefore called its antecedent: as, "Who steals my purse, fteals traft."-Shakespeare. That je, the man who fteals try purfe, steals trash.

Who is applied to persons only, and is either masculine or feminine; which is now applied to things only, and irrational animals; that is used both for persons and things, but it should be confined to the latter, particularly in the solemn style; what stands for both the relative and the antecedent: as, this is what was spoken of before; that is, the thing which was spoken of before.

The relative is the nominative case of the verb, when no other nominative comes between it and the verb; but if another nominative comes between it and the verb, the relative is governed according to the sense of the sentence: as, "the God who made me, whose I am, and whom I ought to serve." In the different members of this sentence, the relative is used in a different sense; in the fast member it stands for the nominative case of the verb, having no other nominative case between it and the verb; in the second member it stands for the possession case; in the third member it represents the object.

Every relative is of the fame person with the antecedent to which it refers, and the verb must therefore agree with it: as, "I that (who) speak unto thee am he." John, iv. 22. "Thou that (who) dwellest between the Cherubims." Psalm lxxx. 1.

The relative is often omitted, and understood, without being expressed: as, "the God I serve;" that is, the God culom I serve. The relative should seldom be omitted even in the semiliar style, and never in the serious and solemn styles.

The proper use of the relative consists in the property of presenting the antecedent to the mind of the hearer or reader, without any ambiguity.

The distributive pronominal adjectives each, every, either, always agree with the nouns, pronouns, and verbs in the singular number only: as, "The king of Israel, and Jehosaphate the king of Judah, fat each (king) on his throne, having a (both) put on their robes."—1 Kings, axii. 20. "Every one ought to cherish and encourage in himself this modesty and assume Lhave here measured."—Speciator. Each agni-

Ses both taken diffinctly or separately; either signification the out, or the other, taken disjunctively.

The ADJECTIVE, having no variation of aumber or gen-

The adjective is always placed immediately before the noun: as, a good men, except in the following inflances: first, when something depends upon the adjective: as, "feed one with food convenient for me." Here the relative and the verb are understood: vs, sood that is convenient.—Secondly, when the adjective is emphatical: as, George the Third; "It. John the Divine.—Thirdly, when the verb to be, or any auxiliary belonging to it, is placed between the adjective and the noun: as, "How beautiful are the tabernacles of the Lord of Hosts!" happy shall be be.—Fourthly, when two or more adjectives belong to the same noun: as, " a general irrove and failful."

The article is placed mostly before the adjective, except the adjectives all, fach, and many: as, all the men; fach a man; man; a man. Or when an adjective is joined to the adverbs fo, as, bow: as, not fo large a concern; as good a man; bow fac a fight in this.

Every adjective has some substantive belonging to it, either expressed or understood: as, "the reactor," for the twelve applies.

Sometimes the adjective is used as a substantive, and has an adjective joined to it: as, the greatest evil, the chief good. At other times the substantive becomes an adjective, and has a substantive added to u, and linked to it by a mark of conjunction: as, assumationed, milk-disc.

The VERE, or attribute of a fentence, always agrees with the agent or nominative case.

For every verb, except the participle of the infinitive mode, hath a nominative case belonging to it, either expressed or understood: at, " an ake, as; e, or be for ever fallen;" that it, amake ye, arise ye, bec. And when the verb waltive, it hath, moreover, an objective sale: as " God made man."

The nominative rate in kinglich in proced before the

verb, and the objective case after the verb : except, first. when the agent or object is expected by a pronoun, in which eafr they are often reverted in their order; as, " Whom ye ignorabily good hip, him deduce I more von. . Secondly, when the early is neuter, the nominative rafe is fornetimes placed after it : as, " prefently entered the ement."-Thirdly, when the adverb charge is connected with the neuter verb; as, " there was a min in the land of Uz." Job, 1. 1. Fourthly, when the relatives are used, though in the objective case, they are always placed before the verb, as are also their com; aunds, subserver, subliberer, &c. as, " subsimilarier von And the thirds he selves you feel." Fifthly, when a ferrrence is interrogative, or when a question is alked, the nominative folidws the principal verb, or the auxiliaty: as, loveft that fine? or defilled love me? Sixthly, when the imperative mode is employed, or when any thing is commanded or requested to be flour, tile nominative case follows the verb or auxiliary . as, come than here, or do those come here; or the anythird let with the objective cale is uled: as, let me go; at at he gone. Secretily, when the conjunctions of or death, are omitted, the nominative sufe femetimes follows the airciflary or the verb, and the verb is in the lubjunctive made as, " had be done this he had been tight;" " hage the complete weetly."

The center with expressing no action, but only a state of condition of licing; a consequently can have no objective cate a pressing the object of an action. Whenever a norm follows a neuter week, it either expresses the same idea with the verb, it forms coronastance of the verb; a preposition being understood; as, to fi for a duel; to ride a mile; that it, the space of a mile.

When the pronoun follows the neuter verb to be, it should always be in the nonunative case; as, it must I; it seem be. Except the verb be in the infinitive mode; as, it was thought to be how. Thus, "Thus, "Whom say ye that I am." — Matt. xiv. is comproper; it ought to be, subo say ye, &c.

When a verb immediately follows another verb, the laft

verb should be in the infinitive mode: as, boys love to play: but the following verbs admit of other verbs following them without being in the infinitive mode: bid, dare, need, make, fee, beer, feel, and all the auxiliaries, except be and bave, which have already been spoken of.

The infinitive mode has the nature of a substantive, exprefing the action itself in the abstract, without regard to any person as an agent. Thus the infinitive is employed as a fubstantive in the nominative case: as, to teach is a master's duty; and in the objective case; as, mankind love to learn.

The prepolition for, placed before the infinitive mode, is now become obsolete.

The participle has the nature of an adjective, as the infipitive mode has that of a substantive; and the participle is fometimes joined to a subfantive. like an adjective, merely to denote its quality; and admits of the degrees of comparison: as, a learned man, a more learned man, a must learned man: and the present participle is varied in the same manper: as, a loving father, a more loving father, a most loving fatber.

When the participle has an article before it, and the preposition of after it, it then has the nature of a substantive, expressing the action itself which the verb fignifies: as, "by the preaching of repentance," and not by preaching of repentance, as is erroneously written in the Collect for St. John the Baptist. For when the participle has the article before it, the prepolition should always follow it; and when the preposition follows it, the article should precede it. But the participle may have a preposition before it: which answers to what is in Latin called the gerund: as, " [uftice confifts in punishing the guilty; and in protecting the innocent."

The case absolute is, when a sentence is formed without a finite verb, by the aid of the participle, or infinitive mode. This case is in English always the nominative; and the adverbs of time, when, while, after, &c. which should otherwife be inferted, are omitted: as, "the doors being shut,

Jefus shood in the midst;" instead of, when the doors were shout, sec.

The infinitive mode is often made absolute, when it supplies the place of the conjunction that with the subjunctive mode: 22, "10 legin with the first;" "10 conclude:" that is, that I may begin with the first; that I may conclude.

The participle is also made absolute in the same manner as the infinitive mode: as, "this, strictly speaking, is the lense:" that is, this, if I man speak strictly, is the sense.

ADVERSE have no government. They should always be placed as near as possible to the word which they modify.

Their place is generally before adjectives, after active and neuter verbs, and sometimes between the auxiliary and the verb: as, "He was a very wife prince; he governed mildly; and was reverentially beloved by his subjects."

When two negatives occur in one fentence, they defiroy one another, and are equal to an affirmative: as,

Nor did they not perceive the evil plicht. In which they were, or the sharp paths not feel.

MILTON, P. L. i. 335.

There is no adverb so liable to be misplaced as the adverb only: most of our classical writers have erred in placing this adverb at too great distance from the word which it medifies: thus, it is commonly faid, "they only sought one hour;" whereas it should be, they sought only one hour.

PREDOTITIOUS have a government of case, and in English they always require the objective case after them: as, with her, from me, to him, by us, &c.

When the prepolition governs a relative, is should be placed before the relative; as, "this is he of whom it is written;" though some writers have placed the preposition at the end of the sentence, and separate from the relative, which is always ungraceful, and can hardly be reconciled to the rules of grammar: as, "Horace is an author whom I am much delighted with."

Many of our best writers have committed errors in the use of the preposition, some omitting it entirely when it should be used, others using one preposition for another: as, into for in, to, or unto; for for of; of for on, &c. as may be seen by an attentive perusal of the classical writers in the English tongue.

The noun mostly requires after it the same preposition as the verb from which it is formed would do: as, "the wisest princes need not think it any diminution to (of) their greatness, or derogation to (from) their sufficiency, to rely upon counsel."—Bacon, Essay 20. Here the nouns diminution and derogation, being formed from the verbs diminish and derogate, require the prepositions of and from.

The prepositions to and for are often understood, without being expressed, before the objective case of the pronoun: as, get me a place; pay bim the money you owe them; that is, get for me a place; pay to him the money you owe to them." This is a relic of the Saxon: in which language, those pronouns which are in the objective case in English, are in the dative case; and consequently have the prepositions to and for understood. In or on is also often omitted beforenous expressing time: as, last week; next year; to-morrow: that is, in last week; in next year; on to-morrow.

The prepolition subjoined to the adverbs here, there, where i as, herewith or bereof, therefore, therewith, wherecoith, wherewon, &c. have the construction or nature of a pronoun; but they are now almost obsolete, except in the very solemal style only.

Conjunctions have only a government of mode. Some require the indicative, others the subjunctive mode.

The following govern the subjunctive: first, hypothetical conjunctions: ar, "if thou be the Son of God." Matt. iv. 3.
—Secondly, conditional conjunctions: as, "though he flaying, yet will I put my trust in him." Job, xiii.—Thirdly, distributive conjunctions; "whether it were I, or (whether it were, they, so we preach." I Cor. xv. 11.—Fourthly, concessive conjunctions:

conjunctions; "Unless he wash his stesh." Lev. xii. 6.— Fifthly, exceptive conjunctions; "no power except it were given from above."—Sixthly, the conjunctions less and that, following a verb in the imperative mode: as, "let him that flandeth take heed less he fall." I Cor. x. 12. "Take heed that thou speak not to Jacob." Gen. xxxi. 24.

Here it must be noted, that all the foregoing conjunctions may be used, and often are, with the indicative mode; when the circumstance expressed is of a more absolute and certain nature. It is the circumstance being of a doubtful nature, or expressed under a condition, or supposition, or in the form of a wish, that determines the verb to be in the subjunctive mode.

Other conjunctions of a more politive nature govern the indicative mode.

There are some conjunctions which have other conjunctions belonging to them, and answering to them: as, although (though), yet, nevertheless; subether—or; neither or nor—nor; either—or; as—as; as—so; so—as. As—as express a comparison of equality; as good as another, that is, equal in some or every quality; as—so express a comparison sometimes of equality; "as he is, so shall we be;" sometimes a comparison of quality; "as the one dieth, so dieth the other;" that is, in like manner; so—as express both quality and quantity: as, "Pope was not so sublime a poet as Milton, nor so great a man as Johnson;" neither, nor, and not, nor, express a double negative, as in the foregoing example; either—or, a double distributive, as, either choose ye this or that.

In comparative sehtences, or when different qualities are compared, the case of the latter noun or pronoun is governed by the verb or preposition, which are sometimes not expressed: as, thou art a greater man than be; that is, than be is; you show him more favour than me; that is, than (you here) me." Thus, by supplying that part of the sentence that is understood, the case of the latter noun or pronoun will be understood.

INTEXPECTIONS in English have no government, nor any particular place in a sentence; they are used only to express the speaker's affection; but when they are used too frequently, they rather expose his affectation.

These are the rules of English syntax, in the construction of sentences. But there are also phrases, consisting of two or more words, employed in the formation of sentences; of which the following are the most common:

Ist Phrase: when a substantive or pronoun is placed before a verb active, passive, or neuter: as, I love; be is loved; them art.

ad Phrase: when the substantive follows a verb neuter, or passive; or when the substantive following the verb intends the same thing as the substantive before the verb: as, I am be; Milton is esteemed a classic.

3d Phrase: when the adjective follows a verb neuter, or passive: as, life is short; exercise is offeened subolesome.

4th Phrase: when the substantive follows a verb active: as, to build a bonse.

5th Phrase: when a verb follows another verb: as, they defire to die.

6th Phrase: when one thing is said to belong to another: as, Milton's poems; or the poems of Milton.

7th Phrase: when a substantive is added to another, to explain it more fully: as, St. John the Baptist; King George; Robert Brown, &c. Here the latter noun is said to be in apposition to the former.

8th Phrase: when the adjective or participle is placed before the noun: as, a flac day; a lowing friend.

9th Phraset when the adjective is placed before a verb in the infinitive mode: as, wereby to live.

roth Phrase: when an adverb is used with an adjective, or a verb: as, he writes quick; he is very just.

rath Phrase: when a substantive with a preposition before it, is added to a verb or an adjective: as, he acts with prudence; good for nothing.

rath Phrase: when the quality of a subject is compared with that of another subject; the positive adjective having after it the conjunction as; the comparative the conjunction than; the superlative the preposition of: as, as tall as you; taller than he; tallest of all.

#### SECT. V.

#### OF PUNCTUATION.

Punctuation is the art of making the feveral points, used in seutences, to express the degrees of connexion between sentences and their parts; and to express the stops or pauses, as they are expressed in a just and accurate pronunciation.

Notwithstanding the different pauses in sentences, and degrees of connexion between them, admit of great variety, yet we have but four points by which to express them.

Thus we are often obliged to express pauses of the same quantity, on different occasions, by different points; but more frequently to express pauses of different quantities by the same points.

The doctrine of punctuation must therefore be very imperfect: few rules can be given that will hold good in all cases; but much must be left to the judgment of the writer,

Grammarians have followed the division of the Rhetoricians, who divide all the paules in writing or discourse into the sour following:

The Period, marked thus	•	(.)
The Colon, marked thus	٠	(:)
The Semicolon, marked thus	. •	(1)
The Comma marked thus	_	1

The Period marks a whole fentence, either simple or conpound, making a full and perfect sense, and not connected in construction with another sentence.

The Colon marks the greatest division of a sentence, and is a member thereof; containing a perfect sense, but not a perfect sentence.

The Semicolon is a less constructive part of a sentence than the colon, and does not form a perfect sense, but holds a middle place between the colon and the comma, being a greater pause than the latter, and less than the former.

The Comma marks the least constructive parts of a sentence; or it marks a simple sentence.

The precise quantity of time required at each of these pauses or points is uncertain; as the same composition may be rehearsed in a longer or shorter time; but the proportional quantity of time of the points is as follows: the period is a pause of double the quantity of time of the colon; the colon; the colon is double of the semicolon; the semicolon is double of the comma.

In order to discover the proper use of these points, we must consider the nature of a sentence, as divided into its constructive parts, and the degrees of connexion between these parts: as also the nature of an impersect phrase.

An imperfect phrase contains no affertion, or does not amount to a proposition or sentence, as was seen in page 41.

A simple sentence, as was before hinted, consists of an agent, or subject, an attribute, and (if the verb be active or passive) an object: or it consists of one agent or subject, and one sinite verb; that is, a verb in the indicative, imperative, or subjunctive mode: as, "God made man;" here God is the agent or subject, as he performs the action, viz. made stans: the verb made is the attribute which always expresses the action; and man is the object upon which the action is exercised; that is, the action of creation.

But the subject, or agent, and the attribute, and the object, may each of them be accompanied with several citcum-

frances or characteristics, called therefore their adjuncts; as the motive, place, time, manner, cause, and the like; and these may be connected either immediately, or mediately, to the parts of the sentence to which they belong.

If the several adjuncts are related to the parts of a sentences in a different manner, they are then only so many impersect phrases, and the sentence is simple.

But if the several adjuncts belong to the parts of a sentence in the same manner, they then become so many simple seatences; and the sentence is then compound.

For a compound fentence confills of two or more timple fentences connected together; or it hath more than one subject, and one finite verb.

Thus, if several subjects belong in the same manner to one verb, or several verbs belong in the same manner to one subject, the subjects and verbs are to be accounted equal in number: for every subject, except the case absolute, and the vocative case, must have its verb; and every finite verb its subject; and generally has its point of distinction.

# Examples of the Use of the Comma.

"This single consideration will be sufficient to extinguish all envy in inferior natures." In this sentence confderation is the subject or agent, extinguish the attribute or verb, envy the object; each of which is connected with its adjuncts. The fubject does not mean any confideration indefinitely, but a particular confideration, treated of in the former part of the hillay (namely, the confideration of the progrefs of a human foul towards perfection in knowledge), and here defined by the adjunct, this fingle (confideration). attribute or verb is also connected with its adjuncts; immediately with energy, as the object of the action; and mediately by the intervention of the word energ with inferior natures, the subject in which envy is extinguished; the adverb sufficient is the adjunct of the verb, denoting its power. It is to be observed, that each of these adjuncts belong to the verb in a different different manner; every belongs to it as the object; infinior no surve as the fabject in which the object is extinguished, and fufficient as the power of the verb to produce the effect. The adjuncts are, therefore, only so many imperfect phrases; and the sentence is simple, and admits of no points to distinguish it into parts.

"Methinks, this lingle confideration, of the progress of a finite spirit to persection, will be sufficient to extinguish all envy in inferior natures, and all contempt in superior." Here two new fentences are introduced: the one inferted in the middle of the former fentence, and the other added to the end of it. The former of them, of the progress of a finite fpirit to perfection, is connected with the attribute in the same manner as the agent, or this fingle confideration, for they both express the same idea; and the verb may be joined with either of them, and the fentence have the same sense : as, " the progress of a finite spirit to perfection, will be sufficient to extinguish all envy in inferior natures." The latter sentence, and all contempt in Superior, is connected exactly in the same manner with the attribute as the object in the first sentence is, though it does not convey the fame idea; and may be made the object of the fentence in the fame manner as the former fentence was made the agent; as, " Methinks this fingle consideration will be sufficient to extinguish all contempt in superior. (beings) The first of these newly inserted sentences may therefore be confidered as only another agent: and the latter as another object to the verb, in the first-mentioned fentence. They are therefore so many simple sentences, and should each be distinguished by a comma; and the whole is a compounded sentence.

And again, "A wife man will defire no more than what he may get justly, use soberly, distribute cheeffully, and live upon contentedly." In this sentence, the phrases, get justly, use soberly, distribute cheerfully, and live upon contentedly, are each connected with the subject, he, in the same manner, and in effect, form so many distinct sentences; as, "a

wife man will defire no more than what be may get juftly: a wife man will defire no more than what be may ufe foberly: a wife man will defire no more than what be may diffribute cheerfully: a wife man will defire no more than what be may live upon contentedly. They must each of them, therefore, be distinguished by a comma. They are so many simple sentences, and the whole is a compound sentence.

As fentences themselves are divided into simple and compound, so the members of sentences may be divided into simple and compound members: for whole sentences, whether simple or compound, may become members of other sentences, by means of a connexion.

# The following are marked by a Comma:

First, Simple members of fentences, closely connected together in one compound member or fentence: as in the foregoing example : except, first, when the members are short in comparative fentences: as, in the former part of the last example, "a wife man will defire no more than what he may get justly." These are, in fact, two simple sentences compared by the conjunction than; but, being flort, they are not separated by a comma. Secondly, when two simple members or fentences are closely connected by a relative, and the subject of the anteredent is confined to a particular fense: as, " the man who is possessed of this excellent frame of mind, is not only easy in his thoughts, but a perfect master of all the powers and faculties of his foul."-Spectator. In this fentence, the man, is connected to the following fentences by the relative which restrains the idea of the antecedent to the sense here mentioned.

Secondly, the cafe absolute: as, "the doors being thut, Jelus flood in the midft."

Thirdly, nouns in apposition, when confisting of many terms: as, "Alexander, the great, cruel, and unjust."

Fourthly, the vocative case, or when an address is made to a person: 4s, "This said, he formed thee, Adam: thee, O man."—Milton.

Fifthly, when there are more than two nouns, or adjectives, connected by copulatives or disjunctives; or when there are only two, if the conjunction be understood: as, "Raptures, transports, and ecitaties are the rewards which they confer, sighs and tears, prayers and broken hearts, are the offerings which are paid to them."—Spectator.

Sixthly, a circumstance of importance, though only an imperfect phrase: as, "the principle may be defective or faulty; but the consequences it produces are so good, then, for the benefit of mankind, it ought not to be extinguished." Spectator.

Lastly, the participle with something depending on it: as,

"Now morn, her rosy steps in th' eastern clime

Advancing, sow'd the earth with orient pearl.

MILTON.

The Semecolow is used when a sentence, or member of a sentence, requires a greater pause than a comma, yet neither forms a persect sense, nor a persect sentence; but is followed by some other member, or sentence, with which it is closely connected; as,

"To look upon the foul as going from firength to firength, to confider that she is to shine for ever with new accessions of glory, and brighten to all eternity; that she will be still adding virtue to virtue, and knowledge to knowledge; carries in it something wonderfully agreeable to that ambition which is natural to the mind of man."—Spectator.

This compound fentence is divided into three principal parts by the semicolon: each part requires a greater pause than a comma; but neither of them expresses perfect sense, or forms a perfect sentence, being closely connected in sense with each other.

The Colon is used when a sentence, whether simple or compound, requires a greater pause than a semicolon: it always forms a perfect sense, and would by itself form a complete sentence, but is followed by another member, or sense sence, making the sense more full and complete: as,

" Were

"Were all books reduced to their quinteffence, many a bulky author would make his appearance in a penny paper, there would be feares any fuch thing in nature as a folio; the works of an age would be contained on a few flielves; not to mention millions of volumes, that would be utterly annihilated."—Spectator. No. 184.

This fentence is divided into four parts by the colon; the first and last parts are compound members, divided by the commes, the fecond and third are simple members.

Bach of their parts contains perfect fonfe, and would also form a complete fentence, if the other parts had not been joined to it.

The colon is also used when a semicolon goes before, and a greater pause is required; though the sentence be not complete; also when a speech or an example is introduced.

The PRHIOD is used when a sentence is so far finished as not to be connected in construction with the following sentence; and marks both perfect sense, and perfect sentence: as,

"Man, confidered in his prefent flate, feems only fent into the world to propagate his kind. He provides himfelf with a fueceffor, and immediately quits his post to make room for him."—Speciator.

These are two perfect fentences, divided from each other by the period, and full-divided into simple sentences by the comma. The first of these two sentences represents the apparent end of man's mission into this present world; namely, to propagate his kind; the second shows the real confequence of his residence here; begetting a successor, and making room for him. They are entirely distinct sentences; unconnected in construction with each other, and wanting nothing to make each perfect both in sense and sentence.

Befide the four foregoing points, used to express the paules in discourse, there are three others, which also affect the modulation of the voice: namely,

The	Note of Interrogation, marked thu	•	(	1	)
The	Note of Admiration, or Exclamatic	n, marked th	) eu	ľ	)
The	Parenthells, marked thus -	•	(		)
	1		T	Ħ	A

The Note of Interrogation is used when a question is asked: as, "Would an infinitely wise Being make such glorious creatures for so mean a purpose? Can be delight in the production of such abortive intelligences, such short-lived reasonable beings? Would be give us talents that are not to be exerted? Capacities that are never to be gratified?" Spect. These are all interrogative sentences, and as such, are marked by the interrogation point.

The Norm of Aumeration, or Exchanation, is used to mark the speaker's admiration, and any sudden passion: as,

#### " And fee!

'T is come, the glorious morn! the fecond birth
Of Heaven and earth!"
THOMSON'S WINTER

Both these points mark an elevation of the voice. The length of time required by them as pauses is uncertain, and may be equal to that of a semicolon, colon, or a period.

The PARRYHESES is used to enclose a word or sentence, inserted in another sentence; which is not necessary to the sense, nor does it at all affect the construction: as, "Pompey on the other side (that hardly ever spake in public without a blush) had a wonderful sweetness of nature." This point marks a moderate depression of the voice, with a pause some what greater than a comma.

There are also other marks used in writing, which, though they do not affect the voice as pauses, yet are often necessary to the sense; the principal of which marks we shall just mention.

The Arostronia, marked thus ('), is only a comma placed at the head of a letter, and fignifies either that fome letter or letters are left out for a quicker pronunciation; as, I'll, for I will; be don't, for be does not: or else it marks the possessive case; as, John's book.

The ACCENT (') is placed over a vowel to denote that the word is accented on that syllable; as, Com-pre-bin-fion.

' Vol. I. G

The Breve ( ), placed over a vowel to fignify it should be founded short: as, Put-ry.

The CIRCUMFLEX ( ), placed over some vowel to shew that it is to be pronounced long: as, dispute.

The CARET, of the same form with the circumslex, but placed beneath the line, to shew that something is omitted which is inserted over the line: as, this is be.

The DIALYSIS ("), or two points placed over two vowels in a word, to shew they are to be parted, not being a diphthong: as, Duël.

The HYPHEN, or note of conjunction (-), being a straight line, used to connest compound words together: as, Heart-breaking; Book-keeper. And when inserted at the end of a line, it shews the word is divided according to its syllables: as, diffinguish.

The INDEX ((4), or hand, pointing to fomething remarkable.

The ASTERISM (\*), or Star, directing to some note in the margin, or at the bottom of the page. Several of them together denote something desective, or improper to be repeated.

The OBELISK (†), is used to refer to a note like the foregoing. And in some dictionaries it denotes the word to be obsolete.

The PARAGRAPH (¶) marks a division of sentences under one head. It is used chiefly in the vulgar translation of the Bible.

The Section (§) shows a greater division than the paragraph.

The CROCTHETS ([]) include a word or fentence explanatory of what was mentioned before.

The QUOTATION ("-") is a double comma (the first reversed), and placed at the beginning and end of a sentence, or sentences, taken from another author.

#### A PRAXIS;

## Or Examples of Grammatical Refulution.

## JOHN, IV.

- 2 When therefore the Lord knew how the Pharifees had heard that Jesus made and baptized more disciples than John;
  - a (Though Jesus himself baptized not, but his disciples;)
  - 3 He left Judæa, and departed again into Galilee.
  - ▲ And he must needs go through Samaria.
- 5 Then cometh he to a city of Samaria, which is called Sychar, near to the parcel of ground that Jacob gave to his fon Joseph.
- 6 Now Jacob's well was there. Jefus therefore being wearied with his journey, fat thus on the well: and it was about the fixth hour.
- 7 There cometh a woman of Samaria to draw water: Jesus saith unto her, Give me to drink.
- I When is an adverb of time; therefore, an adverb with a preposition added to it; the, the definite article; Lord, common noun, fingular number, malculine gender, nominative cate, being the agent of the fentence; know, the verb neuter, third person, singular, governed by the noun Lord, and agreeing with it, past time, indicative mode, and the attribute of the sentence; bow, an adverb of manner; the, definite article; Pharifees, noun common, plural number, nominative cale; bad beard, verb neuter with the auxiliary bad, plural, third person, past time, indicative mode, governed by Pharifees; that, a copulative conjunction; Ye/us, a proper name, maleuline, nominative case, and the agent of the sentence; made, and baptized, two verbs active, third person, singular, past time, indicative mode, connected with each other by the copulative conjunction and, and are the attribute of the fentence; more, an adverb of comparison; disciples, noun plural, objective case, and the object of the sentence; than, comparative con-

comparing the number mentioned in the foregoing fentence with that of the following; as, baptimed more dijerples, than John (did); John, a proper name.

- s Though, a disjunctive conjunction; Jefus, a proper name as before; bim/elf, the objective pronoun of the third person fingular, matculine gender, joined to the fingular subfluntive felf, to express an exclusive emphasis; beprised, verb active, third person, singular, past time, and indicative mode, though it be governed by the conjunction though, for it is not of a doubtful, but absolute nature, declaring that Jejus did not baptime any; it forms the attribute of the fentence to the agent Jefus; not, a negative adverb, added to the verb, and altering its fense, the potleflive pronoun any being understood; but, a disjunctive conjunction, corresponding to the former conjunction thenge, and expressing an opposition in meaning a bis, the possessive pronoun, third person, singular, masculine gender; disciples, the plural substantive, nominative case, the auxiliary (did) being understood : as, bis diferples did. whole verse is included in a parenthesis, and is not connected in fense, or construction, with the rest of the chapter.
- 3 He, a pronoun of the third person singular, masculine gender, nominative case; used as a substitute for the noun Josus, and governed by it; lest, a verb active, third person, singular, governed by the pronoun be, past time, indicative mode; Judan, a proper name of a city, objective case, as it forms the object to the sentence; and, a copulative conjunction; departed, a verb neuter, third person, singular, governed also by the pronoun be, past time, indicative mode; again, an adverb; into, a proposition; Galder, a proper noun, objective.case, governed by the preposition into.
- 4 And, a copulative conjunction, expressing an addition; be, a pronoun as before, agreeing with its antecedent noun felus; muft, an auxiliary, denoting necessity, and having no variation; needs, an adverb; go, a neuter verb; through, a proposition; Samaria, a proper name for a country, objective case, being governed by the preposition through.

z Then, an advertised time; cometh, a neuter verb, governed by the pronoun & in perion and number, and placed before it. as it fometimes the cale when the agent is a promount indicative mode, and prefent time (improperly, for it flould be in the path time; as, then same he); he, a pronoun; so, a prepolition; of the indefinite article; eith, a common noun. tingular, neuter gender, objective cafe, being governed by the prepolition to a of a perpolition a Sameria, a propor name, tingular, objective cate; which, a relative, agreeing with its unteredent sites in the neuter verb to de prefent time, fingular, third perfon, indicative mode; relied, the perfeet participle of the neuter verb to call, being placed after the auxiliary is Sychar, a proper name of a city, nominative cale, being placed after the neuter verb, called; near, an adverb of differences so, a proposition s soon the definite articles. served a common noun, lineular, objective cafe, governed by the prepolition to a still preparation; ground, fubiliantive common, objective cate, governed by the prepotition of; ther, a relative, agreeing with its autoredent, the parcel of resunds Yours, a proper name of the patriarch, mafculine, nominative calc; gare, a verb active, third person, singular, patt time, indicative mode, governed by Jacob, the same us Jacob gave that; m, a prepolition; Mr, a policilive pronoun, agreeing in perion, number, and gender, with the noun Jacob, and goseened by it, and in the policilive cale to thew the relation of policition between Yarel and fee; fee is a common noun, fingular, maleuline gender, objective cate, governed by the prepolition to: Yorks, a proper name, put in appolition to jon; that is, in the lame cafe, and governed by the fame prepofition //.

o Now, an adverby Joseff, a findinative proper, possessive case; well, a common noun, singular, nominative case, the tame as the well of Joseff; seen, the neuter verb to be, third person singular, past time, indicative mode; there, an adverb of place; Josef, a proper name; therefore, an adverb with a preposition, the same as there and for, it has the construction

of a pronoun; being, the prefent participle of the neuter verb to be; wearled, the perfect participle of the neuter verb to weary, being placed after the participle of the auxiliary to he, which, as has been thewn, in all its forms requires the prefent or perfect participle after it; with, a prepolition; bis, a poffeffive pronoun, third perfon fingular, mafculine gender, Randing for the possessive case of the noun Jefus, journey, a Substantive fingular, objective case, governed by the preposttion with; fut, a neuter verb, third person, fingular, past time, indicative mode, governed by Jefus; thus, an adverb of manner, improperly inferted in this place, as it refers to the manner of fitting, or the pollure, whereas no particular posture or manner of sitting is mentioned, either before or after this fentences on, a propositions the definite artieles well, a common noun, fingular, objective cafe, governed by the preposition out and, a conjunction copulative : //. the usuter pronoun, nominative cafe, flanding for the time of the day; was, the neuter verb to be, third perfou, fingular, puft time, indicative mode, governed by the neuter primoun // s about, an adverb; the, the definite article; flath, an adjective; hour, a common fubitantive fingular,

There, an adverb; someth, the neuter verb, third perfon, fingular, indicative mode, and prefent time, though it flundle be the past time, as the event here mentioned was evidently past, and in the seventeenth verse of this chapter the woman of Samaria is spoken of in the past time; as, "the woman indivered and said;" a, indefinite article; woman, a substantive common, shoular, seminine gender, nominative ease, being the agent of the sentences though placed after the verb; of, a preposition; sumaria, a substantive common, singular, objective ease, governed by the preposition of; to draw, the infinitive mode of the verb draw; wover, a common substantive, singular, Jesu, a proper name as before; such, a neuter verb, third person singular, governed by Jesus, and present time, improperly for the past, as this should also be as it stands in the tenth verse of this chapter; "Jesus answered and fald

unto her;" unto, a prepolition; ber, a pronoun, shird person singular, seminine gender, objective case, standing for the woman of Samaria; give, a verb active, second person singular, imperative mode; me, a pronoun, sirst person singular, objective case, standing for Jesus, and governed by the verb in the imperative mode, the word water being understood; to drink, the infinitive mode of the active verb; it is here made absolute, supplying the place of the conjunction that with the subjunctive mode: as, give to me that I may drink.

#### SECT. VI.

#### OF ELOCUTION.

ELOCUTION is the art of reading or speaking with propriety and elegance; or delivering our words in a just and graceful manner, untainted with pedantry or affectation, and uncorrupted with any provincial found.

Few people need be told the necessity of a graceful elocution. All will allow, that what a man has occasion daily to do, should be done well; yet so little attention has sometimes been paid to this accomplishment, even by those from whom (from their profession as public speakers) we have been led to expect a perfect model of the art, as hath tended greatly to eclipse all their other merits, however great; while others, of inferior attainments, by the help of a tolerably good style, and a just elocution, have risen to a considerable eminence.

A graceful elocution is to a good style, what a good style is to the subject matter of a discourse, an essential ornament. For if the subject of a discourse be ever so interesting, and the speaker's knowledge ever so prosound, without a correct style, the discourse must suffer greatly in its reputation; and though the speaker's abilities be great, and the style good, with a bad elocution,

elocution, it will fare little better. So great an effect have these exterior accomplishments upon public taste.

The first rule in Elocution, as in Rhetoric, is to follow narrure. All other rules, without a strict regard to this, will only produce the affected declaimer, and not the graceful speaker. The excellency of this rule, and the affectation of some modern examples of eloquence, have induced some to disregard all other rules as superstuous; and to imagine that this gule alone, in a person of good sense, and custivated taste, is sufficient to form a public speaker. This, however, is an error. But it is necessary to observe the effects of nature, in order to distinguish between them, and those of arbitrary custom, or false taste; and to observe the various ways by which nature expresses the several passions, emotions, and perceptions of the human mind: in order to which, much assistance may certainly be derived from the following particular rules:

rule. This confifts in giving a clear and full utterance to all the founds, both fimple and complex. For this purpose, the nature of those founds should be well understood, and much pains taken to correct any faults in the pronunciation. Sometimes a fault in articulation is ascribed to a natural defect in some of the organs of speech, when it is the effect of bad example, or inattention only. Many of these saults concern the sounding of the consonants. Some cannot pronounce the letter 1, others the simple sounds, r, 1, 1b, fb; others omit the aspirate b. These may be corrected by reading sentences chosen for that purpose, wherein these sounds frequently occur; and by constantly guarding against them in conversation.

The other fault in articulation confiss in the confusion and cluttering of words together. Most people, who have not learned the art of speaking, have a habit of uttering their words so rapidly and indistinctly, that it is impossible for them to give any emphasis to their words, or natural tone to their sentences; though they may pronounce every word plainly.

The most effectual means to conquer this habit are, to read aloud passages chosen for that purpose, which abound with long and unusual words; and to read much slower than the sense and just speaking would require. Aim at nothing higher till you can read distinctly and deliberately.

a. Let every word be presented with property. This is a most necessary rule, as errors in pronunciation are more frequently committed, and less guarded against than any others. Faults in pronunciation are innumerable. Some of them are the following: omitting the aspirate b where it should be used: as, our for bour; and using it where there should be none: as, begg for egg: confounding and interchanging the w and w; pronouncing the diphthony on like an, or os; and the vowel i like si, or e; and cluttering several consonants together, without regarding the vowels. These errors, and many others too numerous to mention here, must all be carefully guarded against, by every person who would be thought a correct speaker.

It is difficult to point out any standard by which the propriety of pronunciation is to be determined. Profound scholars generally make the etymology of the word the rule of pronunciation, and thus bring upon themselves the charge of pedantry and affectation, by a delivery altogether novel to While, on the other hand, the mere the rest of mankind. man of the world, notwiththanding all his other accomplishments, often retains to much of his provincial dialect, as justly to exclude him from the honour of being the pattern of a just pronunciation. This excellency is perhaps to be found in those only who unite those two characters, and who, to the correctness of true learning, add the elegance and ente of genteel life. An attention to fuch models, an intercourfe with the solite world, and a regard to the etymology of the words themselves, are the best rules that can be given, to correct any errors in pronunciation, and to guard against any peculiarities of provincial found: which every person should endeavour to avoid, who is supposed to have seen too much of the

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would, to tetain the peculiarities of the diffrict in which he was born.

- 3. Let every word of more than one fillable be presented with its proper ACCENT. Many writers have lake it down as a fundamental rule, that the accent of words in the English language should be thrown as far back as possible from the end of the word. A very erroncous rule? and one which has no foundation in the English language; for many words in the English have the accent on the last syllable, and the generality of them have it on the second or third syllable from the end, but a very few on the fourth syllable from the end of the word. The best rule that can be given for this precept, is the foregoing; namely, a strict attention to the best examples; always observing that the accent is not to be determined by any rules of quantity, but by the number and nature of the simple founds.
- 4. The pronunciation should be bold and forcible. Many public speakers deliver their discourse with such a fairt and soeble utterance, and seem to wholly unconcerned with their subject, that their words may be said rather to drop' from their lips than to be delivered by them. This seldem tails of producing the same unconcern and indifference among their auditory. Inanimation is a principal fault: a speaker without energy is little better than a lifelets statue.

To remedy this evil, inure yourleft, when reading, to take in as much breath as you can with eafe contain, and to expedit with vehemence, in uttering those founds which require an emphatical pronunciation; read aloud in the open air, with all the energy you can command; preferve your body in an erest attitude; let all the founds, both vowels and confonants, have a free, full, and bold utterance. Practite these rules with peateverance, till you are mader of a bold and manly delivery,

But in acquiring an energy of speech, the following caution is necessary, namely, that the speaker avoid the opposite extreme, of running into a passionate and distracting vocateration. This exists among those speakers, who value nothing above

tha

the admiration of the vulgar. There, as Shakerpeare has justly observed, "offend the judicious bearer to the foul, by tearing a passion to rags, to very tatters, to split the ears of the groundlings." Cicero compares such speakers to cripples, who get on horseback because they cannot walk they believe, because they cannot speak.

C. Lourn to acquire a graceful wariety, both in the beight and sows of the woire. It is owing to the neglect of this rule, that we daily hear fuch languid and unaffecting difcourfes. Speakers, who deliver their tentiments, or read their compofitions in a dull, that, intipid manner, whatever other merits they may pollets, feldom convince or affect their auditors. This tame unmeaning mode of delivery, to univerfally prevalent, is called a menerony; and confitts in one unvaried tone of delivery. Most people, in familiar convertation, can deliver their thoughts with fome variety, both in the tone and the height of their voice, which they generally modify according to the nature of their difcourfe; yet the fame perfous, when required to read any composition, immediately assume a dry, uniform manner of delivery; as though reading and convertation were to be performed in quite a different manner from each other: whereas, the fame fentences, whether delivered ipontaneoutly by the ipeaker, or read by the leeturer, thould always be delivered with the fame tone, and on the fame key, notwithtlanding all that has been faid by superficial critics to the contrary.

A perform of a moderate capacity will, therefore, he able to alter the tone, as well as the height of his voice, as it may be necessary. Different species of speaking, require different modifications of the voice. Different characters, in different tituations, speak in very different keys. The vagrant when he begs, the soldier when he gives the word of command, the watchman when he announces the hour of the night, the senator when he harangues, the lover when he whispers his tender tale, differ as much in the key as in the tone in which they speak. The same person also, in the same situation,

may have occasion for all the variety of tone and diversity of voice: as, in the support of an argument, the relation of a story, the command given to a servant, a lamentation, an exclamation of anger, and many other cases, require not only different tones, but different elevations of the voice. Reading, therefore, in which all the varieties of expression in real life are copied, must have continual variations in the height of the voice.

To acquire the power of changing the key on which you speak, accustom yourself to pitch your voice in different keys, from the lowest to the highest notes you can command; reading, as exercises on this rule, such compositions as abound with a variety of speakers, observing the height and tone of the voice necessary to each sentence, and changing them as the nature of the subject requires. This will give you such a command of voice, as is not to be acquired by any other method.

6. Distinguish the more signisticant words in overy sentence by their proper EMPHASES. The emphasis serves to point out the precise meaning of a sentence, shews how one idea is connefted with another, gives to every part of a sentence its proper found, and conveys the fenfe of the whole to the mind of the hearer. It also expresses the opposition between the parts of a fentence, where the fense is pointed. Sometimes the emphasis is double, and sometimes treble in a sentence. Emphasis serves likewise to express some particular meaning which does not arise from the words themselves; as in this flioit sentence: "Did Alexander conquer the Persians?" This simple question may have three different meanings, according to the intention of the speaker; and the emphasis has, consequently, three different places: as, when the speaker knew that the Persians were conquered, but did not knew by whom, then the emphasis is placed on the word Alexander: as, "did Alexander conquer the Perfians?" When it is known that Alexander attempted the conquest, but the iffue is not known, the emphasis is then placed on the word conquer: as, "did Alexander conquer the Persians?" When it is known that he conquered the adjacent countries, but it is not certainly known that he conquered the Persians, the emphasis is placed on the word Persians: as, "did Alexander conquer the Persians?"

There are four ways by which the emphasis of a sentence is generally destroyed, or misapplied. First, by placing so strong an emphasis on any one word, as to excince all the star words in the sentence from being in any degree emphasis; which they often require; for, as was before emphasis is sometimes double, and sometimes are a sentence. There are also, of emphasis in the sentence some which require a more forcible some the sentence is an error which many animated speakers.

Secondly, by placing too great at employed or particles, and those words of femore was though sometimes proper, yet it is in the femore was though sometimes proper, yet it is in the femore was the femo

Another way by which emphasis a second in one uniform musical tone, when a realled reading meleciacly. An agree attention; but to submittee one attention to all the grant one exclusion to all the grant of the effect only or great pages.

Lastly, the emphasis a rise passes of the fentence. This is the more to be committed, and are the reader be not perfectly and full meaning of every and full meaning of every and full meaning of every difficulty of the more difficulty of the emphasis cannot be a second which is the work which is the work which is the work and the second second

To speak was a part of the same of the same of

is necessary than previously to enter into the meaning and spirit of every sentence; and to express it as nearly as possible to the manner in which we express ourselves in conversation: for, in familiar discourse, we generally express ourselves emphatically, and place the emphasis properly. As to artificial help, such as distinguishing words by particular characters, they generally mislead rather than assist the reader, by confining him to a particular word or sentence, which he generally overstrains.

7. I. carn to acquire a just variety of pause and cadence. The pauses consist of those certain stops, which are used both in reading and conversation, and which are always necessary to the sense. The cadence is that fall of the voice which is generally directed to be made before every full stop.

There are principally two faults committed with regard to-paules. The first, and one of the worst faults a speaker can have, is to make no other paules than what are necessary for breathing. Such speakers or readers make no distinction between a good speaker and a quick one; and seem to consider reading quick the same thing as reading well. But, without pauses, the sense must always appear consused and obscure, the meaning often be misunderstood, and consequently the energy of the piece wholly lost.

The next fault confifts in a too mechanical attention to the stops or pauses used in printing. These, though very proper in writing, are often unnatural in speaking; for, as was observed in Functuation, the doctrine of points is very imperfect; the variety of pauses required in discourse is so great. A strict regard, therefore, to these points has been one chief cause of monotony, by using the reader to an uniform sound at every imperfect break, and an uniform cadence at every period. The use of points is, to assist the reader in discerning the grammatical construction; not to direct his pronunciation. In reading, it is often necessary to make a pause where the grammatical construction requires none, for the sake of pointing out the sense more strongly, preparing the audience for what

by the manner in which we utter our words, the form of the countenance, and other well-known tights. And even when we deliver our thoughts on any left interesting subject, and when the more violent emotions are not excited, some kind of feeling accompanies our words, which should always have its proper external expection. These exterior expections are the effect of nature alone, and every judicious imitation of it in a speaker will always appear graceful and pleasing; none can deserve the appellation of a graceful speaker, till, to a distinct attendation, a perfect command of voice, and a true emphasis, he can add the various expressions of the passions and emotions of the mind.

It is impossible to lay down any fet of rules by which the speaker may form these outward expressions, as they must be an various as the passions they indicate; the following general direction is the only one that can be depended upon to-

In acquiring this accomplishment, as all others in this art, the fundamental tule is, to fallow nature. Observe in what manner the several emotions, or passions, are expressed in real life, or by those who have with great labour and taste acquired the happy power of imitating nature; and either follow the great original herself, or the best copies to be met with, always observing the caution given by Shakespeare; ~ \*\* O'erstep not the modesty of nature.\*\*

More is to be learned by a fliret attention to good examples than is perhaps imagined. Example has as much the advantage of precept, as practice has of theory; and many, who have arrived to great perfection in this art, have candidly acknowledged it to be more the effect of unitation, than any theoretical rules.

In order to apply the foregoing rules to practice, it is abfoliately in effect to go through a regular course of exercises;
beginning with such as are most easy, and proceeding by flow
advances to those that are more distinctly. For it the reader
cannot deliver with property the plain sentiments of simple
marrative, and didactic pieces, how can it be expected be flighted.

manufacture in the Committee of the Comm aire and a man and a management Secretar recognition of the Contract of it is the new --- --- --- --es, de grando mor de como en como en ings and forcing of the same of the same of the same greet with the last section is the last section in mu. Beam was the see was true in lider, 1986 in August States in August States and August States minima. This is the second of iocurica usa allegate attitue a tita allegate a tion with the control of the control ared vi....z Then the distant to the first terms of the second s vered, his ferral in the in the control of the cont البيسين الدائر بالمال المستحدد المستحدد المالية المالية المالية المالية المالية المالية المالية المالية المالية CDS. icumatum. ... pailions, teatings. .... intention. .= \_\_\_\_\_ --- · as often is convenient in the conis perion. He in . . . . a memory. In the supplement nory, and frequent that .... ling it. It enquies the letter is a reining and laut it iit i.eta ii. Tat I.

the ideas which he is to express. It gives him a previous knowledge of the several inflexions, emphases, and tones, which the words require. And by not having his eye confined to the book, it relieves him from the school-boy habit of holding down his head, and, consequently, reading in a different key and tone from that of conversation; and leaves him at full liberty to express his own seelings, by all the varieties of countenance and gesture.

It generally requires some time, and many and frequent exercises, before the student can be brought to consider reading in the same light as conversation; and be persuaded that it should be condusted in the same manner. There is, more or less, in all people (except in a very sew accomplished speakers), an artificial uniformity, which always diffinguishes reading from conversation: the fixed posture, the bending of the head, and the attentive look at the book, which are requisite, are all destructive of that ease, freedom, and variety of both expression and action, accessary to a just elecution.

It would superfede the necessity of most of the foregoing rules, if public speakers would deliver their discourses from immediate conception, or from memory. But if this be too-much to be expected, especially from preachers of divinity, who have so much to compose, and are so frequently called upon to speak in public; it is, however, very necessary, that they should make themselves so well acquainted with their discourse, that they may be able to take in a considerable portion with a single glance of the eye.

After the student has acquired a just and statural elecution, it is, perhaps, not the least difficult part of this art to apply this accomplishment to the purposes of real life. Many can deliver their discourses in a graceful manner in private, of before a few select friends, who, when required to speak in a public capacity, at the bar, from the pulpit, or in the senate, generally betray either a timid bashfulness, or an impertment assurance. The former is apt to lead the speaker into an awkward uniformity, the latter into a disgusting assectations

the former arises from an humble dissidence of the speaker's own abilities, and respect for the understandings of his hearers; the latter is the effect of couceit, and a contempt for the opinions of his auditors; the former may soon be overcome by a successful attention to the soregoing rules; the latter can feldom be subdued, till, by repeated disappointments, the rash adventurer is convinced, that he made a false estimate of his own value.

We shall close this section with Hamlet's instructions to the players, taken from Shakespear; which has always been considered as containing an important lesson on elecution, and may exemplify most of the foregoing rules.

trippingly on the tongue. But if you mouth it, as many of our players do, I had as lieve the town crier had spoke my lines. And do not saw the air too much with your hand, thus; but use all gently; for in the very tornent, tampess, and, as I may say, whirlwind of your passion, you must acquire and beget a temperance that may give it smoothness. O! it offends me to the soul, to hear a robustious periwig-pated sellow tear a passion to tarters, to very rags, to split the ears of the groundlings, who (for the most part) are capable of nothing but inexplicable dumb shows, and noise: I could have such a fellow whipp'd for o'erdoing termagant; it out-herods Herod. Pray you, avoid it.

"Be not too tame neither; but let your own discretion be your tutor. Suit the action to the word, the word to the action, with this special observance, that you o'erstep not the modesty of nature; for any thing so overdone is from the purpose of playing; whose end, both at the sirst and now, was, and is, to hold, as 't were, the mirror up to nature; to shew virtue her own seature, scorn her own image, and the very age and body of the time, his form and preffure. Now, this overdone, or come tardy off, though it make the un-skiiful laugh, cannot but make the judicious grieve: the censure of one of which must, in your allowance, o'erweigh



ROUND TEXT.

#### CHAP. II.

# OF PENMANSHIP.

SECT. I.

RULES FOR THE ATTAINMENT OF THE ART OF WRITING.

THERE is no part of literature acquired with less difficulty than the art of writing. Few people, be their capacities ever so mean, are incapable of learning this. Hence we see so many, who, though ignorant of the more early parts of science, such as English grammar, and even spelling good English, yet can write a tolerably good hand. This is a glaring fault; for the more correct the penmanship, the more does it display the orthographical and grammatical errors. I therefore advise all those who may have occasion to write much, to make themselves perfectly acquainted with what has been delivered in the former chapter concerning English grammar. I trust it need not be mentioned, that they should render themselves perfect in spelling: every one knows the necessary of this, and the ridicule and contempt which only one or two words wrongly spelled bring upon the writer.

I shall proceed to give a few directions, by the help of which an inexperienced person may qualify himself in this

art; and without which, though perhaps deemed fuperfluous by fome, a work of this kind might possibly appear deficient.

It is necessary that the learner be provided with the implements requifite for writing a good pen, and good free ink; without which it is impossible to write a fair copy: a round or flat ruler (the round one is used for dispatch, and the flat one for fureness), a leaden plummet, or black lead pencil, to rule the lines, without which the learner will never write Araight; and fome pounce, or gum-fandrack powder, to rub the paper with, if it be too thin to bear the ink, and when hold hands are to be written, as large text, German text, or the like; also when a word or fentence is feratched out with the penknife, in which eafe, the place must first be rubbed smooth with the haft of the knife, or a piece of clean paper, and then rubbed with the pounce, to enable it to bear the ink, A quarto fized copy-book is the most proper, at each page will contain a copy of ten or a dozen lines, which will be fufficient to write at one time.

Bolog provided with these implements, the learner may proceed to practice. The lines should be ruled straight and even, and at the same distance from each other, at the dotted lines, marked No. 1, in the plate. The distance between every two lines of writing should be about twice or three times the distance which there is between the two pencil lines that belong to the same line of writing; though this is often note or less, according to the caprice of the writer.

The pen must be held in the right hand, between the thumb and the fore and middle singers. The middle singer must be placed on the back of the pen, opposite to the upper part of the cut or cradle of the pen, and the fore-singer close to it, and both held straight. The thumb must be placed against the opposite side of the pen, called the belly of the quill, and must be hent a little in the joint. The top of the pen should point towards the right shoulder. The elbow should be drawn in towards the body, but not too close. The

arm may rest lightly on the edge of the desk, or table, between the eibow and the wrist; but the stomach should not press against the desk. The pen must be held very lightly; for if it be griped hard, the learner will never acquire an ease and expedition in writing.

The learner, having acquired a just habit of holding the pen, may copy the small letters i, e, o; having his lines ruled according to the dotted lines in the plate. He may next copy the other small letters; taking care to be perfect in each, before he proceeds to the next. Then the capital letters; ruling his copy in squares, according to the pattern in the plate: and also join-hand copies, as soon as he can make the capitals. When the learner can write an indifferent good round-hand text, he may proceed to the small round hand, and running hand; in writing which last, the pen should never be taken off the paper till the word is sinished.

The learner flould imitate the best copies. Copper-plate copies are to be preferred to those written by the men, as being more correct. Those small letters which have tops or flems, as b, d, f, b, k, l, f, must all be of the same beight. And those with tails, as f, g, j, p, q, f, y, must be all of the fame length. A due distance must be observed between the words, and between the letters of the fame word. The eapitals must be all of the fame fize. The upright firokes, or those that are formed by the upright fireke of the pen, must be fine or hair Brokes; and the downight Brokes must be fuller and blacker; but a confiant attention to the copy would in a great measure superiede the necessity of most of tie foregoing rules. The learner should not fit long at ece time, left he grow tired of learning, in which case he will not improve; nor be ambitious of writing Ch., for five or fix lines, well written, will improve the learner more than fifty lines, written in the family time, without attention to their correline's.

When the learner has arrived to fonce proficiency writing, it is requisite that he know how to make and mention

This is former to be acquired by an attentive observance of those who can make a pen well than by any verbal directions; the following rules, however, may be of fervice. Being provided with a good gools quill (thois called feconds are the belty, for aporthe fourf from it, with the back of the penknife, foraping the back of the quill mod, that the flat may be clear, their our the quilt half through, near the end, on the back part; and cut the other fide of the quill quite through, near half an inch from the sad. The quill will now appear forked; next cut away a very fhort fit in the back north, where the flit of the pen is to be ; and putting the peg of the penkife halt, or the end of another quill, under this flir, and holding the natl of the left thumb pretty hard on the back of the quall, so high as it is intended the fin field go, with a quick fudden force rend up the fit ! at mult be very fudden and quick, that the flat may be clear and close; for if the flit be clear and close, that it cannot be feen through, it is done well. Then, by feveral necestary cuts, the qual is to be brought into the form of a pen; and having brought it to a fine point on each fide of the flir, it is to be inblied in this mainter: place the infide of the infiliant the left thumb and, holding the pen between the fore and middle lingers of the left head, and enter the knife at the extremity of the rab, and out it through a little floping a then, with an almost downleight out of the kinde, out off the will, laftly, by other proper cuts, the pen is to be brought into an handlone form. How the cate is not afterwards to be mended by any cutting or fersping, for that causes a roughnets, and additively fportain. If the rate, therefore, he alreads, or mended, with the leads after it is rabbed, it mid be uitsted again, as before directed. And coderer, that the breadth of the rab mult be equal to the condition the downinght fit olds 41 11 - 1- 1-10.

#### Copies for Round Hand Text.

Avoid bad company.
Care destroys the body.
Expect to receive as you give.
God is perfect in his works.
Innocency need not fear.
Keep faith with all men.
Money corrupts many.
Opportunities are slighted.
Quiet men have quiet minds.
Sin produces shame.
Value a good conscience.
Wisdom is valuable.
Yield patiently to fate.

Be wife betimes.
Do the things that are just.
Frequent good company.
Hours fly fwift away.
Join experience to theory.
Learn in the time of youth.
No task is too hard to learn.
Provide against poverty.
Remember your duty.
Time and tide stay for none.
Understand your trade.
Xerxes wept at mortality.
Zeal is sometimes proper.

# Copies for Round Hand.

All letters even at head and tail must stand : Bear light your pen, and keep a fleady hand. Carefully strive in each line to excel; Do every thing, that is to be done, well. Excel in each new line, in every part: Faults for the future shun, by rules of art. Gripe not your pen, but hold it very flight, Hold in your elbow, have a left hand light. In all your writing at the copy look; Join all your letters by a fine hair-stroke: Keep free from faults, and blots, your copy-book. Learn the command of hand by frequent use, Much practice will good penmanship produce. Never thrive to write too taft at first; Of all a learner's faults, this is the worft. Practice alone can produce expedition; Quick writing is most learners' vain ambition. Vol. I. ĸ

Rule

Rule your lines thraight, and make them very fine;
Set thems of letters fair above the line,
The tops above the flems, the tails below.
Use pounce to paper, if the ink go through.
View well your copy, see how much you mend;
Wipe clean your pen, your task being at an end.
Your spelling mind, write each word true and well;
Zealously strive good writers to excel.

#### A Receipt for making black Ink.

To one quart of fait water, put four ounces of fresh blue galls of Aleppo, bruiled pretty small; two ounces of copperas; and two ounces of gum-Arabic. Bottle it up, and shake it once a day, and in three or four weeks it will be fit for use.

The green peelings of walnuts, foaked in the water before the link is made (if they be in featon), will render it the ftronger, and more beautiful.

# A Receipt for real Ink.

Simmer three pints of stale beer, or vinegar, with four ounsess of ground Brazil wood, for an hour; then strain it through a stannel, and bottle it up for use.

Or a little gum-water and vermilion will make a curious red ink for prefent purpose.

#### SECT. II.

#### OF SECRET WRITING.

SECRET writing may be performed feveral ways. Former ages were very fertile in inventions of this kind; and, by these means, intelligence has been obtained by countries, from others.

others, with whom they were in a flate of hostility; and that not unfrequently in modern times. It may also serve individual purposes, where secrecy is required.

There are principally three ways of writing, so as not to be read by any, but those who can discover the manner in which it is written. First, writing in cipher, which requires great ingenuity, and of which, my limits will not permit me to speak. Secondly, substituting other arbitrary marks or characters, for words or letters, than the words or letters themselves. And, thirdly, writing with some ink or liquid which will not appear legible, till rendered so by some mechanical operation.

The second method, of substituting one character for another, is easily performed; as any person might make an alphabet of his own, consisting of twenty-six characters, each of which might stand for some one letter of the English alphabet; and thus the writing would be unintelligible to any but those who have the key or index. Or, the numerical sigures may be used to the same purpose: as for example, a may be represented by 1; b, by 2; c, by 3; &c. as follows:

1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 10 20 21 22 23 74 25 26 a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, v, u, w, x, y, z.

According to this index, the following fentence, riches gain friend; will be written thus: 18, 9, 3, 8, 5, 19, 7, 1, 9, 14, 6, 18, 9, 5, 14, 4, 19. Or the figures, to correspond to the letters, may be placed in any other order. Or the letters in the alphabet may be transposed. Certain confonants may be substituted instead of the vowels, and the vowels instead of the confonants: as, instead of the vowels, \(\sigma\_i, \cdot i\_i\), \(\sigma\_i, \cdot v\_i\), \(\sigma\_i, \

fecond place, in one part, with those in the first or second place, in the other part; or, dividing it into three columns, and applying this rule alternately; first, to the first column, and then to the second: and a number of other ways there are, too numerous to mention.

The third way of writing fecretly, is, First, by writing with the juice of a lemon, the juice of an onion, urine, or the spirits of vitriol, which will not appear legible till it be holden to the fire.

secondly, by tracing the letters on the back of the paper, after it is written, with a pen dipped in milk; these letters, so traced, will not appear legible, till the paper be holden to the fire; then they will appear of a bluish colour. But, in this manner of writing, the paper should be very thin.

The last method I shall mention, is, by using sympathetic inks, as they are generally called: there are various preparations under this name. I shall mention only two, and which may fafely be depended upon.

r. If a little green vitriol be dissolved in water, with a little nitrous acid, the characters written with it will be myrable, till they are wetted with the following mixture:—

Put two ounces of finall Aleppo galls in half a pint of water; when it has flood three or four days, pour it off. A peneil, dipped in this mixture, and drawn over the letters, written with the former ink, will render them of a beautiful black.

Or, letters written with the latter ink, will be invitible, till they are wetted with a folution of Pruffian blue in water; and letters written with this folution, will also be invisible, till watted with the above ink of galls, and water.

a. Incorporate one ounce of litharge of lead with two ounces of distilled vinegar; let it stand twenty-four hours, then strain it off, and let it fettle.

I'ut one ounce of orpiment, in powder, and two ounces of quick lime, in a quart bottle, with water fufficient to :

LOVE

cover them about an inch above the ingredients. Place the bottle in a moderate heat, for twenty-four hours; then pour it off, and cork it close.

The letters written with the former of these inks, will not appear till they be exposed to the vapours of this latter inks when they will appear perfectly plain.

#### SECT. III.

# OF EPISTOLARY WRITING, AND SUPERSCRIPTION OF LETTERS.

Or every species of composition, there is none that, in its nature, approaches nearer to familiar convertation (except plain dialogue) than epistolary writing. is a direct address from one person to another, and should, therefore, contain all the cafe, elegance, and familiarity of convertation; paying the fame regard to the nature of the tubject, and the person addressed, as in a personal application. The principal characteristics of a letter are, nature, fimplicity, fprightlinefs, and wit. The flyle of a letter should be natural; and appear to express the genuine feelings of the mind. It thould not indicate the leaft mark of fludy. There should be no formal divition of the parts, no laboured introduction, nor pathetic conclusion; but all should appear the fpontaneous product of the writer's own emotions. It should likewife be wholly devoid of any complexity or ambiguity of expression a for this purpose, the fentences should be thort, and the flyle perspicuous. It should contain all the vivacity of convertation. And, if the writer be mafter of any wit, a letter (if the tubject permit) affords as proper a place for the dilplay display of it, as any composition whatever. A gentle satire, a repartee, or a burlesque, may sometimes be introduced with success: nay, it is often expected, in letters on domestic subjects, between familiar friends.

It is needless to give copies of letters on different occasions, in such a number as is usually done; the subjects of letters being as various as those of conversation: any attempt, therefore, to give specimens of letters, to serve for every purpose for which the writer may have occasion, must be absurd. A learner who copies his letter from any precedent, will not be able to express his own thoughts with ease and freedom. By being confined to a copy, from which he will find it difficult to depart, his letters will carry an awkward stiffness and formality; and he will be a long time before he acquires that freedom, and unadorned elegance, always expected in extemporary writing.

To form an epiftolary writer no more is requifite than an intimate acquaintance with English grammar; whereby he will be able to deliver his fentiments with propriety in conversation. If he possess this qualification, it will supersede the necessity of any artificial helps; but if this be wanting, other assistances will be of little use, except to serve to publish his desiciency to his correspondents.

Nevertheles, in conformity to general custom, I have added a few examples. It need hardly be mentioned, that the name, by which the person is addressed, be placed on the left hand side of the page, at the top of the letter; and the letter begun just under it: the name of the writer at the bottom of the letter, on the right hand; the date of the letter, either on the right hand, at the top of the letter, or on the left, and at the bottom: and the letter should conclude with the name by which the receiver of it is addressed at the beginning.

# From a Mafter to his Scholar, during the Holidays.

#### Dear George,

I take the first opportunity that has offered, to inquire after your health, and that of your friends. And I expect, that you will regularly answer each of my letters, that, during this time of leiture, I may have an opportunity of observing, whether you remember, or have forgotten, the rules I formerly gave you, concerning writing letters. I now, therefore, call upon you to put those rules into practice. But, willing to grant you every includence at this time of festivity, and lest your recollection should not be so clear, as when in constant exercise, I shall briefly repeat those rules, to which, I hope, you will pay a strict attention.

You remember, no doubt, my first direction was, to be very correct and circumspect in your spelling: this is the first, and most effential requisite in all kinds of writing; and make use of no word, of which you do not perfectly understand the The vulgar part of the world, in general, are very much addicted to this abfurdity. You will, now, often hear people condemn a work, as ungrammatical, and deficient in the ornaments of flyle, though themselves be unacquainted with the first form of grammar, and know not the meaning of a flower in rhetoric .-- Avoid repetitions: they always offend the judicious car, and are feldom proper, except when they enforce any particular meaning, or explain it more fully. Parenthefes are always inclegant, and thould never be uted (but suben absolutely needfury), as they render the fentence too complex. Never use the long / in a word, except when two meet, in which case it is necessary for diffinction. A letter interlined has a very ungraceful appearance; it is also an affront: for it indicates either laziness or indisference, or both. Use no capital letters, but at the beginning of a sentence, to proper names, and to the first word of every line in poetry. When you wish to lay a strong emphasis on any word, or in-

tend that it should be particularly noticed, it is common to draw a stroke under it with the pen, thus; such words, when printed, are put into Italics: but, when these emphatical words are employed too frequently, they lose their effect, and when used improperly, they puzzle the reader. Beware of using many monosyllables, they are infignificant words: nor use many too long words, left you exceed comprehension. Shun particles, as much as possible: be very sparing of your audia fors, and buts. Be not fond of inventing new words; there are enough, already, to express all our ideas: and more, I fear, than you will ever fully comprehend. Be attentive to the rules of grammar, and do not jumble the prefent, past, and future times of the verb together; as many incorrect writers do: neither confound the genders of the pronoun: nor use the singular, for the plural verb; which is frequently done: as, you was, for you were. If the sentence be conditional, use the conditional mode. Let your Ryle be simple and perspicuous, and your sentences short: let it be as concise as possible; for a prolix writer tires the patience of his reader. Observe that your points be all placed justly, which will add grace and perspicuity to your writing. These hints I hope will be attended to: let me see the effects of them in your next letter; while I remain, with compliments to your father and mother.

#### Dear George,

Berksbire, Your sincere friend, &c. &c. Jan. 2, 1803,

The Scholar's Answer.

Honoured Sir,

I return you my fincere thanks for the kind attention you shew me. It shall always be my study and ambition to follow your instructions. I never write a letter to

any of my friends, but I pay a particular regard to all the directions you have given me, on the subject of letter-writing. I exercise myself daily, in grammar, arithmetic, or some other part of literature; my sather inside upon my setting apart two hours every morning for that purpose. My fat, or and mother desire their best respects to you, and return you their kind thanks for the trouble you have taken in your late letter. I remain, with the greatest respect,

Honoured Sir,

Your very much obliged
And humble Servapt,
Guorge \*\*\*.

Louden, Jan. 10, 1803.

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# A Letter from a Pather to his Son, of School. :

My dear Boy,

I am exceedingly happy to hear of the great progress you have made in your learning. I hope you will continue to pay the same attention to all your matter's instructions as you have done hitherto. I have herewith feets you a present of a gold watch; which I defign, in the first place, as an encouragement for you to proceed; and, in the fecond place, as a monitor, to remind you of the swiftness and importance of time. This little machine travels with the hours, yet keeps pace with months; it keeps time with minutes, yet does not outrun years. Whenever you look upon this little prompter, let it remind you of your time. Every complete revolution of the minute hand filently informs you, that there has elapfed, what a whole world cannot redeem-an hour of your precious time. And, though you may perform in the following hour, or half hour, the butiness that should have been done in the foregoing hour, yet you must remember, that one hour is for ever irre overably lost. The whole life of man, at the longest, is but short; there is no time to lofe. Though you make the best use of your Vol. I. time L

time possible, while young, you will hereafter (if you have any ferious reflection) chide yourself, that you improved your time no better. Suffer no portion of your time, though ever so small, to pass unemployed; but let me give you the advice which Lord Chestersteld gives his son, on this subject: "Take care of the minutes, for the hours will take care of themselves." I have read of an Augustine monk, who kept a daily diary of his time, for upwards of thirty years, that he might know how many hours, out of each twenty-sour, he had employed in literary and religious exercises, how many in sleep, how many in the necessary avocations of the day, and how many he had shamefully loss in sloth, or unpredicable conversation. And Cato, having spent a day in which he had done nothing, thought it a matter of such consequence, as to be lamented during the rest of his life.

I do not mean by what I have faid, that I would have you always at your book, and allow you no time for recreation. In the hours appointed for play, if you find yourfelf so disposed, join in the diversions of your companions; but if, at any of these times, you prefer your book, either to anticipate through, it will better answer the purpose of your residence at school, which is to improve your mind in useful knowledge, and not in childish sports; it will redound more to your present credit, and contribute infinitely more to your future advantage.

All that I mean by what I have advanced, is, that I would never have you perfectly idle. When you are not at your play, be at your work; and when you are not engaged at your work, you may join in play at the appointed times, but no others. Heware of an inanimate indolence; fome boys are too great cowards to play, and too great dunces to learn. Hence they fland idle spectators of all that pass, and generally, in the islue, prove idle men, who are the most unprostable animals in the creation. The Arabians have a proverb, that "an kile person is a playfellow for the devil." And it

is a maxim of the Chinefe law, that, "for one idle person, the whole state suffers." Which is as true as it may appear novel to us; for he eats the produce of others' labour, without making an adequate return.

In order to guard against idleness, never give way to proerastination, or defer that till to-morrow which may be as well done to-day. Many people postpone their business till a future day, merely because it is future; but you must remember, that two days ago, yesterday was a to-morrow; and two days hence, to-morrow will be yesterday. Never, therefore, defer that to a future time which may be done at the present, without a very substantial reason.

Lastly, attend to the manner in which every thing is performed, even the most trivial matters. It is not sufficient that a chapter be read, or a copy written, without a fault, but they should be done well, with all the skill you are master of, if you mean to excel. Whenever you speak, though it be to your own companions, be fure to express yourself in the most proper and expressive words, paying a strict attention to their grammatical construction. Whenever you read. though it be but a fign-post in the street, read it with propriety and emphasis. And, whenever you have occasion to write, though it be only your name, let it be done as correct as possible. These directions, constantly observed, will render you an accomplished character, in whatever department of life you may be engaged. I hope the foregoing hints will be fufficient. Let them be well attended to, and I shall, no doubt, see the effect of them in your future acquisitions. Your mother and fifter join with me in their love to you.

I am.

Dear Boy,

London, March 20, 1803. Your loving Father, THOMAS \*\*\*.

# The Son's Answer.

C-d-n School, March \$5, 1803.

Honoured Father,

I received your letter, with your kind prefent of the watch; for which I return you many thanks. I hope it will always have the effect you defire, of reminding me of the shortness and importance of time. I never look at it, but I recollect your alarming letter. I shall always set a just value on time—it is impossible to over-value it. I shall be particularly attentive to all the commands in your letter. I often decline the diversions of my schoolfellows, and apply to my book, conformably to your defire. Yesterday I entered into Decimal Fractions; which having gone through, my master informs me, I shall begin Algebra. When I have the pleasure of coming home, next Christmas holidays, I have no doubt, but you will be well satisfied that I have made a good use of my time. Pray give my duty to my mother, and my kind love to my sister. I am,

Honoured Father,

Your most obedient and dutiful Son, Grongs \*\*\*.

From a young Shopkeeper to a 11 holefale Dealer.

· Sir.

By the recommendation of Mr. Chapman, who is my neighbour, I think proper to apply to you for the following articles:—Two dozen pieces of yard-wide calico, ten pieces of the best Jaconet muslin, thirty pieces of ell-wide town printed cottons, &c. &c. I hope you will let them be of the best quality of their fort, and at a reasonable price; as I intend all our dealings shall be for ready money.

Hull,

I am, Sir,

March 20, 1803.

Yours, &c.

#### The Anfarer.

P.

Sir.

London, Marci 24, 1803.

I have, in answer to your favour of the auth flant, sent you the articles you ordered. Should you think oper to favour me with your orders, I have no doubt but shall give you ample satisfaction. I am,

Sır,

Your obliged Servant, &c.

#### From Wholefale Dealers to a Retail one.

Sir.

As you have lately been very backward in your militances, we are under the necessity of informing you, eat, unless you send us an immediate draft, or order, for CL which has so long been due, we must use such means will prove very disagreeable both to you and ourselves.

We remain,

Liverpool,

Sir,

Yours, &c.

# The Answer.

Gentlenien.

Several severe and unexpected toffes have been be sole cause of my late remissions. I am very sensible of he lenity you have always shewn me. I only request your coeptance of my bill, payable in two months; money being a this time very karce, and my debtors very backward in heir payments.—Should this be agreeable to you, I shall mays be very punctual for the future. I am,

Berifore,

Gentlemen.

Larab 30, 180;

Your much obliged Servant, &c.

#### The Reply.

Sir.

Liverpool, April 3, 1803.

As we should be forry to diffres you, we are willing to accede to your proposal; and hope, that, by the time you mention, you will be able to make good your promise. We remain,

Sir,

Your humble Servants, &c.

#### From a Tradefman to his Friend.

Sir.

Relying upon the fincerity of your friendship, I have taken the liberty to solicit your affistance at this critical juncture. My affairs are greatly embarrassed; and, unless I can procure the sum of sool. I shall inevitably be ruined. If, therefore, you can oblige me with the above sum, to be paid by instalments, at three, six, nine, and twelve months, at 50l. each payment, you will save me from impending bankruptcy, and infinitely oblige,

Sir,

Merch 27, 1803.

Your distressed Friend, &c.

P. S. You know the value of my flock, and also my expectations.

#### The Answer.

My dear Friend,

I am very forry to hear of your present dissiculties. I desire you will call upon me to-morrow, when I hope I shall be able to accommodate you with the sum you want; or, if I cannot furnish you with the whole, I can let you have the greater part, and the remainder in a few days.

I am,

Westminster, March 30, 1803. My dear Friend,

Yours fincerely, &c.

It is as necessary to know how to direct, or subscribe, as to write a letter. Persons in high rank, and peculiar stations in life, are to be addressed in a peculiar manner.

For the Directions or Superscriptions of Letters.

To the King-To the King's Most Excellent Majesty.

To the Queen-To the Queen's Most Excellent Majesty.

To the Prince of Wales—To His Royal Highness, George Prince of Wales.

To the Princes-To Her Royal Highness, &c.

#### To the Nobility.

To a Dake-To [His.Grace] the Duke of, &c. \*

To a Marquis-To [the Most Noble] the Marquis of, &c.

To an Earl-To [the Right Honourable] the Earl of, &c.

To a Viscount-To [the Right Hon.] Lord Viscount, &c.

To a Lord-To [the Right Honourable] Lord, &c.

The fons of dukes, marquisses, and the eldest sons of earls, have the title of Lord, and Right Honourable; and the title of Lady belongs to their daughters, with the addition of their Christian and surnames: as, Lady Caroline Russel, &c.

The eldest sons of dukes, marquisses, and earls, enjoy the second title of their father, by the courtesy of England.

The children of viscounts and barons are also styled.

To a Baronet-To [the Honourable] Sir J. H. Bart. &c.

To a Knight-To [the Right Worshipful] Sir J. H. Knt.

To a Privy Counfellor—To [the Right Honourable] J. H. one of His Majesty's Most Honourable Privy Council.

To an Ambassador-To His Excellency, &c.

Also plenipotentiaries, foreign governors, the lord lieutenant of Ireland, and lords justices of Ireland, and the captain general of His Majesty's forces, have all the title of Excellency added to their other titles.

<sup>\*</sup> The words included in crotchets are forestimes omitted.

The title of Right Honourable is given to no commoner, except members of the Privy Council, the three lord-mayors of London, York, and Dublin, and the lord-provett of Edinburgh, during their office only.

# To the Clergy.

- To an Arabbifop-To the Most Reverand Vether in God, See, 1 or, To His Grass the Lord Archbishop of York, or Canterbury.
- To a Rightp-To the Right Reverend Father in Grad, been or, To the Lard Bilhop of, &c.
- To Deans, Archdencous, Wo.-To the Rev. A. B. Dean of, . Rec. ; or, To the Rev. A. B. Archdencon of, Re.,
- To the inferior Clergy-To the Rey. Mr. A. &c. ; or, To the Rey. Dr. &c.

#### To the Military and Navy.

All colonels are flyled Honourable; and all inferior officers thould have the name of their rank fet first; as, To Majer G. C.; To Captain I. H. &c.,

All admirals in the navy are flyled Honourable; the inferior officers are flyled by their rank, as in the army.

# To the Judges and Lawyers.

- To the Lord High Chanceller of Great Retrain.—To the Right Honourable J. Lord E. Lord High Chancellor of Great Britain.—Lord Pretident of the Council.—Lord Privy Seal .—One of Hie Majefty's Principal Secretaries of State, &c.
- To the Mafter of the Rolls-To the Right Honourable bir W. G. Kut. Matter of the Rolls.
- To a Judge-To the Right Honourable E. Lord E. Lord Chief Justice of the King's Bench, or of the Common Pleas.
- To the other Judget-To the Right Honomable A. B. Efq. one of the Juffices of, &c. ; or, To Judge A.

To the Chief Baran.—To the Hon. Sir A. M. Lord Chief Baran.

To His Majeffy's Attorney, Solicitor, or Advocate General.—

To Sir A. B. His Majeffy's Attorney, Solicitor, or Advocate General.

Every judge has the title of Right Honourable, if a Privy Counsellor 4 otherwise only Honourable. All others in the law are flyled according to the office they bear 3 and all barristers have the title of Esquire.

To the Lieutenancy and Magistrucy.

- To a Sherif-To A. B. Efq. High Sheriff of the County (of York.)
- To a Recorder—To the Right Worshipful A. B. Recorder of the City of, &c.
- To an Alderman—To the Right Worshipful A. B. Esq. Alderman of Tower Ward.

The aldermen and recorder of London are flyled Right Worthipful, and Efquire; as are also all fheriffs, and mayors of corporations, during their office.

Every gentleman in the commission of the peace has the title of Esquire, and Worshipful.

To the Governors of the Crown.

- To the Lord Lieutenant of Ireland-To his Excellency A. Lord B. Lord Lieutenant of Ireland.
- To the Governor of Dover Caftle—To the Right Honourable

  A. Earl of D. Governor of Dover Caftle, &c.

The fecond governors of foreign fettlements, appointed by the King, are called Lieutenant Governors. Those appointed by the proprietors of the fettlement, as the East India Company, &c. are called Deputy Governors.

To either House of Parliament, to Commissioners, Bodies Corporate, &c.

- To the House of Lords—To the Right Honourable the Lords Spiritual and Temporal, in Parliament affembled.
- To the House of Commons—To the Honourable the Knights, Citizens, and Burgesses, in Parliament assembled.

- To the Trenfury or Admirally To the Right Honesistantha that Lords Committeeness of the Treasury; or Admirally.
- To the Commissioners of the Customs, or Receiver To the Honour this the Commissioners of the Majetty's Cottoms, or Resease of the Preise, & .
- To ring of the Companies of the City of London -- To the Matter, Wardens, and Central Affillance of the Wor-flapful Company of, & .
- To the Contenues of Cheeff's Hoppine To the Right West-High Atta Converse, and Cheeff's Holpital.
- To the Lieft India Compan, "Vo the Homenrable Court of Emeritary of the United Conspiny of Merchants teading to the East India:
- To the Inne of Court. To the Honomable Society of the Inner, or Modelle Temple, or Gray's Inn, 20.

The governors, truffees, &c. of holpitals, colleges, &c. are flyled Worfingful or P ghi Worfingful, or Honourable or Pight Honourable, if my of them pull france of these titles.

It is also necessary to know move to be given letter to any of the foreign age, and to

### For the Reprinting of Letters

To the King or May or please your May By.

In the Sension of May at the May at the deep your May By.

To a Principal South to, as May at the deep your Bright of the New Principal Statistic, or May at preade your Bright of the Two Principal Styles of States, or May at please your Grace.

To a Date of the May at the May at the your Grace.

In a Date of the May at the May at the your Grace.

In a Margine, Earl, Principal Burens My Land, or May a position of the office.

To describe the Marin, or May a perfect year Ladylingo To a Borrows and a May at piecte your Houseur.

To a Ku for more as May a piecte your World p.

To their Conjust. Madam, or May at piecte your Ladylin p.

To an Archieftop May a please your Course.

To a Riftop My Lord, or May at please your Lordling.

7.

	•		
•			

Married wanter and widows are conflict to the fame mask among each other as their butbands would have been emirical to among themselves a except facility rank be marriy professional or official :—and unmarried women to the fame rank as their eiden brothers would bear during the lives of their famers.

#### SECT. IV.

### THE 137 OF STENOGRAPHT, OR SHORT HAND.

Syzalo value value of Short Hand, is the set of writing to a more expectations manner than by the common mode, for the purpose of taking commit speech, or clicourfe, as decvered by the Speeker.

For the purpose, the writer of these bead is permitted to ing for half of deveral revenues which as other where a Lipinet. He ma me liberry of invention an alphanet of his tives, to effect of common arbitrary marks, or characters, which is the face of emediment are of a left complex form that their of the other altimaters. He may refer our of the ettere in the common libration, where we not evil serie nenellem for the writer to near edit the ferfer or labelishing res une que fume champiten qui feme fon troi e il più pentera : an le conse corre le tile fineri-hand albaraber, where if and et are crise chie diminante in que que fon que orden, en à repreferres ne tre fin e that fiere de ere alle me E des nard 4, the e det the fifth. He sub omets the nowell except where they are enchibes il um deutiliem au disconem the femile . Confesioene vi But a bot to its form the ordinatery mease of localities, such is to talen ba mere lener. A & word iber die preulet tentelling na expendit the factor.

The fliort-hand writer, besides these advantages, sometimes makes use of single characters to express whole words, and even whole sentences: but of this hereaster.

The first and principal rule in short hand, is, to make afor of no more letters than are needlary to give the reader an idea of the found of the word. For if the writer use all the letters that are necessary to express the found itself; he will gain but little advantage by it; as he will be obliged to use too many letters to be very expeditious.

But it must be here observed, that this rule must not be followed too strictly at first, and during the learner's exercises; less it render his writing too imperfect, and unintelligible to himself. He should, therefore, at first, content himself with using every character for every consonant, till he be perfectly acquainted with them all, and can very readily form them; marking the points for the vowels, as is hereaster directed.

### Of the Short-hand Alphabet.

The fliort-hand alphabet confifts of the following conionants: b, d, f or v, g or j, k or hard c, l, m, n, p, q, r, s ov foft c, and z, t, v, x: each of which has its proper character, as seen in the plate. The characters it inding for these letters are to be neatly joined together, to form words; and written in the most expeditious manner possible, without taking the pen off the paper till the word be finished; and the vowels are to be noted afterwards (if necessary) by points.

Though the omission of the vowels may at first somewhat puzzle the reader, to read even his own writing; yet a little practice will render it perfectly familiar to him; as the chief dissiculty, both in writing and reading short hand, arises from the novelty of the characters, and from the want of a familiar acquaintance with them.

. In order to perfect the learner in the construction of all the characters in the short-hand alphabet, it is absolutely necessary that he frequently copy them. He should, daily,

write

write a copy of the short-hand alphabet; ruling his lines according to the dotted lines in the first line of the first lesson in the plate; and writing the fignification of each character at the end of each line, and the letter it represents at the beginning of the line; using three or four lines of a quarto copy for each letter.

In the aphabet given, I doubt not but the characters will be fived as convenient for prairies as any entant. I have endeavoured to make it could of the moft fample, and, at the fame time, the most diffinit characters. I final only coderve, that by the help of this alphabet, and the aburevanious that follow, I have been able to follow the most rapid speakers.

This alphabet, though confifting of the characters for fifteen conformate only, will be found quite inflicient. The sbeing fupplied by either i or a according as n is pronounced hard or foil. The é-may very well be omitted in fluori hand, as it is only an alphabet of the breath and the found of the cord (which is all that is minded in this freeze of writing may be only a shall that is minded in this freeze of writing foil, which has the fame found. It is also supplied by fibeing only a market found must that error. It is represented, if necessary, by the vower is never generally the latter found of and a by a from value is differed in found out a linear being of a counter nature.

The vivel are lexion info a from tank; on when it a meeting to a few any of them, they are represented by points; as will be feen hereafter.

Three of the characters in this a parameters horizontal figures. Figure 2014, and we are the time the increasing anti-dependent of the course dependent enters in the course of them are section of the course of the course dependent of the course of the course dependent of the course of the course

In forming the Inomenant characters Ingle, the estimating colors of the wilder to have be well as may be able to

that the horizontal characters are only half the height of the hursh, and inclined ones. For the two latter ones generally occupy the whole space between the two lines, as seen in the plate. But this direction is to be strictly adhered to only while the learner is forming the characters singly: when he comes to join the characters together, to some words, it will be often necessary to make them less or greater than their usual stage; sometimes for convenience, and at other times from necessity; as will be shown in its proper place.

#### Of the B.

This letter, in thost hand, is formed by an inclined curve line, or small segment of a circle; it should always be formed from the top, which is on the left hand; and universally I would advise, that all inclined and horizontal letters be formed from the left hand part, as it is the most natural, and will be found the most expeditions. This letter may also be used to express the words be, by, but, and black; and, with a short lateral stroke joined to the fore part, it represents the word before; and the same stroke, when placed in the hinder part, signifies the word behind \*; as shewn in the plate. This letter is also used to denote the inteparable prapositions be, ob, and ab, when helonging to a word: as, believe, sh-scure, &c. It also forms the terminations ble, or able, both singular and plural, and hy: as, remarka-ble, move-ables, and a-bly.

C.

This letter is not diffinguished by a separate character; for its sound (except before b, which is provided for) is either hard, like k; or soft, like c. It is, therefore, repreferred by the one or other of these characters, according to its sound.

When the Arche is drawn chrough the chundres, it lightles that words hefore and behind a mid when the Arche is but at the late hand groups, it mainly the west beginning.

#### D.

This letter is the fegment of a fmall circle, with its two points downwards: it is begun at the left hand point, as the last. When used alone, it represents the word and, band, and end. It also stands for the prepositions de, di, dis: 28, de-bate, di-vide, dij-pute. And is used for the termination ed: 28, turn-ed.

### F, or V.

This letter is formed by a straight, downright or upright, stroke of the pen (for it may be made either upwards or downwards, as is found most convenient to the writer). When it follows a letter that is finished at the bottom, it is formed upwards; but when it succeeds a letter that is concluded at the top, it is formed downwards, that the pen be taken off the paper as seldom as possible. It also stands for the m, which is a letter of nearly the same sound, being only a little coarser, and is, therefore, not distinguished in short hand by a separate character: but if it be necessary to distinguish it at any time from the f, it is only making the character a little blacker, or fuller. This letter also represents the words for, if, of, off, and fine; and the inseparable preposition for: as, for get. And the terminations fy, if, ful, and fulness: as, de-fi, sanct-igh, forget-fulness.

### C, or J.

This letter confifts of a fegment of a circle, the same size as the d, but formed in a different direction from that letter; this being in a vertical direction, running from the top line to the bottom one. It is also used for the j, which has partly the same found as the soft g., But, when used for the j, it should be written fainter, particularly towards the bottom. This letter may also be begun either at the top or the bottom, as is found most convenient to make it join with the foregoing letter. When it stands alone, and as a g, it represents the words again, against, great; and as a j, it signifies the words judge, just, join. Joined to other characters, it repre-

fents the word grand: as, grand-father; and the terminations gree and join: as, a-gree, con-join.

#### H.

There is no character to distinguish this letter; for, as it is only an aspiration of the breath, its insertion is not necessary to discover the sound of the word; it is, therefore, wholly omitted.

Ţ.

This is represented by I; as hath been shewn.

#### K. or C hard.

This letter is formed in the same shape and size as the d, but in the quite opposite direction; it is always begun at the lest hand. When it stands alone, it represents the words can, could; and with a short stroke drawn under the middle, it signifies cannos. Used as a preposition, it signifies com, con, and contra: as, com-pound, con-ceal, and contra-ry; as a termination, it represents acle, ical, and icle: as, spect-acle, period-ical, and art-icle.

L.

This letter is formed of a straight lineal stroke, like the f, but turned a little at the top, towards the left hand. It is mostly begun at the top; but, if found necessary, may be made from the bottom. By itself, it represents the words all, always, altogether; joined to other characters, it stands for low, latter, and late: as, low-ly, latter-ly, late-ly: and, as a termination, it signifies by: as in low-ly, latter-ly, and late-by; thus, two of those characters represent each of these words; and when thus used, should have its vowel point to the first syllable.

#### M.

This letter is represented by a straight lateral stroke; and is always begun at the left hand. Alone, it represents the words am, among st, my, mine, me, whom; also, much or many; when made larger than common, it signifies the word more: with a short stroke across the middle, it stands for the words

rvice

review as much, or twice the number, or doubt the quantity; with two such strokes, it signifies shore since as much, &c. ; and with a dot placed under the middle, it thanks for helf as much, &c.; and with two such dots placed under it, it signifies the word med. With the negative stroke under it, it signifies not me, not so much, &c. Joined with other characters, it represents the propositions magni, and mis to, magnify, missiortune; and as a termination, it shade for ment or ments: as, testa-ment.

This letter is formed of a straight lineal stroke, with the top a little turned towards the right hand. It is mostly begun at the bottom, but it may be formed from the top, if requisite. When used alone, it represents the words on, in, mader: as a preposition, it stands for one, one; in, interpoder: as, ante-codent, anti-podes, in-ter, inter-rogation, under-mino. As a termination, it stands for one and ness; as, garment, haraes.

This letter is formed of an inclined curve line, leaning towards the right hand. It is always begun at the bottom. When used alone, it stands for the words spen and poor. As a preposition, it represents per, pre, and pro: as, per-plex, pre-tage, and pro-long. As a termination, it is seldom or never used in English.

This letter is formed of a straight stroke in a lineal direction, with the top curled quite round towards the less hand. It may be begun either at the top or the bottom, as is found most convenient. When it stands alone, it signifies the words question and quantity; with a short stroke across the middle, it represents the phrase double the quantity; and with a dot placed under it, it stands for balt the quantity; with the negative mark under it, it stands for not the quantity. When joined to other characters, it represents the words a quarter, and a quarter as, a quarter of an hour, a quart of water. As a termination, it stands for quires as, re-quire.

THE WALL

R.

This letter is formed like the g, but in an opposite direction. It may be formed either upwards or downwards, as most convenient. When used alone, it stands for or and other; when joined to other characters, it represents re: as, resolve. As a termination, it stands for ary, ing, ings, and er; as, di-ary, exceed-ing, turn-er.

### S. Soft C and Z.

This character is formed of an inclined curve line, and is mostly begun at the bottom. It represents also the soft c, and the set but as the se has a coarser sound, it may be represented by a blacker and fuller character. When used alone, it signifies as, is, us, and yes, when it is joined to other characters, it stands for fasis, circum, super, and substantially, eircum-vent, super-sine, sub-tract. As a termination, it stands for tion, self, and seevers as, ora-tion, my-felf, whom-supers.

Т.

This letter is formed of an inclined but straight line, and is mostly begun at the top. Alone, it stands for the and to. As a preposition, it stands for transfe as, transfer. As a termination, it signifies ty or ties: as, beau-ty, beau-ties.

u/

This letter is formed of a flraight but inclined ftroke, like the former, but in the opposite direction. It is mostly begun at the bottom. By stielf, it stands for will, will, would, and with a fliort stroke drawn under the middle it represents will not, or would not. Joined to a following character, as a preposition, it signifies with: as, with-out. As a termination, it stands for ward and well: as, out-word, and holy-well.

X.

This letter is formed of a straight lineal stroke, a little turned at the bottom towards the right hand. It is generally formed downwards, but it may also be formed upwards, if sound more convenient. Alone, it stands for except, exercise, and exercises. Joined to other characters, it represents ex.

extra, and exceed: us, ex-pose, extra-ordinary, exceed-ingly.

As a termination, it represents lex: us, comp-lex.

#### Y.

There is no character appropriated to this letter, being represented by the vowel mark for i.

#### Z.,

This letter is represented by the character which stands in common for the fost c, and s; as hath been seen.

Befides the characters appropriated to express the confonants singly, there are three other characters for three double confonants, viz. cb, fb, tb.

#### CH.

The character used to express these two letters, is a straight lateral stroke, turned upwards a little at that end towards the left hand. It is always begun at the left hand point. When it stands alone, it signifies each, which, and finds. As a preposition, it stands for arch: as, arch-itest.

#### SH.

The character appropriated to these letters is like the foregoing; but turned downwards at the lest hand point, instead of upwards, and like that is always begun at the lest hand. When it stands alone, it represents the words shall, shall, and should; and with a short stroke under the middle, shall, should, or would not. As a termination, it stands for ship: as, ward-ship.

#### TH.

The character used to denote these two letters, is also a straight lateral stroke, with the end turned a little upwards, at the right hand point. This is also begun at the left hand. When it stands alone, it represents the words they, them, that, this, and than.

There are also other characters appropriated to express feveral treble conforants, which frequently occur in words of most common use.

CHR.

#### CHR.

The character used for these three letters, is two perpendicular lines joined at the top by a curve:—it is mostly begun at the lest hand point: and is used in the words Chrisk; and, with the vowel point for a, in the word charanter.

#### LCH.

This character is formed like the two fides of a triangle, with the point downwards; and is mostly begun at the left hand; as the foregoing.

#### LTR.

This character is formed like the two fides of a fquare, with the conjunction of the lines at the bottom, and towards the left hand. It is generally begun, like most of the others, at the left hand.

#### LTH.

This character is formed like that for kb, but with the point upwards; and is begun at the left hand point.

#### MPL.

This character is a double curve, and inclined towards the left hand, at the top; at which part it is begun.

#### NCH.

This character is just the reverse of that for . hr, and begun at the left hand.

#### RCH.

This character is composed of the two sides of a square, joined at the top, towards the right hand.

#### RTL.

This character is an inclined double curve, leaning towards the right hand, being in the opposite direction to that for mpl.

#### RTH.

This character is an inclined line, leaning towards the left hand, where it is begun, and curled quite round at the top-

#### SHR.

This character is also an inclined line, but leaning towards the right hand, and curled round at the bottom.

SKR.

#### SKR.

This character is also an inclined line, leaning towards the right hand, and curled round at the top.

#### STR.

This character is formed of two straight lateral lines, joined together at the left hand end by a curve. This letter small be begun at the top, and at the right hand.

#### SPL.

This character confilts of the two fides of a figure, joined together at the bottom of the right hand fide. It is always begun on the left hand.

#### SPR.

This character is formed of a double curve, and inclined towards the left hand, like that for mpl; but the curves are formed in an opposite direction.

#### THR.

This character is an inclined line, leaning towards the left hand, and curled round at the bottom.

Here it must be noted, that the characters for those trebie confonants are to be used, though the confonants which they represent do not follow each other immediately; as in the words alray, and arithmetic.

When the learner is perfectly acquainted with the conftruction and full fignification of each of the foregoing characters, he may then proceed to join their characters together, in order to form words; observing, that each character be neatly joined with the foregoing one; for which purpose, it is often requisite, that many of the characters be formed less than their real fize; as may be seen in the plate.

### Of the Fowels.

The vowels, in fhort hand, are represented by dots. In the perpendicular and inclined letters, a is represented by a dot, placed on the left hand side of the letter, and near the top of it: c, by a similar dot, near the bottom, on the left hand side: fide: i, by a dot placed just above the letter, like the tittle to a small i: e is represented by a dot placed near the top, but on the right hand side of the letter, just opposite the place of a: and u is represented by a dot near the bottom of the right hand side, opposite the place of e. But, in horizontal characters, the dot for a is placed under the letter, and at the left hand point; that for e, unde: the letter also, but at the right hand end; the i, over the letter, a, before; the e, over the left hand end of the letter, and opposite the place of a; the u, over the right hand point, opposite the place of e.

This order of placing the vowels about the character for any confonant, is to be observed only when the vowel immediately follows such confonant; if the vowel precede the confonant, just the reverse takes place, in placing the vowels. When this is the case, the dots for the a and e are placed on the right hand side of perpendicular and inclined letters, in the place of o, and u, respectively; and o and u are placed on the left hand, where a and e are placed in the former case; that is, when the vowel follows the consonant. And i, or y, is always noted by a dot, placed above the consonant it follows. In horizontal letters the same rule obtains, whether the vowel follows or precedes the consonant.

But the former method of marking the vowels, viz. by fetting the mark about the confonant which immediately precedes the vowel, is more natural and perfpicuous; and should always be followed, if possible.

To mark the double or treble vowels, when necessary, a dot should be set in the place of that vowel which is of the nearest sound to such double or treble vowel: as for example, to express the ea in the word great, we use the vowel point for a: as, grat; and to express the triphthong eau, in beau, we use the vowel point for o: as, bo; but for the vowels in the word beauty, we use u: as, buty.

It is necessary that the learner, in his first exercises in this art, make the character for every letter of which each word is composed, marking all the points for the vowels. This is necessary

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following one: if they be joined in any other manner, as the words by the No. 18, in the third lesson; or if they stand separately, they signify whole words, and not single letters.

#### RULE II.

There are many words which frequently occur in writing upon any subject whatever, and may easily be recollected by the writer, though expressed ever so impersectly; such words may be written by only marking the first letter of the word, if it be a consonant; or the vowel point and the first consonant, if it begin with a vowel, as is often done in the third lesson with the words modelly, affarance, bafful, and impudent, and baffulness and impudence.

#### RULE III.

When words are thus expressed by their first, or sirst and second letters, it is often necessary to distinguish them, as being either substantives, adjectives, verbs, or adverbs. If the word be a substantive, it is marked by a dot placed against the end of the character; if an adjective, by a point placed just before or above the place where the substantive point is placed; and if an adverb, by a point just behind or below the substantive mark, that is, on the opposite side to the adjective point. The places where the three points are or should be situated, must be in a straight line, which line must be at right angles to the end of the character; as seen in the plate; (see distinguishing points). When the substantive thus expressed is plural, the substantive point is to be made a little longer than usual. The verb has no point to express it.

#### RULE IV.

When the same word is required to be repeated with a preposition, whether it be a substantive, adjective, verb, or adverb, it is only placing another point after its substantive, adjective, or adverb point i as in sig. 5, time after time.

RULB

#### RULE V.

When two words are expressed by their first consonants, and a preposition should be between them, which is omitted, they are to be joined together in the common manner, and a point placed at their point of conjunction; as in fig. 7 and 8, the love of money, the thirst for gain.

#### RULE VI.

When any word begins with any of the prepolitions, it is to be begun with the mark for such prepolition; and, in general, the next consonant will be sufficient. And when they end with any of the terminations, the first, or first and second consonant of the word with such termination, will generally suffice to discover the sound. But when prepositions and terminations are used, as they are joined to the other characters like single letters, the word should always have at least one of its vowels' points to prevent consultion.

#### RULE VII.

Most of those phrases which consist of a word with a preposition, conjunction, or article, before and after it, may be written as one word.

#### RULE VIII.

When a pronoun follows a preposition, they are joined together, as the foregoing. And pronouns may always be expressed by their first, or first and second consonants, having the vowel point if requisite,

#### RULE IX.

To express the definite article *the*, the consonant mark for t is used; and to express the article a, a small point is placed at the beginning of the following consonant.

The foregoing rules are all that can be fafely given; and if strictly attended to, will answer every purpose that can be expected

expected from this art. I have avoided arbitrary characters for certain long words and phrases, as I am convinced they are not adapted to every one's memory; and from the great number of words with which our language abounds, it is impossible that a sew hundred characters to express so many peculiar words can be of much utility to the learner, and particularly as the chief use of short hand is to follow a public speaker, many of whom possess a very extensive slow of language. Besides this, the method of substituting a set of characters for many words or phrases is very burdensome to the memory, difficult to learn, and is easily and soon forgotten.

I have thought proper to mark all the vowels by points, according to many of my predecessors in this art, though I have differed from all others in the order of placing them. Dr. Mavor, Mr. Angel, Mr. Mason, and Mr. Gurney, also express the vowels by points; but the method of the three latter is to denote the vowels by points placed on the same fide of the letter: thus, a and care represented by points near the top of the character, or the beginning of it; i by a point in the middle of the character; and and a by points near the bottom or latter end of the character: whereas, in this fystem, the points for a and e are placed on one fide the character, and those for and a on the other fide of the character, and the point for i, at the top; which must give this method a great advantage over the other. By the former method the place of the a and e cannot always be distinguished from each other, nor that of the o and w: by this method, I will venture to affert, they will never be confounded.

Though fome writers on this subject have given different characters for all the vowels, I have given the preference to points; they give the writer infinitely the advantage over the other method, in point of expedition; and by an attentive perusal of his work after he has written it, and while the subject is still fresh in his memory, he may mark all the vowels; which will render it intelligible at any future time.

With regard to the characters for the confonants, I have endeavoured

andeavoured to render them as simple as possible in their con-Arnetion, yet perfectly different from each other. Moft writers on this art either make their characters too complex, or, if they make them simple, form them so much alike, that they are eafly confounded with each other. In tome modern systems, the difference between different characters confice only in one being a fine and the other a black stroke; which diffinction, writers of foort hand have foldon time to make: not to mention the other fimilarities between the characters. such as, different characters being of the same form, but of different fixes; with many other abfurdities. While, on the other hand, thate who have rendered their characters futticiently different, have formed them to complex, as to give the learner no advantage, in point of facility, above the common round hand. It must be allowed by every one, that the more simple a character is, the more easily it is formed. When a character confifts of two lines, whether arraight or curve, it requires almost twice as much time to form it as to form a character confisting of only one of such lines; and characters which confift of two lines joined together at one ond, to as to form an angle, require thill more time to form them. Willia, who published a tystem of short hand in the year 1648. has no lefs than thirtren characters in his alphabet, which are formed with angles in them, belides two which are complete ovals, or circles. And Mr. Mawd, who published another fythem in 1635, has also eleven angled characters, and those for the most part taken from Mr. Willis. Mr. Skelton, also, who improved upon the two former, has, in his alphabet, published in 1600, fourteen very complex characters, namely, ten angled ones, three curled at one end, and one complete circle. But Mr. Rich, who published his system in 1660, has only foven angled characters, three curled ones, and one entire circle. His fyftem was in great repute for many years, and Mr. Locke recommends it in his treatile on Education (becaute there was at that time none better). Yet Mr. Nicholas, who published his system thirty years after Mr. Rich, and evidently

took

teck most of the characters in his alphabet from that, has also angled characters, three curied ones, and one circular. Mr. Nicholas, also, was the first who omitted inferting regular characters for all the five vowels, though he has used one farg. For Mr. Willis has diffinct characters for every one of the vowels; Mr. Mawd has characters for all but i'and u; Mr. Skelton and Mr. Rich have characters for them all.

In the year 1715, Mr. Lane published a system of short band under his own name; but his alphabet, as well as that of Mr. Addy, published some time before, is taken literally from Mr. Rich; except that Mr. Lane has omitted the character for c, which Rich has used; and inserted a character for c, which is not in Mr. Rich's.

In 1727, Mr. Weston published his system, which was taken for the most part from Mr. Rich; but confiding of more complex characters than any of his predecessions ting thirteen angled characters, four curied ones, and a continued circular one.

In the year 1732, Aulay Macaulay, Eq. published his treatife of short hand, which though more original in the construction of the characters than any preceding one, is, nevertheless, very complex, as in forming many of the letters the pen must be taken off the paper before the letter can be finished, as is the case in the u, where the pen must be taken off to mark a point to distinguish it from the e, to which letter it otherwise would bear an exact resemblance; the same can be said of the character for the k, which must also have its point. And the vowels in his system are all expressed by characters, which must render it still more tedious to the writer.

Mr. Annett soon after published a treatise on short hand, taken from the former, but rendered a deal more simple, or rather too simple. For many of the characters in his alphabet are formed so much alike, that it is impossible for a writer in haste to mark the difference: the characters for a, e, i, and y, are all formed by a straight lateral stroke, and only distinguished from each other by their length, which must necessarily

create

create much confusion. The characters also for  $\delta$  and  $\rho$  are fimilar, differing only in length, as are also those for d and t.

In 1753, Mr. Gurney published his treatise of short hand, being an improvement on that of Mr. Mason, published near fifty years before, and who was the first who made any confiderable improvements in the construction of the characters since Mr. Rich. Mr. Gurney's alphabet, though an improvement on that of Mason, has, nevertheless, eight characters which have angles in them; besides a curled character, a common round hand r, and a circular character with a straight stroke before it, like the figure 10.

Mr. Angel, in 1758, published a system of short hand, being an improvement on that of Mr. Gurney, and in the year 1762, Messrs. Swaine and Sims published their system, which was also an improvement on the same author. Each of these phabets contain six characters with angles in them, one circular or curled letter, and one like the sigure 10.

Soon after this, Mr. Hodgson published his treatise of short hand, taken chiefly from Mr. Gurney's alphabet, but being a great improvement thereon; his characters are more simple, and, at the same time, full as different from each other as those of any alphabet that had been made before his time; he has but two characters which have an angle in them, only one curled one, and one like the figure 10; the others are simple curves, or straight lines.

The Rev. Mr. Byrom, A. M. published his universal short hand in 1771, which, though consisting of no angular nor circular characters, has no less than nine characters completely curled at one end, which must render his system very complex and sedious.

In 1774, Mr. Palmer published a treatise on short hand, in which he somewhat improved on Mr. Byrom's plan, having only seven curled characters in his alphabet.

In 1776, Mr. Williamson published his system of short hand, in which alphabet there are also eight curled characters.

Mr. Blanchard, in 1776, published a complete system of

that thand, in which the characters are all timple, firsight, or curve lines, except one curled character, one circular one, and a croisone. His alphabet is, therefore, more timple and fit for practice than that of any or me predece flors, and the letters are fulficiently different from each other to prevent mittakes.

Since Mr. Blanchard published his fystem, feveral others have appeared, which I have not room to mention; fuffice it to lay, that from that period to the prefeut, most, if not all the writers on the art have run into the opposite extreme to the writers before his time, which is, that of rendering their alphabetical characters too fimple. In many modern alphabets fon e of the characters refemble each other to nearly, that the writer, some time after he has written his piece, is often at a lots to discover the fense of the greater part of it. I have met with feveral writers who have learned from Mr. Taplin's fystem, and have experienced this difficulty. Mr. Taplia's alphabet has not one angled or compound character, and only one finall circular one for the letter it; but then he has one character for two or more letters: thus, b, f, p, and w are all reprefented by a firaight flooks in the fame polition, and diffinguished from each other only by the length or boidness of the charafter: the fone may be obtained of the charafters for p, j, k, and a, which are also thought lines in the same polition; and though the functionty between those and other characters in that alphabet may not be for apparent when viewed fingly, yet when fir his harafters come in contact with others, it foldom fails to pazzle its writer, except he be very converfant in the fyftem.

Mr. Taplin's method of marking the vowels is forectimes by dots, and for coinces by the fitting of one of the conformation

I have noticed the alphabetical characters only of the foregoing writers, without adverting to their other characters for double and treble letters, words, and phrafes, as those characters form the flund of each writer's futtern.

Concerning the alphabet I have here the honour to propose, I must just observe, that I have avoided all angular, compound,

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Letton II.—If I were put to define Modesty, I would call it, the reflection of an ingenuous mind, either when a man has committed an action, for which he censures himself, or fancies that he is exposed to the censure of others.

For this reason a man truly model is as much so when he is alone as in company, and as subject to a blush in his closet, as when the eyes of multitudes are upon him.

I do not remember to have met with any inflance of modesty with which I am so well pleased, as that celebrated one of the young prince, whose father, being a tributary king to the Romans, had several complaints laid against him before the senate, as a tyrant and oppressor of his subjects. The prince went to Rome to defend his father; but coming into the senate, and hearing a multitude of crimes proved upon him, was so oppressed when it came to his turn to speak that he was unable to utter a word. The story tells us, that the fathers were more moved at this instance of modesty and ingenuity, than they could have been by the most pathetic oration; and, in short, pardoned the guilty father for this early promise of virtue in the son.

I take affurance to be the faculty of possessing a man's felf, or of faying and doing indifferent things without any uneasines or emotion in the mind. That which generally gives a man affurance is a moderate knowledge of the world, but above all a mind fixed and determined in itself to do nothing against the rules of honour and decency. An open and direct behaviour is the natural consequence of such a resolution. A man thus armed, if his words or actions are at any time misinterpreted, retires within himself, and, from a consciousness of his own integrity, assumes force enough to despite the little censures of ignorance and malice.

Leffon III.—Every one ought to cherift and encourage in himself the modelly and affirmance I have here mentioned.

A man without affurance is liable to be made uneasy by the folly or ill-nature of every one he converses with. A man a sthout modelty is lost to all fense of honour and virtue.

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people of depraved mines and more than the people of depraved mines and more they are not able to more a man and the people of the people of depraved mines and more than the people of the people of

Such a perion feems x zero mas a manufactura in spite of himself, and m minutes at a manufactura in spite at a manufactura at

Upon the whole, I would enterwhen I was in the maxim, that the practice of vurne is the most proper section to give a man a becoming affurance in the words and always feeks to fheirer their in one at the entermedant is formetimes attended with name.

I have, for the ease of the seamen difficience at the ward of each of the foregoing leffons, into a regular mass that prefixed to each word, or purate, its number. & the numbered in the plate; by which, the marginer mass the pure a may be seen at one view.

P =

In the first lessen is inserted every conforant belonging to each word, with the point for every vowel; which practice, as was before observed, the learner must pursue, till he be very ready in both writing, and reading, all his exercises. The first ten words in this lessen have their characters formed separately from each other.

In the fecond leffon no more letters in a word are inferted than are absolutely necessary to discover the found. The fingle consonant marks are also used for the words, propositions, and terminations they represent; and the characters for the double, and trable letters.

The third leffun is written upon the most finished principles of this art. Above all the advantages which it positions, in common with the second leffun, it has, moreover, all the abbreviations delivered in the foregoing rules. And which rules the writer should have very perfectly in his ministry.

### LESSON I. (See the Plate)

: Iknow	s4 Modesty	A7 10
a no	as and	47 to 48 fignify
3 two	66 Affurance.	49 a theepith,
4 words	27 To	ço awkward
c that	a'B fay,	çı fellow,
s that o have	sg tuch	se who
7 been	30 A one	53 has
8 more	3 r in	54 neither
g abused	32 a modest	ςς good
10 by	33 man,	c6 hreeding.
11 the	34 fometimes	57 politenets,
18 different	35 indeed	58 nor
13 and	30 paffes	59 any
14 wrong	37 for	60 knowledge
15 interpretations	38 n good	61 of
16 which	39 character;	6s the
17 Are	40 but	64 world.
r8 put	41 nf	64 Again,
19 upon	43 prefent	65 a man
20 them,	43 is	66 of
ar than	44 very	67 affurance,
as thefe	45 often	of though,
23 two,	46 used	bg at

70 first.	gs the	Tie W
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72 denoted	94 of	in the
73 a períon	9; desency	try 🗯
74 of	gó and	ः हो ब
75 a free	97 morality	sig modelly
76 and	as without	est item
77 open	gg a blutte.	isi denig
78 carriage	100 I fhall	122 Confidencial
79 is	101 endervour.	123 with
80 now,	102 therefore,	124 tiest
81 very	103 in	125 of
82 ufually,	104 this	126 heepillmest.
83 applied	105 effay,	127 and
84 to	106 to	128 to
8 a profligate	107 restore	129 hinder
86 wretch,	10 <b>8 these</b>	130 impudence
87 who	100 words	131 from
88 can	110 to	132 patting
89 b <b>ran</b> k	111 their	133 for
90 through	112 true	134 affurance.
gr all	113 meaning;	•

# LESSON II.

ı If	21 for	41 is
2 I were	22 which	42 as
3 put	23 he	43 much
4 to	24 censures	44 fo
ς define	25 himself,	45 when
6 modesty,	26 or	46 he
7 I would	27 fancies	47 is
8 call	28 that	48 alone
9 it,	29 he	49 as
10 the	gó is	ςο in
11 reflection	31 exposed	ζι company,
12 of	32 to	ς2 and
13 an ingenuous	33 the cenfure	ζą as
14 mind,	34 of others.	54 Subject
15 either	35 For	śś to
16 when	36 this	ς6 a blush
17 a man	37 reason	57 in
18 has	38 a man	ς8 his
19 committed	39 truly	59 closet,
20 an action	40 modest	60 as

thort hand, in which the characters are all timple, firsight, or curve lines, except one circled character, one circular one, and a crota one. His alphabet to, therefore, more timple and fit for practice than that of any of his practice than the letters are fulficiently different from each other to prevent miliakes.

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Mr. Taplin's method of marking the vowels is fometimes by dots, and fometimes by the fituation of one of the conforants.

I have noticed the alphabetical characters only of the foregoing writers, without adverting to their other characters for double and treble letters, words, and phrases, as those characters form the flandard of each writer's system.

Concerning the alphabet I have here the honour to propose, I must just observe, that I have avoided all angular, compound,

and circular characters, and used only one curled one, which is for the letter g; and I trust I have made them sufficiently diffinct in their forms. There are some angled and compound characters, used for the treble letters; but then it should be remembered that each of these characters with a vowel point, will very often serve for a whole word, and I was as raid by indulging too great a simplicity in these characters I might degenerate into the modern uniformity.

The method of marking the vowels by points, as I have here advited, will be found a very great faving of time. It will also afford those who can so far depend upon their memory, an opportunity of entirely omitting them, till the writing be finished; when, by an attentive perusal, the piece may have all its warels marked; which will render it intelligible to the writer at a future time, when he has, perhaps, forgotten the subject matter.

### A PRAXIS.

#### OF THREE LESSONS.

## On Modelty.

Lesson I.—I know no two words, that have been more abused by the different and wrong interpretations which are put upon them, than these two, Modelly and Assurance. To say, such a one is a modest man, sometimes indeed passes for a good character; but, at present, is very often used to signify a sheepish, awkward fellow, who has neither good breeding, politeness, nor any knowledge of the world.

Again, a man of affurance, though, at first, it only denoted a person of a free and open carriage, is now, very usually, applied to a profligate wretch, who can break through all the rules of decency and morality without a blush.

I shall endeavour, therefore, in this essay, to restore these words to their true meaning; to prevent the idea of Modesty from being confounded with that of Sheepishness, and to hinder Impudence from passing for Assurance.

Vol. 1. P Leffon

120 OF PRN	MARRIE.
go It is	77 thus
gr more	78 mixed
as than probable,	79 and blended
33 that the prince	go together,
above mentioned	81 they
15 poffeifed both	ge combote
36 these qualifications in	83 what
17 a very	84 we endeavous
38 cminent	By to expres
39 degree.	86 when
40 Without affurance	By we fay
41 he	88 a modest assurance:
4s would never	8g by which
43 have undertaken	90 we understand
44 to fpcak	91 the just mean
45 before the most	92 between
46 angust	93 ballifulness and impudence.
47 Affembly	94 I shall conclude
48 in the world;	95 with observing,
49 without modefly	96 that
50 he	97 as the fame
51 would have	98 man
ça pleaded	99 may be
53 the cause	100 both modelt and affored,
çı he	tor fo it is also
çç had taken	rea polible
ç6 upon him.	tog for the lame
67 though it had	104 perion
så appeared	tog to be
co ever	106 both impudent and halk-
60 to feandalous.	ful. '
6) From what	107 We have
62 has been	roß frequent
6. taid,	tog inflances
64 it 14	tro of this
6 c plain,	ttt odd
66 that modefly and affurance	tra kind
fiz are	113 of mixture
68 both	114 in people of
69 amiable.	ris depraved
70 and n ay	116 minds
71 very well	117 and mean
n meet	118 education 1
73 in the fame	11g who,
74 perion.	ino though they
75 When	181 are not able
76 they are	148 to meet

Q

seg a man's 184 eyes, 185 or pronounce 186 a fentence 127 without confusion. 188 can 289 voluntarily 130 commit 131 the greates 13s villanies, 193 or most 134 indecent 135 actions. 136 Such a person 137 feems 138 to have made 139 a resolution 140 to do ill, 141 even 142 in spite 143 of himself. 144 and in defiance 145 of all 140 those checks 147 and restraints

148 his temper 149 and complexion

1 co feem

151 to have laid 158 in his way. 153 Upon the whole, 154 I would endeavour 255 to establish
250 this maxim, 157 that the practice 158 of virtue 259 is the most 100 proper 161 method 16s to ĝive 163 a man 164 a Decoming affurance 165 in his words 166 and actions. 167 Guilt 168 always 169 feeks 170 to shelter 171 itself 17s in one 173 of the extremes, 174 and is 175 fometimes 176 attended 177 with both.

### CHAP. III.

## Or VULGAR, ARITHMETIC.

#### SECT. I.

#### notation of numbers.

ARITHMETEC is the most necessary of all the science.

From hence we may account for the perfection to which the part of literature is brought, above any other branch of mathematical science.

Notation, strictly speaking, is that part of arithmetic which teaches how to write any number by its proper characters, or figures, and consequently in their due places; also to read, or discover, the true value of such number, when written.

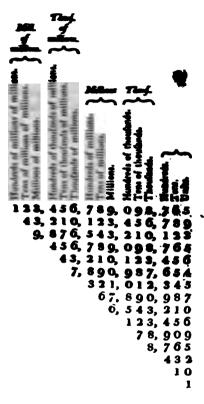
All numbers, and the various combinations of them, are noted by these ten characters, 1 one, 2 two, 3 three, 4 four, 5 sive, 6 six, 7 seven, 8 eight, 9 nine, 0 cypher or nothing.

Each of these characters, when used alone, stands for no more than its own intrinsic value: thus, I stands only for one in number, 2 for only two, &c. But when any of them are joined to other figures, they together stand for more than their own real separate value: thus, I and 2, joined together thus, I2, stands for twelve; 6 and 5, joined together, stands together, stands together, stands together, stands together, &c.

In order to discover the value of any compounded number, it must be observed, that a number placed in the first place towards the right hand flands for no more than its real intrinsic value, but increases in value in a tensold proportion by every remove towards the left hand; thus, in the number 1799, the first figure 9 frands for 9 early; the second figure being in the second place towards the left hand, its value is increased tenfold: thus it represents ninety, or tes times nine; which, with the foregoing a, flands for ninetynine. Again, the figure 7, which flands in the third place towards the left hand, is increased to ten times as much as it would be if it flood in the next inferior place, viz. where the last-mentioned 9 stands: thus it represents seven hundred; which, with the two fore-mentioned figures, fland for feven hundred and n'new-nine. The figure 1, which flands in the fourth place, towards the left hand, is also increased ten times in value to what it would be if it flood in the next inferior place, where the 7 is placed; in which case it would repre-Tent one hundred, whereas, in the prefent infrance, it flands for one thousand; and with the other figures represent one chousand, seven bundred, and ninety-nine.

This description of the four foregoing figures may serve to give the uninformed an idea of the value of figures, according to the different places they occupy in a compounded number. For every remove of a figure towards the left hand increases its value to ten times as much as before; as will more fully appear by the following table, called the Numeration Table:—





In order to read any number with facility and eafe, it is necessary that the learner have all the names of the numbers at the head of the table perfectly in his memory, that he may apply them to any other number he may have occasion for; calling the first figure, on the right hand, units; the second, tens; the third, hundreds; the fourth, thousands, &cc. as in the table.

Thus, the bottom figure in the table, standing under the The next place of units, is itself an unit, or a single one. higher

higher number in the table confilts of two figures, 1 and 0: the first whereof, standing in the place of tens, flands for ten, being only a figure one; the other figure, being a cypher, and in the place of units, stands for nothing, or me units: these two figures, therefore, express only ten. The next number confids of the figures 428; the four being in the place of hundreds, figuifies fo many hundreds; the three, as many tens; and the two, as many units; and is thus exprefied: four hundred and thirty-two. The fourth number in the table confifts of four figures, the first whereof stands in the place of thousands; this number, therefore, is thus expressed: eight thousand, seven hundred, and sixty-five. The fifth number has its highest figure in the place of team of thousands, and is thus expressed: seventy-eight shouland. nine hundred, and nine; it having a cypber in the place of tens, which flands for nothing. The fixth number confids of hundreds of thousands, and is thus expressed: one hundred and twenty-three thousand, four hundred, and fifty-liv. The highest place of the seventh number is that of millions: it is expressed thus: fix million, five hundred and forty-three thousand, two hundred, and ten. The eighth number confifts of tens of millions, and is thus expressed: fixty-seven million, eight hundred and ninety thousand, nine hundred and eighty-seven. The ninth number has its highest figure in hundreds of millions; it is expressed thus: three hundred and twenty-one million, twelve thousand, three hundred, and forty-five.

The fix other numbers are expressed as follows:—The tenth number: seven thousand, eight hundred and ninety millions, nine hundred and eighty-seven thousand, fix hundred, and fifty-four. The eleventh number: forty-three thousand, two hundred and ten million, one hundred and twenty-three thousand, four hundred, and fifty-six. The twelfth number: four hundred and fifty-six thousand, seven hundred and eighty-nine million, ninety-eight thousand, seven hundred, and fixty-sixe. The thirteenth number:

sine million of millions, eight hundred and feverey-fix thousand, five hundred and forty-three million, two hundred and ten thousand, one hundred, and twenty-three. The fourteenth number: forty-three million of millions, two hundred and ten thousand, oge hundred and twenty-three millions, four hundred and fifty-fix thousand, seven hundred, and eighty-nine. The fifteenth number: one hundred and twenty-three million of millions, four hundred and fifty-fix thousand, seven hundred and eighty-nine millions, ninety-eight thousand, seven hundred, and fixty-five.

I have, in the table, diffinguished every three figures by a point, or comma, beginning at the right hand, so is generally done in public offices, and by men of extensive befiness.

This method also affords an eatier way of anumerating numbers, than by the foregoing table, as everythree figures may have a common furname appropriated technol (inferted in italics at the head of the table), belides their names of units, tens, and hundreds: thus, when the learner can entmerate the first three figures in a number, and knows the proper furname to apply to each three figures, he may coumerate any number, however large. The first three figures on the right hand have no farname, as they stand simply for units, tens, and hundreds; but the next three figures have the furname of thousands; the next three have the furname of millions; the next three, thousands of millions; and the other three figures have the furname of millions of millions. Thus, to repeat the highest number in the table, beginning at the left hand, I fay one hundred and twenty-three (to which I add its furname of) million of millions; four hundred and fiftyfix (with its furname) thousands of millions; seven hundred and eighty-nine (with its furname) millions; ninety-eight (furname) thousands; seven hundred, and fixty-five.

I have been more particular in the description of the Numeration Table, as it is generally found the most difficult of all the tables in Arithmetic to a learner; and several persons who have arrived to a tolerable proficiency in this science.

are, nevertheless, very imperfectly acquainted with this most effential part.

Befides the foregoing ten characters used to express numbers, there are also letters employed for the same purpose, called Numerical Letters. This was the ancient assethed of expressing numbers; and is still number use of frequently, in the title-pages of books, and is suneral anonuments in Roman history, to express the date of the year.

I, stands for one.
V, five.
X, ten.
L, fifty.
C, an hundred.
D, or IO, five hundred.
M, or CIO, a thousand.
IOO, five thousand.
CCIOO, ten thousand.
CCCCIOOO, a hundred thousand.
IOOO, fifty thousand.
CCCCIOOOO, a hundred thousand.

dred thousand, or a mil-

The letters MDCCCIII express the number 1803, the date of the present year—M standing for one thousand, D for sive hundred, CCC three hundred more, which is eight hundred, and III three; together one thousand, eight hundred, and three.

If a letter or letters of inferior value follow one of superior value, they are to be added thereto: thus, VI signify six, VII seven, VIII eight, and DCC seven hundred. But when a letter of inferior value is placed before one of superior value, it is then to be deducted therefrom: thus, IV signify four, IX nine, XL forty, CD four hundred, &c.

#### SECT. II.

#### OF ADDITION.

Apprison is that part of arithmetic which teaches how to add two or more numbers or fume together, in order to discover the total, or value of the whole.

Addition of whole numbers is principally divided into two parts: namely, Addition of numbers of one denomination; and Addition of numbers of divers denominations.

Addition of numbers of one denomination confids in adding together simple numbers or sigures; in which it such be firstly observed, that the units are to be set directly under each other, in the same column; the tens, in like manner, under each other; the hundreds also under each other; the thousands also, tens of thousands, and those of every degree, are all respectively to be placed in their respective places, from the right hand, to which their rank entities them; the in the following examples:—

Tds.	£.	Gallens.
<b>9</b> I	171	184731
18	239	648943
33	713	756574
17	604	818973
49	830	861413
54	135	963678
88	100	347365
208	2704	4479671
	-	

The feveral numbers to be added together being fet down in a regular order, as feen above, they are to be added together; beginning at the bottom figure on the right hand, and proceeding upwards, till you have added all the figures in one column together; then place the first figure on the right hand, or unit figure, of the sum so found, under the same column, carrying the remaining figure or figures, if any, to be added to the next column: having discovered the amount of the second column, place the unit figure also under

the

the same column, adding the other figure or figures to the next column, proceeding in this manner till the whole be finished, and setting down the total amount of the last column under the same.

Thus, in the first example, I say 2 and 4 is 6, and 9 is 15, and 7 is 22, and 3 is 25, and 2 is 27, and 1 is 28; this being the amount off the first column, I set down 8 (which is the figure in the place of units) under the same column; and carry the remaining squre 2 to be added to the next column; saying, 2 and 2 is 4, and 5 is 9, and 4 is 13, and 1 is 14, and 3 is 17, and 1 is 18, and 2 is 20, the whole amount of the last column; wherefore I set it down under the column, and the total is thus found to be 208.

Proceeding in the same manner, in the second example, I say 5 and 4 is 9 (for the o stands for nothing), and 3 is 52, and 9 is 21, and 1 is 22; wherefore, I set down the 2 under the column, and carry the remaining 2 to be added to the next column; saying, 2 and 3 is 5, and 3 is 8, and 1 is 9, and 3 is 12, and 7 is 19, the amount of the second column; wherefore I set down the 9 under the column, and carry the remaining sigure 1 to be added to the next column, saying, 1 and 1 is 2, and 1 is 3, and 3 is 11, and 6 is 17, and 7 is 24, and 2 is 26, and 1 is 27, the amount of the sast column, and to be set under the same; wherefore the total is 279s (two thousand seven hundred and ninety-two).

In the fame manner the third example is wrought; as also the three following; in which the operation is purposely omitted, for the practice of the learner.

Gallons.	Yards.	£.
17964017	12794368	1'.729430
43706123	64368401	12090736
94218742	20107036	67342617
£9991815	45736298	742:,8064
58007252	12449327	29020721
55122753	72976517	4.739402
Total 300000700	Total 228147147	Total 2412200/10
284036683	\$15652779	224491540
<b>Proof</b> 300000700	Proof 228.4.47 147	Proof 241221. 60
Vol. J.	K	liere

Here it must be noted, that when the amount of any column in any sum has a cypher in the place of units, such cypher is to be placed under the column; as in the first of the three last examples.

The three last examples are proved—which is done in this manners after the total is sound according to the foregoing rules, and placed in the first of the three bostom lines, the top line of the sum is to be separated by a line drawn under it, the remaining part of the sum cast up, and the amount of it placed under the aforesaid total; this last amount, and the top line of the sum, are then to be added together; and if the amount of these two lines be equal to the total in the sirk bottom line, the sum is rightly cast up; otherwise net.

All other fums in addition are to be proved in a finisher manner, whether they be of one denomination or of divers denominations.

Addition of divers denominations confifts in adding togsther numbers of different denominations, whether they be money, weights, or measures.

Before the learner proceeds to addition of money, it is necessary that he have the following tables by heart; called the Pence Table, and the Stalling Table.

Th	e Pence T	$\Gamma at B$	" <b>•</b>	<i>T1</i>	k Shilling T	able.
20	ponce is	i. 1	d. 3	20	fhillings is	f. s. 1 0
30	_	2	6	30		1 10
40		3	4	40		8 0
50		4	2	50		2 10
60	- • -	5	Q	60		3 0
72	-	5	ıυ	70		3 10
80		6	8	80		4 0
4,2		7	6	90	-	4 10
1113	-	8	4	100		5 0
115	*****	9	2.	110		5 10
120	-	10	0	120		6 0

In addition of divers denominations, those numbers which are of the same denomination are always placed in the same column, and their name or mark generally at the top: thus, in addition of money, the pounds are placed in one column, with an £ at the top for libra, the Latin word for pounds; the faillings in another column, with an a at the top for folidis, the Latin word for fillings; the pence also by them-falses, in another column, with a d at the top for denoming the Latin for pence; and sometimes the farthings are placed in a separate column, with a qr. at the top for quadron; but the most general rule is, to place them immediately after the pence, as a fraction of a penny: thus, \( \frac{1}{2} \) for one south part of a penny, or one farthing; \( \frac{1}{2} \) for one half, or a half penny; \( \frac{1}{2} \) for three souths of a penny, or three farthings: as in the following examples:—

6. s. d.	6. 6. de	£. s. d.
5 7 4	27 9 44	172 9 2
12 0 8	136 4 0	225 8 74
1 6 19	124 11 3	144 19 11
979	90 7 9 <del>2</del>	176 12 10£
80 10 4	166 19 104	238 17 11
3 15 16	101 7 94	234 14 72
272	24 0 04	814 17 19
6 19 18	107 15 6	937 2 0
52 :5 19	778 15 74	3445 0 11
47 8 1	751 6 3	2272 11 42
52 15 10	778 15 74	3445 9 114
	Contraction of the last of the	

In addition of numbers of divers denominations, this is the general rule:—To begin at the right hand column, or the Estam of the leaft denomination; adding all the numbers in the faid on usen together, and observing how many units there he is it of the next higher denomination, and how then overplus: the overplus is to be fet down under the face, and the units of the next denomination are to be added to the next column. The next column being taking, it must be a next column. The next column being taking, it must

also be noted how many units there are in it of the next higher denomination, and how much overplus: the overplus is to be placed under its own column, and the units of the next denomination added to the next column, as before; and so on to every new column.

Thus, in the first of the three foregoing examples, I begin with the unit figures of the lowest denomination, which is pence, faving, 1 and 2 is 3, and 1 is 4, and 4 is 8, and 9 is 17, and 2 is 19, and 9 is 28; to which I add the tens in the fame column, faying, 28 and 10 is 38, and 10 is 48, and 10 is c8; now, by the pence table. I know that co pence is 4 shillings and 2 pence, therefore 58 pence is 4 shillings and 10 pence: thus, I must set down the 10 pence, which is the overplus, under the same column; and the & shillings, which are 4 units of the next higher denomination, I carry to be ailded to the next denomination, faying, 4 and 9 is 13, and 7 is 20, and 5 is 25, and 7 is 32, and 6 is 38, and 7 is 45; to which I add the tens, faying, 45 and 10 is 55, and 10 is 65, and 10 is 75: now, by the fulling table, I find that 75 shillings is a pounds of shillings; the of shillings are to be fer under the column of flullings, and the 3 pounds, being units of the next denomination, viz. pounds, are to be added thereto; and the pounds, being the laft and highest denomanation, are to be idded together as fimple numbers of one denomination, and the total placed under the fune: thus the total is found to be 52%, 156, 15%.

In the next example I begin with the firthings, being of the lowest denomination, saying, 2 farthings and 2 is 4, and 2 is 7, and 1 is 8, and 2 is 10; 10 fathings is 2 pence and 2 farthings; the 2 fathings is to be set under the line as overplus, and the 2 pence is to be added to the column of pence, which, added up, amounts to 43 pence, which is 3 shillings and 7 pence; the 7 pence is to be set under the column of pence, and the 3 shillings is to be added to the column of shillings; in which column, with the 3 added, there is 75 shillings, or 3 pounds 15 shillings; the 15 shillings,

lings must be placed under the shillings, and the 3 pounds added to the column of pounds, and the pounds added together as before, and the total placed underneath: thus the amount of this sum is 7781. 151. 74d.

In the same manner the third, and every other sum in this part of addition, is to be wrought. The sums are all ready proved, for the ease of the learner. The line under the total shews the amount of the sum without the top line: the bottom line shews the amount of the line just over it added to the top line of the sum, and proves the work right, by being equal to the first total.

### More Examples for the Learner's Practice.

£. s. d.	£. s. d.	£. s. 2.
472 7 12	$1762 9 6\frac{1}{2}$	179 9 91
19 2 0	1000 3 2	184 19 OF
145 19 10 <del>1</del>	10 10 6 <del>1</del>	200 7 9
7 0 1	12 9 3	301 <b>8</b> 10 <del>1</del>
o 10 6₹	17 4 03	401 6 4
27 8 2	123 18 0 <u>1</u>	21 8 7 <del>\$</del> 33 0 0 <del>\$</del>
30 7 9 <del>1</del>	129 0 0	33 o o <del>i</del>
145 0 4	71 6 9 <del>1</del>	12 12 0½
301 10 10	41 2 11	19 4 4 8 8 c <del>I</del>
<sup>2</sup> 9 7 <sup>2</sup> / <sub>2</sub> 6 6 0	7 4 2 4 8 8 0	
660	8 8 0	$\frac{6}{12}$ 10 $\frac{1}{2}$
1185 0 2	3183 16 54	1368 17 9
712 12 91	1421 6 114	1189 7 11
1185 0 2	3183 16 53	1368 17 9

### Addition of Avoirdupois Weight.

By this weight are weighed all kinds of goods whatever, except bread, gold, filver, and precious fiones.

# The Table of Avoirdupois Weight.

4 quarters	make	t dram,	410	marked	dr.
16 drams		i onnce,			04.b
16 ounces	_	ı pound,			16.
s# pounds		1 quarter of	a hundred w	eight,	gr.
4 quarters	-	s hundred w		**	C.
so hundred	weight	t ton.			T.

Avoirdupois weight is divided into two parts, called the greater and the lefs. Avoirdupois the greater confids of hundreds, quarters, and pounds; avoirdupois the lefs is divided into pounds, ounces, and drams.

4 28	4 28	16 16
C. qri. lb.	G. qrs. lb.	16, wz. dr.
7 3 12	24 2 4	9 9 19
16 0 9	10 0 9	60 13 14
13 6 7	0 1 20	37 12 0
37 1 0	<b>84 8</b> 0	49 4 7
<b>8</b>	36 3 21	62 0 1
40 0 60	49 <b>6</b> 9	10 7 0
130	50 1 62	. 11 6 7
207	40 0 19	14 0 18
123 1 6	227 2 11	215 6 3

These examples are wrought in the same manner as the former; but having regard to the avoirdupois table, instead of the pence table. And the number of units in each column, which compose an unit in the next higher column, is placed at the head of the column; thus, in the suff example, as all is the number of pounds which form one quarter of an hundred, it is placed over the column of pounds; and 4, which is the number of quarters contained in an hundred, is placed over the column of quarters. And in the last example, to being the number of drams contained in an ounce, it is placed over the column of drams; and, as to ounces form a pound, to is placed over the column of

ounces:

ounces; and the like is observed in addition of other weights and measures.

In the first of these examples the number of pounds in the first column is 6s, which is a quarters, and 6 pounds over; the 6 is to be set under the pounds, and the a quarters added to the column of quarters, which, with the amount of the whole column, is 13 quarters, which is 3 hundreds and t quarter; the 1 quarter is to be set under the quarters, and the 3 hundreds added to the next column, and the whole amount is found to be 123c. 1qr. 61b.

# Addition of Troy Weight.

By this weight are weighed bread, gold, filver, and precious stones. The tifual denominations are pounds, ounces, pennyweights, and grains.

# The Troy Weight Table.

#4 grains #	nke :	I	pennyweight.
so pennyweigh	<b>ts</b> :	ı	ounce.
18 OUNCES	1	ī	pound troy *.

# Examples of Troy Weight.

18 20 24 16. es. pav. gr.	12 20 24 16. az. prv. gr.	12 20 24 16. oz. prv. dr.
4 9 1 17	12 7 11 21	32 9 2 20 154 8 1 0
7 0 17 8	19 2 19 8	47 0 19 21
0 10 14 80	20 10 7 7 7 11 6 12	30 2 13 13
4 11 10 11	14 10 0 15	347 7 9 9
7 4 3 5 28 10 19 3	18 0 10 12	1,170 6 6 1
		The second secon

The goldfmithe divide the pound troy into 12 marks, inflead of counces; and each mark into 24 carats; and each carat into 4 grains

These examples are wrought according to the general rule given in the former part of this section, and in the same manner as addition of avoirdupois; but paying a strict regard to the table, or the figures at the head of each column.

Nore. That the pound avoirdupois is heavier than the pound troy; but the troy ounce is heavier than the avoirdupois ounce, for 116. Box. 12900. troy is equal to a pound avoirdupois; and a pound troy is about 1300. 2240. avoirdupois.

It is unnecessary to give examples of the other parts of addition, concerning apothecaries' weight, liquid, dry, and long measures, &c. as the same method serves for all of them; having respect to the table belonging to each.

# The Table of Apothecaries' Weight.

20 grains	make	r feruple,	marked 9.
3 feruples	-	z dram,	3.
8 drams	-	t mince,	3.
ts ounces	-	r pound,	<b>√</b> .5.

By this weight apothecaries mix their drugs; but they are bought and fold by avoirdupois weight.

### The Table of Wool Weight.

7	pounds	กาสke	t clo <del>ve</del> .
2	cloves, or r	4lb.	a flonc.
	Aene, or a8	lb.	r tod.
6	tod and a h	alf	t wey, or 1821h.
	wers or 36	4lb.	t lack.
12	<b>Gecks</b>		r last, or 43681b.
40	lb.		a pack of wool.

Note. That a stone is generally 14th, in most parts of England; but among the London butchers it is only 81b.

# The Table of Cloth Meafure.

make	1 quarter of a 3	ard.
	ı yard.	
:		
1	dell French.	
	1 ell Flemich.	•
	make	1 ell English.

# The Table of Wine Measure.

8 pints	make	1 gallon.	
42 gallone	-	ı tierce.	
63 gallone		1 hogshead.	
84 galions	-	1 puncheon.	
s hogsheads	_	1 pipe, or butt.	Ċ
2 pipes, or b	utts	z tun, or s 52 gallons	•

Note. That sweet oil hath only \$36 gallons to the tun. All liquids are measured by wine measure, except beer and ale.

# Ale or Beer Meafure.

8 pints	make	ı gallon.
S gallons		ı firkin.
2 firkins		ı kilderkin.
s kilderkins		ı barrel.
1 barrel		1 hogfhead.

The ale and beer gallons are the fame; but the beer firkin contains 9 gallons; confequently, the kilderkin 18, the barrel 36, &c.

In a Tun of Wine there are,	In a Pipe, or Butt, there are,		
a pipes, or butts. :	s hogsbeads. ::		
6 tierces.	3 tierces.		
252 gallons.	rs6 gallons.		
504 pottles.	a (a pottler.		
1008 quarts.	con quarts.		
2016 pints.	1008 pints.		
Vot. L	In.		

In a Punchean there are,

84 gallons.

108 pottiss.

336 quarts.

67s pints.

In a Hag fiead there are,

63 gallons,
286 potiles.
858 quarts,
504 pints.

### In a Barrol of Boer there are,

a kilderking.

4 firkins.

36 gallons.

78 pottige...

144 quaria

s88 piets.

#### In a Barrel of Ale there are,

a kalderkins.

A firkup.

3ª Kullons.

64 postice.

rall quarts.

agé puits.

# The Table of Dry Meafure.

s pints makç s quart. s quarts i pottle. gallon. s pottles a gallona 1 peck. 1 buthel, land meature. 4 pecks i bufliel, water measure. ς pecks 3 buffiele 1 fack. ملوملتونا م s comb, or half quarter. e combe J QUARTEL. s chaldron. 4 quarters 5 quarters I Wry. & Weys s lait, or so quarters. 4 fats or vate, or 36 buffiels : chaldron.

Note. That in wheat flour there are always five huftiels to the fack a and fall and fea-coal are heaped, or elie there are five pecks to the huftel.

A 14 6

In a Last there are, to quarters. 80 buthels. 320 pecks. 2566 quarts. çuso pints.

In a Wey there are, 5 quarters. 40 bushels. 160 pecks. 320 gallons. 640 pottles. 1880 quarts. a 560 pints.

# Long Meafure.

3 barley-corns	make	r inch.
ta inches		ı luot.
3 feet		ı yard.
3 feet, o inches		r ell English.
3 feet, 9 inches	_	a geometrical pace.
6 feet		ı tathom.
51 yards	•	1 pole, perch, or rod.
40 poles, or perches		r furlong.
8 furlongs	`	r English mile.
3 miles		1 league.

#### In a Mile there are,

8 furlongs.	5 s 80 feet.
380 poles.	63360 inches.
1760 yards.	190080 barley-corns

# Land Meafure.

5å yards	make	, pole, pe	rch, or rod.
46 Iquare poles"		1 rood, 0	r quarter of
2 60' Iquare poles	-	ı acre.	[an acre.
80 poles in length, and	s in breadth	ı acrè.	
40 poles in length, and		I acre.	
4 polei in length		ı chain.	
to chains in length, and	l i in breadth	ı acre.	
	ο.		G.L.

### The Table of Time.

6d seconds	make	s minute.
60 minutes,		1 hour.
s4 hours	-	z day, natural.
7 days	***	1 week.
4 weeks		1 month, lunar.
12 months, 1 day,	and near 6 hours	1 solar year.

#### In a Year there are,

13 months, 1 day, 6 hours.	8,766 hours.
52 weeks, 1 day, 6 hours.	525,960 minutes.
365 days, 6 hours.	31,557,600 seconds.

Note. The folar year is divided into 12 unequal months, called calendar months, according to the ancient verse, which may serve to impress the number of days each month contains, on the memory:

Thirty days hath September, April, June, and November; February hath twenty-eight alone, And all the rest have thirty-one.

#### SECT. III.

#### OF SUBTRACTION.

SUBTRACTION, vulgarly called Substraction, teacheth how to take a less number from a greater; and sheweth the remainder, excess, or difference. Thus, if I take 7 from 9, there will remain 2.

Rule. Place the less number under the greater; observing, that the figures of each denomination in the less number fland directly

directly under the figures of the same denomination in the greater number, that is, the units under units, tens under tens, and pounds, shillings, pence, ounces, drams, &c. &c. directly under the same, as in addition. Then, beginning at the right hand, or the least denomination, take the value of each figure in the less number from that in the greater number, which stands directly over it; setting down the remainder underneath. Proceed in this manner till the work be sinished. But if, as it frequently happens, any single sigure in the less number be greater than that in the greater number, from which it is to be taken, an unit is to be borrowed from the next figure towards the less than do the greater number, and added to the uppermost sigure, that the bottom sigure may be taken therefrom; which borrowed unit must be paid, or added, to the next figure of the less number on the less thand-

#### Examples.

Prom 6954 Take 5443	1719886	370290370 greater numbers. 128403402 lefs number.
Rem. 1511	630979	841880878
Proof 6954	1789886	370200370

To flew the use of this rule, I say—Suppose a merchant owed 69541, whereof he has paid 54431.: to know what remains to be paid, the sums are to be set orderly one under the other, according to the foregoing rule, and as seen in the examples: then, beginning with the unit sigures, in the first example, I say, take 3 from 4 and there remains 1, which I set under the line; next take 4 from 5 and there remains 1, which is also set under the line; again, take 4 from 9 and there remains 5, which must be set down as before; and, lastly, take 5 from 6 and there remains 1: thus there remains due 15111.

Subtraction is proved by adding the remainder to the lets of the two given numbers, and if the total of these two numbers amount to the exact sum of the greater number, their

work is right; interesting our colony, in this example, I god the runnimies excell to the left number 54437, and the amount is highly, the looks at the greater number.

In the farmula hample, I herein with the units, as inchare a faying, take y from 6.1 cannot, but by horrowing a from the near figure B. and which added to the bimakes in the # being the next inperior number), I lay, a from 16 and there conditions their, for the chart I busined, I early can ection to the next figure of the left number, faving, a that \$ Interested and a to but to therefore, I from & and there tamains 73 aprile, of from 8 1 campar, but luncoving a no below from the next figure, I fay, of from it and there remains as then for a that I bear wad. I must add the the meet figure is, laying, of from a and there remains a fwhich may always In theme when the two figures are the farms) & again, o from a Leannest, but o from its theappearing a from y) and there remains a then I that I begressed, added to the equal taken from the gethere tamina to this the work in finitheal. The found descendentes is right.

Princiding in the fame mount in the third example, I fay; a firm of count, but a from 11 (burrowing a from the 7), there remains it; then a that I horrowed sind to be in, to from y I cannot, but to from 17 and there remains y; again, a that I horrowed and a is 1, 1, from a I count, but a from a g (burrowing 1) and there remains it; then, A from a (us muching) I cannot, but a from remains it; again, a, that I horrowed, from a paid there remains it; and a from 12 and there remains it; and a that I horrowed and it is 1, from 10, and there remains it; and a that I horrowed and it is 1, from 10, and there remains a; and a that I horrowed and it is a 1, from 10, and there remains a; lattly, a from y and there remains a; lattly, a from y and there remains a; lattly, a from y and there remains a.

#### Mine Laumples.

Pan cyngay	कार्यात्रक्षेत्र	र १९१४ रहते । साम्याहर गामाणे.
Taka cayn cy	कार्यात्रीत्रात्री	१ १४४७मा विक मतामाणिक.
Bong gendh	कवात्रीय्रीत्रात्र	१ १४७मा विद
Print ly Buyly	44774394	1 11/4 46 11 1

The number of years finer any event happened, may be diffeovered by fubtracting the date of the year the event happened from that of the pretent year. Thus :---

The prefert year 1804. The figs of London 1969.	Spanish 1 Set	Charpowder   1804 Treaten   1904
Years there Till	* 1 t	No.
Proof They	18.04	្តែកើ

Subtraction of divers denominations is performed upon the fame principle as inhtraction of numbers of one denomination. Observing, that when an unit is horrowed of the next higher denomination, it must be considered according to its true intrinsic value, and must be repaid to the lower signic of the same denomination; as will be seen in the following examples:—

		10	18 4		• 3	17 1
	Ľ.	4.	d.	Ĺ.	١,	./,
Money owing	17	14	υŧ	104	14	7\$
bissi	ıú	10	6	111	11)	IJ <b>ŧ</b>
Remains		4_	<u>_</u> 34	. !!	14	te <b>j</b>
Press	17	14	υ	101	1.1	. 1
	14-16				11	<u>.</u>

In the first of these examples, beginning with the faithings. If ay, a farthings from a Leannot, but borrowing an unit from the next denomination, or a penny from the 10 penny (and which added to the 2 faithings makes 6 faithings), I have a farthings from 6 faithings and there remains a faithings, which I fet under the faithings, then for the unit I borrowed of the pency. I add a to the 6, faying 6 and a 12.74 now 7 from 9 and there remains 2; then to from 14 and there remains 4; lattly, no from 12 and there remains 7; thus the remains is 74.44. Add, which is proved in the example.

In the fecond example, I fay, a facthing from a and there remains a farthings, or an haitpenny, which I fet down in its proper place, viz. under the denomination of farthings at then a from 7.1 cannot, wherefore becoming a fhilling from the 14, and adding it to the 7 pence, which makes 14 pence. I say, a from 15 and there remains 152 then 1 that I bo

rowed

rowed and 19 is 20, 20 from 14 I cannot, wherefore I borrow 2 pound from the pounds, which, added to the 14, makes 34 fhillings; therefore, I fay, 20 from 34 and there remains 14; then 2 that I borrowed and 1 is 2, 2 from 3 and there remains 1; and 2 from 2 and there remains 1; thus, the answer to this fum is 111. 141. 102d.; and its proof, under the answer, shows that it is right.

### More Examples.

	_	10	114		10	12 4	_	20	114
_	£.	1,	d.	٤٠	s.	d.	£.	ı.	d.
Due	174	10	9 <del>1</del>	145	6	101	1294	19	10 <u>‡</u>
Paid	99	17	10	110	12	T I 🖢	1001	19	10
Remains	74	12	117	34	13	111	243	0	of
Proof	174	10	94	145	6	102	1294	9	10

If the money paid be paid at several times, the sums so paid are to be added together, and the total subtracted from the sum first due.

Due	£.	1. 10	d.	Received	£.	1. 10	d.
27.10		~ <u>`</u>	-:	**************************************		7	~
	10	10	o		( ;	10	6
Paid at Several	30	9	8	Paid to several	10	8	8
times	0	10	6	perlons '	12	12	0
•	3	9	4		20	19	10
	12	•			~ _9.		<u> </u>
Paid in all	59	Q	٥	Paid in all	55	1 1	•
Kelts duc	86	14)	6	Ress due	1064	19	0
Proof	145	14	6	Proof	1120	10	0
			-			-	===

#### Examples in Avoirdupois Weight.

Remains	2 U 27 12 3 50	30 8 85 1+7 2 9	7 0 15
Take	10 2 21	116 3 14	19 9 14
<b>4 7</b>	4 28 C. qrs. lb. 12 3 20	C. q.s. lb.	16 16 C. grs. lb.

### Examples in Troy Weight.

	H.	az.	so pres.	gr.	so en. pau.	
From	336	10	18	20	3184 16	<b>8</b> L
Tako	<b>947</b>	11	19	21	220 19	83
Remains					\$So3 16	8,3
Proof	336	10	18	80	3184 16	81

These examples, and all others of other denominations, are wrought in the same manner as subtraction of money; having respect to the table belonging to the denomination: thus, in the first example of avoirdupois weight, I say, take as pounds from so I cannot, wherefore I borrow 1 quarter of an hundred from the 3 quarters, and add it to the so, which makes 48 pounds; then I say, as from 48 and there remains a7; next, 1 that I borrowed and a is 3, 3 from 3 I cannot, wherefore I set down 0, as before hinted; lastly, 10 from 1s and there remains a.

The figures at the head of the columns show the number of units which each unit of the next higher denomination contains.

#### SECT. IV.

#### OF MULTIPLICATION.

MULTIPLICATION is, perhaps, the most necessary rule in arithmetic, for business, on account of its dispatch in resolving several long questions.

Multiplication teaches how, from two given numbers, to find a third, that shall contain either of the two given numbers as often as the other contains units: thus, 3 times 4 is 1s; here 3 and 4 are the two given numbers, and 1s is the third number, or product, which contains 3 as often as 4 contains units, viz. 4 times; or it contains 4 as often as 3 contains units, 3 times.

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There are three ends principally to be answered by multiplication:—

First. It serves to bring the greater denominations of money, weights, or measures into small ones; as, pounds into shillings, pence, and farthings; hundred weights into pounds, ounces, or drams; miles into yards, feet, barley-corns, &c.

Secondly. Having the length and breadth of a plain furface, we flud its contents.

Thirdly. Having the rate or value of any one thing, we know the rate or value of any number of fuch things, however great.

But before the learner can begin this rule, it is abfolutely necessity that he have the following table perfectly by heart s

The Multiplication Table.

The use of this table is, to find the product of any two numbers: thus, to find the product of 6 times 7. I look in the brace which has 6 at the point, and in the line which has 7 at the bagianing, appoint to which is the product, which is 40.

The table is to be thus read :-

Beginning with the first brace, I say—a times a is 4, a times 3 is 6, a times 4 is 8, a times 5 is 10, a times 6 is 19, a times 7 is 14, a times 8 is 16, a times 9 is 18, a times 10 is a0, a times 11 is as, a times 10 is 4.

Then, proceeding in the fame manner, I begin with the fecond brace, faying, 3 times 3 is 9, 3 times 4 is 12, 3 times 6 is 18, 3 times 7 is 21, 3 times 8 is 24, 3 times 9 is 27, 3 times 10 is 30, 3 times 11 is 33, 3 times 12 is 36.

Again, I begin with the third brace, faying, 4 times 4 is 16, 4 times 5 is 20, 4 times 6 is 24, 4 times 7 is 28, 4 times 8 is 32, 4 times 9 is 36, 4 times 10 is 40, 4 times 11 is 44, 4 times 12 is 48.

Then, I fay, 5 times 5 is 25, 5 times 6 is 30, 5 times 7 is 35, 5 times 8 is 40, 5 times 9 is 45, 5 times 10 is 50, 5 times 22 is 55, 5 times 12 is 50.

Then, 6 times 6 is 36, 6 times 7 is 48, 6 times 8 is 48, 6 times 9 is 54, 6 times 10 is 60, 6 times 11 is 66, 6 times 15 is 72.

Then, 7 times 7 is 49, 7 times 8 is 56, 7 times 9 is 63, 7 times 19 is 70, 7 times 11 is 77, 7 times 18 is 84.

Then & times & is 64, & times y is 79, & times to is 80, & times to is 88, & times to is 90.

Again, 9 times 9 is 81, 9 times 10 is 90, 9 times 11 is 99, 9 times 20 is 108.

Then, to times to is 100, to times it is 110, to times is is 120.

And, 11 times 11 is 181, 11 times 12 is 132.

Laftly, 18 times 18 is 144.

In multiplication there are three terms: viz.

The Multiplicand, 12 or fum to be multiplied;

Multiplier, 10

Product, 120 or refult of the whole.

Multiplication confifts of two parts: multiplication of numbers of one denomination, and multiplication of divers denominations.

Multiplication of numbers of one denomination is either fingle or compound.

Single multiplication is, when the multiplicand and multiplier, confist, each of them, of only 12, or less than 12; and may be performed by one operation, and with one product. Hence the greatest product that can arise by single multiplication is 144, as that is the product of 12 times 12.

Compound multiplication is, when the multiplicand or multiplier, or both, confift of more than 18, and requires more than one operation.

Rule. Place the multiplier under the multiplicand, in the natural order of figures, viz. units under units, &c.; then, if the multiplier confift of 12 or lefs, multiply every figure of the multiplicand by the multiplier; beginning at the place of units, and placing the units of the product right under the units of the multiplier; carrying the tens, or tens and hundreds, if there be any, to be added to the next product. Proceed in this manner through the whole, and fet down the whole product of the last figure, as in the annexed example; observing, for every ten that is carried to the next product, an unit is to be added thereto; and for every hundred, ten is to be added.

Multiplicand 1209
Multiplier 12
Product 14508

In this example, the multiplier being 18, I say, 12 times 9 is 108, wherefore I set down 8, the units of this product, and carry

carry 10 to be added to the next product, saying, 22 times 0, or 12 times nothing is nothing; thus I have no product from this figure, wherefore I set down the unit figure of the 10 I carried to be added to this product, which is 0, and carry the remaining 1 to be added to the next product; saying, 12 times 12 (as the two next figures in the multiplicand is 12) is 144 and the 1 I carried makes 145; wherefore I set it down, being the product of the last figures. And the whole product of 1209, multiplied by 12, is 14508.

But, if the multiplier confift of several places, after having multiplied the multiplicand by the first, or two first figures, as before directed, multiply it in like manner by the next, or two next figures, if they be 12 or less, and in like manner by all the other figures; placing the products below each other, strictly observing that the product of each new multiplier is to have its unit placed exactly under the unit in such new multiplier, and the subsequent sigures in their regular order towards the lest hand; and then the different products added together in the order in which they stand; as in the following examples:—

Example.	Proof.
Multiplicand 1097012	First multiplicand 1097012
Multiplier 1204	Half the multiplier 647
4388048	7070054
9873108	4388048
13164144	6382072
1419533528	First product, or 2d multiplicand 709766764  Proof, or 2d product 1410533528

In this example, I begin with the first figure in the multiplier (as the two sust are more than 12), saying, 4 times 2 is 2 times 4, that is 8, which I place in the sirst line of the product, and under 4 the multiplier; then 4 times 1 is 4, which I also set down in the next place; then 4 times 0 is 0, or nothing, wherefore I set down 0; next, 4 times 7 is 28, therefore I say, 8 to be set down, and carry 2; 4 times 9 is

16, and a that I carried is 48, 8 and carry 3; 4 times o is nothing, wherefore I have nothing to fet down but the 3 l carried; again, 4 times 1 is 41 thms I have done with the first figure in the multiplior. Beginning with the next, I say, g times s or s times g is 18, 8 and carry 1; the 8 is to be fet exactly under the multiplier at then a times t is a and t I carried is 10, 0 and carry 1; 0 times 0 is 0, wherefore I fet down the I carried; again, a times 7 is 63, 3 and carry 6; g times g is 81, and 6 is 87, 7 and carry 8; g times o is o, but 8 was carried; 9 times 1 is 91 thus I have done with the fecond multiplier. The next and last two figures in the multiplier being ta, I multiply by them as by one figure, placing the unit figure of the first product under that of the multiplier, which is the s; faying, 18 times s, or s times 18 is 24, 4 and carry s; is times t is is, and s is 14, 4 and carry 1; 12 times o is o, but 1 was carried; 12 times 7 is 84, 4 and carry 8; 12 times q is 108, and 8 is 116, 6 and carry 11; 12 times o is o, but 11 was carried, therefore I fet down 1, and carry 1; 12 times 1 is 19, and 1 is 19; which being the last, I set it down. The work being finished, all the several products are added together, and the total is the real product.

The work is proved by dividing the multiplier in half, and multiplying the original multiplicand by one half, and the product thence arifing by the number a, as feen in the foregoing example. But if the multiplier cannot be divided exactly in half, as is the cuic when it confifts of an odd number, then a number that is an unit lefs than the multiplier is to be divided in half; and the multiplicand multiplied by the one half, and that product by a, as before, and the original multiplicand added to the last product, as in the following examples:—

Example.
379643058
43a t
379643058
759886104
1138929156
1518578808
1640437627698

Proof.
379643058 8160
82778583120
379643 <b>052</b> 759 <b>28</b> 6104
820028992320
1640057984640
1640437627692

In proving this example, I cannot divide the multiplier 43sz exactly in half, because it contains an odd number in the place of units; I therefore take a number that is an unit less, viz. 43so, and divide it in half thus: saying, the half of four thousand is two thousand, and the half of three hundred and twenty is one hundred and fixty; which, together, is siso for the first multiplier in the proof; the product of which is again multiplied by s, and that product added to the first multiplicand, which gives a product equal to the product in the example: which proves the work right.

When the multiplier has cyphers intermixed with the other figures, the fignificant figures only are to be regarded as multipliers, observing the directions before given, to place the unit figure of each product under that of the multiplier; as in the following examples:—

Example.								
7	Q	6	3	8	2	4	9	
			,	2	0	4	ó	
7	6	4	9	8	5	l	1	
	7 8 7	7 9 5 7 6	7 9 6  8 5 5  7 6 4	7 9 6 3  8 5 5 2  7 6 4 0	7 9 6 3 8  8 5 5 2 0  7 6 4 0 8	7 9 6 3 8 2  2 0  8 5 5 2 0 9  7 6 4 9 8 0	7 9 6 3 8 2 4 8 5 5 2 0 9 6 7 6 4 0 8 0	

					1	o <sub>r</sub>	<b>0</b> 0	f.			
			2	7	9	6	3	8	20	4 2	9
2	7	5	5	9	8	7 2	6	4	9	8	0
2	8	5	2	3	1	0		3	9	8	0 2
5	17	o	4	6	2	0	2	7	9	6	o

When the multiplier, or multiplicand, or both, confift of cyphers

eyphers towards the right hand, and fignificant figures towards the left, such cyphers are omitted in the operation, and placed on the right hand of the product; as follows:—

Rnampie.									
3 /4	3 7	6	49	9	7 5	9		H	١.
								0	9
- 4	7	۵	49	Q	7 8	4			
91		ŧ	53	0	99				L
915	lol	ì,	9 8	6	7	ā	a	۲.	14
	Į		_	=			ı	ı	-

						1	P,	e4	/:				
	¥	8	7	6	4	9	0	7		5	0	0	9
3	9	3 5	00 a	4 0	48	5	4	04	0	0			
4	Ó	9	ŧ	180	*	0	8	9	0	9	0	9	0 8
919	3	8	8	4	5	3	6	17	0	0	0	0	0

In the proof of the last example, the multiplicand is added to the product as before directed, when the original multiplier cannot be divided exactly in half.

# Multiplication of divers Denominations.

Multiplication of divers denominations is performed by multiplying each denomination by the multiplier; beginning with the leaft denomination, and carrying the units of the next denomination to be added thereto, as in addition of money.

Multiplication of divers denominations is either fingle or compound; fingle, when the multiplier confids of is or less, and is performed by one multiplier; compound, when the multiplier confids of more than is, and requires more than one multiplier.

Z,	Bayample.								
£.	10	d. H							
		8							
70	_5_	4							
-		_							

Proof.			
L.	J,	Ŋ,	
		4	
.54	4	H	
70	. <b></b>	-	

In this example I begin with the pence, faying 8 times 8 is 64, which is 5 shillings and 4 pence; the 4 pence I set down under the pence, and carry the 5 shillings to be added to the product of shillings; faying, 8 times 10 is 80 and 5 is 85, or 4h 5h the 5 shillings I set under the shillings, and carry the 4 pounds to the next product; then 8 times 9 is 7s and 4 is 76.

The work is proved as the former examples, viz. by dividing the multiplier in half, and multiplying by one half, and that product by a.

But in compound multiplication of divers denominations, or when the multiplier is more than 12, the multiplier is to be refolved into its two commensurable parts, if it be a commensurable number, and the multiplicand multiplied by one of those parts, and that product by the other part: thus, if the multiplier be 36, I multiply by 6, and also the product thence arising by 6, which are the two commensurable parts: for 6 times 6 is 36.

But if the multiplier be not a commensurable number, or one which cannot be resolved into parts exactly, then the next lower number which is a commensurable one, is to be taken, and the multiplicand multiplied by the two parts at before, and the multiplicand multiplied by the overplus, and that product, added to the last product: as in the number 40. This number cannot be resolved exactly into two, or three commensurable parts, there being no such number in the multiplication table, wherefore I take the next lower commensurable number 45, because 5 times 9 is 45, and multiply by these two numbers, and the multiplicand by 1, which must be added to the product.

1 2 very. What is the amount of 36 pieces of cloth, at 71. 141. 6d. each piece - Here I multiply by 6, and that product by 6.

Example.	Proof.
£. s. d. 7 14 6	£. s. d. 7 24 6 3
46 7 0	23 3 6
278 2 0	139 1 0
	478 . 0

2 2s. What is the amount of 46 score of sea-coal, \$\mathbb{R}\$
38%, 18s. od. per score?

Example.	Proof.
L. s. d. 38 18 0	£. s. d. 38 18 0
194 10 0	116 14 0
1750 10 0	816 18 0
789 8 0	
	77 16 0 894 14 0
	1789 8 0

In the first of these examples, the work is proved by multiplying by 3, and that product by 6 (which is equal to multiplying by 18, half the original multiplier), and the last product by a, as directed before.

In the second example, I multiply by 5, and that product by 9, which is equal to multiplying by 45, and for the other one I add the multiplicand to the last product. In the proof of this example, I multiply by 3, and that product by 7, which being equal to st, wants s of half the multiplier 46; I therefore multiply the original multiplicand by s, and add the product to the last product; the whole of which I lastly multiply by s.

Example

#### Examples in Avoirdupois Weight.

3 Qu. What is the weight of 107 chefts of tea; each cheft weighing four hundred, three quarters, and twenty-two pounds?

E.	· and	plo.	P	reej	<b>*</b> .
		lb.		grs	
4	3	10	4	3	22
49	1	84 10	84	8	86 10
494	8	16	247		8
		<u></u>	-		3
34	8	14	14	3	10
589	1		a6s	•	18
			524	ı	8
			529	ī	2

In this example roo is the nearest commensurable number, but the multiplier is 107; I therefore multiply by 10 and 10, and the original multiplicand by 7; which last product is added to the other.

In the proof, because 107 is an odd number, I take the half of 106, which is 53; multiplying by 5 and 10, for 50, and the original multiplicand by 3; then I multiply the whole product by 2, which doubles it to 106; and, lastly, add the multiplicand to the product, for the 1 that was wanting.

By these examples it may be seen, that there is no occasion to have always a commensurable number, or to come very mear one; for, if it want ever so much, it may be worked in this manner; always multiplying the original multiplicand by the overplus, and adding such product to the other.

It must be observed, that if the multiplier, in this part of multiplication, consist of more than 144, it must be resolved into three multipliers at least; and if it consist of more than 1728, it must be resolved into more than three.

4 Le. What is the superficial content of a piece of ground, whose breadth is 20274 feet, and length 24640?

Here I multiply the length by the breadth (which is the general rule in superficial measure), and the product is a 53151360 square feet; for the answer.

5 2. How many folid feet does a piece of timber contain, that is forty feet in length, four in breadth, and three in depth?

Here the general rule is, to multiply the length by the breadth, and that product by the depth. And the product is 480 folid feet, for the answer.

length 40 breadth 4 160 depth 9

Multiplication teaches also how to multiply different denominations of measure by different denominations, called sre/s multiplication; of which I shall speak in mensuration.

Multiplication also serves to bring great denominations of money, weights, or measures, into small ones: but this more properly belongs to the rule of reduction.

#### SECT. V.

#### OF DIVISION.

Division teacheth how, from two given numbers, to find a third; that shall be contained in the largest of the two given numbers, as often as the smallest contains units; or the third number contains units, as often as the smallest of the two given numbers is contained in the other. Thus, if 15 were to be divided by 3, the answer would be 52 for 3 is contained in 15, 5 times; and 5 is contained in 15, 3 times.

As multiplication teacheth how to bring great denomina-

tions into small ones; and having the rate or value of one thing, to know the rate or value of many; and from the length and breadth of a superficies, to know its contents, &c.: so, on the contrary, division teacheth how to bring small denominations into great ones; and from the rate or value of many things, and the number of them given, to know the rate or value of one; and from the contents of a superficies, and the length, to find the breadth; or from the superficies, and the breadth, to find the length; and from the contents of a solid, and one dimension thereof, to find the other two.

In every fum in division, there are three parts which are to be particularly remembered, viz.

The Dividend, or number to be divided.

Divitor, or number by which we divide.

Quotient, or answer to the work, which flews how often the divisor is contained in the dividend. I'hus, in the before-mentioned inflance, 15 is the dividend, 3 the divisor, and 5 the quotient.

Besides these three parts, which are in every sum, there is sometimes a remainder, when the work is simished, which will always happen when the dividend does not exactly contain the divisor a certain number of times: as, it I were to divide 13 by 4; here 4 the divisor is contained 3 times in the dividend 13, and there is a remainder of 1; and in division of divers denominations, it must be noted, that the remainder is always of the same denomination with the dividend.

Division is either single, or compound: single division is when the divitor does not consist of more than 12, and the dividend of not more than 144. Any questions of this fort may be answered at once by the multiplication table, without setting them down: thus, if it were required to divide 110 by 10, by that table I know that 10 times 11 is 110; thus 10 is contained 11 times in 110, and 11 is the quotient.

Compound division is when the divisor contains more than 12, or dividend more than 144, or both.

In division the dividend is to have a crooked line placed at

eyphers towards the right hand, and fignificant figures towards the left, such cyphers are omitted in the operation, and placed on the right hand of the product; as follows:—

Example.	7		1	9	7	
7 0 4 9 0 7 8 0 9 3 8 4 5 3 6 0 0 9 5 7 0 1 0 8 6 7 1 0 0 0 0		34	976	9 5	4	
-	Ž.	9	3	8	1 11	

						1	4	00	f.				
	1	ğ	7	6	4	0	o	7	9	0	13	ı	1
-	Ц	4	Ų	L	Ш		Ц	Ц	0	A	0	0	0
1	9	3	8	a	4	9	348	P	9	0	N		٠
31	7	5	2	9	12	4	4	4	0	Ļ	Ц	L	Ļ
4	0	9	٨	2	Š	0	B	9	0	0	0	0	9
41	4	-	ų		Ų	Ļ	4	100	H	Щ	Щ	Ä	ē
9	Ą	0	님	4	ä	B	6	0	0	0	0	0	10
2	2	7	0	Ш	IQ.	Ц	Ó	7.	_	0	0	10	10

In the proof of the last example, the multiplicand is added to the product as before directed, when the original multiplier cannot be divided exactly in half.

# Multiplication of divers Denominations.

Multiplication of divers denominations is performed by multiplying each denomination by the multiplier; beginning with the least denomination, and carrying the units of the next denomination to be added thereto, as is addition of money.

Multiplication of divers denominations is either fingle or compound; fingle, when the multiplier confifts of is or lefs, and is performed by one multiplier; compound, when the multiplier confifts of more than 12, and requires more than one multiplier.

-	cam	
4.	10	d.
9	10	8
76	4	4

I therefore place 6 in the quotient, and multiply the diviker 7 thoreby, and the product 4s I fot under the dividend 48. to be subtracted therefrom and to the remainder 6. I bring down the next figure 7, of the original dividend; thus I have 67 for a new dividend. Then I atk how often 2 is contained in 67, which I find is a times; I therefore put a in the quotient, and multiply the divitor thereby, and the product 64 I place under, and fubtract from, the last dividend; and to the remainder 4 I bring down the next and last figure 6 in the original dividend, which makes 46 for a new dividend. Then I alk how often 7 is contained in 46, which I find is 6 times; I place 6 in the quotient, and multiply the divide thereby: the product 40 1 fubtract from the last dividend 46. and there being no more figures in the original dividend to bring down there is a remainder of 4 after the work is finished, and which remainder is always left than the divitor, if the work be right.

The remainder, may be fet over the divisor as a fraction of an unit; thus in the answer to this question; if 48766, were to be divided equally among 7 men, what would each man's share amount to? Asi, 646, and 4-7ths of a pound.

Division is proved by multiplication: thus the foregoing example is proved by multiplying the quotient by the division, adding thereto the remainder, and if the product be equal to the dividend the work is right; otherwise not.

8) 61#30(760a 8 ••• 8	11)1H747(1703
58 61489 proof.	77 18747 proof. 77
48 48	U# G
0.5	47 48 5

In the first of these two examples, I say, & is contained in \$1,7 times; and 7 times & is 56, which I place under the dividend, and subtracted from it, there rests 5; to which I bring down the 2, which makes 52 for a new dividend. & in 52, 6 times; and 6 times & is 48, which, subtracted from 52, there rests 4, which with the 8 brought down is 48. & in 48, 6 times; and 6 times & is 48, which subtracted from 48, there remains 0; to which I bring down the next, and last figure 0. & in 00 no times, wherefore I set 0 in the last place in the quotient; and thus the work is sinished rightly; as shown by the proof.

The second example is wrought in the same manner, saying 11 in 18 once; and 11 subtracted from 18, leaves 7, which, with the 7 brought down, is 77. 11 in 77, 7 times; and 7 times 11 is 77, which subtracted from 77, rests 0; to which I bring down the a. 11 in a, no times; therefore I place 0 in the quotient; and 0 times 11 is 0, which subtracted from a there rests 2, and 7 brought down is 27. 11 in 27, 2 times, and 2 times 11 is 22, which subtracted from 27, there remains 5 after the work is ended.

From these examples it may be seen, that there must be always one figure, or cypher, brought down at a time, and no more than one; and for every one, so brought down, a figure or cypher must be placed in the quotient.

Though the foregoing method is the regular way of performing division, yet there is a more expeditious method, when the divisor confists of no more than 12, by placing the quotient under the dividend, and performing the subtraction in the mind; as in the following examples: --

8)279083(	11)743002(	12)94736846
3+885	67545	789473
		·
Remains 3	Remains 7	Remains &

In the first of these examples, I say, & is contained in a7, 3 times, and there remains 3; the 3 I place under the 7 in the dividend, and the 3 which remains I imagine to be placed before the 9 in the dividend, which makes 39 for a new dividend. Then 8 in 39 is 4 times, and remains 7; the 4 I place in the quotient, and the 7 placed before the 0 (the next figure in the dividend) gives 70 for a new dividend. Then 8 in 70, 8 times, and remains 6, which, with the next figure 8, make 68. 8 in 68, 8 times, and remains 4, which, with the last figure, gives 43 tor the last dividend. And 8 in 43, 5 times, and there remains 3 at the last.

Proceeding in the fame manner in the next example, I fay, 21 in 74, 6 times and there remains 8. Then 11 in 83, 7 times, and remains 7. 11 in 60, 5 times, and remains 5. 11 in 62, 5 times, and remains 6. 11 in 62, 5 times, and remains 7.

This is the most expeditious manner of dividing by a figure under 18; and is generally done in public offices, shop-books, &c.

But when the divisor consists of more than 12, the work must be performed according to the regular method first laid down, as the divisor is to be multiplied by each autwer placed in the quotient.

375)743801(1981	4240 4349
375	4200
36Ra	4070
1375	1710
3070	3004
1000	3420
701	1541
375	1710
316	111
<b></b>	

In the first of these examples, I mark off by a point the three first figures on the left hand, because there are three figures in the divisor; then I ask how often the two first figures in the divisor are contained in the two first figures of Vol. I.

this pointed off dividend, which I find to be twice; but multiplying the divider by a, the product is 750, which is greater than the first dividend; I therefore place I in the quotient, and place the dividend; I therefore place I will not increase by multiplication), which I subtract from the dividend, and to the remainder I bring down the next figure a, which makes 368s for a new dividend; then repeating the question, I proceed in the same manner throughout the whole.

When the divisor consists of several figures, the most expeditious, and at the same time equally safe, method is, to make a table of the divisor, which may contain the different products of the divisor, multiplied by every number from a to 9 inclusive; as in the following example:

	Table of the Divisor.
#9 <b>8</b> 74398)#43098#4937#(8137	1 89874308
898994464 · · ·	50748016
41097853	3 8964.944
511635457 80644024	4 119497818 5 149371549
980125333 980125333	0 170845848 7 800130156
11005176	Ta Hijija 464
क का को की दिया है।	o soundly

The foregoing table is formed by multiplying the dividor by the fignificant figures from a to 9, or it may be formed by adding each laft product to the first, thus, the second number in the table is formed by doubling the first, the third number is formed by adding the second to the first, the fourth number by adding the third to the first, the fifth by adding the fourth to the first, &c.; and the table may be proved, by multiplying the first number (#9874308) by 9, and if the product be equal to the last number (#0886877%), the table is sight.

The use of this tuble is, to find how often the divisor is contained in any particular dividend; thus, in this example. after having pointed off the first nine figures in the dividend \$13008\$10 (because the first gight figures are less than the divisor), I cast my eye on the table, and find that the next less number is a 18001404, and which I find by the table contains the divisor 8 times; I therefore place 8 in the quotient. and the multiple of 8, taken from the table, I place under the dividend, and subtract it therefrom, and to the remainder bring down the next figure ; for a new dividend; then, by the table. I find the divitor is contained in this dividend but once, I place a in the quotient, and fubtrack the multiple of s (or the divisor) from such dividend as before, and to the remainder I bring down the next figure 24, in this dividend (by the table) I find the divisor is contained a times, which I place in the quotient, and take the multiple of a from the table to be fubtracted from the last dividend, to which remainder I bring down the latt figure a: and, by the table, I find the divisor is contained in the last dividend 7 times; and the multiple of 7 being subtracted from this last dividend. there remains 11005176 after the work is ended.

When the dividend may be divided by the figuriant figures only, and the cyphers feparated from the divitor by a stroke of the pen; in which case there must be as many figures separated from the right hand of the dividend, as there are separated cyphers, and such separated figures are to be set down at the last as a remainder; and if there be any other remainder, the separated figures are to be fet on the right hand thereof. When the divisor has an unit only on the less hand, with nothing but cyphers on the right hand thereof, the division is performed at once, by cutting off as many sigures from the right hand of the dividend as there are cyphers in the divitor: the remainder of the dividend is the quotient. See the following examples:—

Ks ' 18,0)

ss,00)4760,8s(s16	1,00`39	947,34
36 25 140 132	Rem.	94
	53	44 · Rem.  36  53  140  132

## Division of divers Denominations.

Division of divers denominations is performed by dividing each denomination in the dividend by the divisor, placing the quotient of each denomination under the same denomination in the quotient, and carrying the overplus of each denomination to be added to the next, as follows:

Divide 4371. 191. 10d. among \$4 men.

In this example, I first divide the 4371. by \$4, the quotient of which is 181. and there remains \$1. which, added to the 191. makes 1191. for a new dividend; then the divisor is contained 4 times in 119, wherefore I set down 41. in the quotient, and \$31. remains, which added to the 10d. make \$86d. for the next dividend; in which the divisor is contained 11 times, and there remains \$8d. or \$8 farthings, in which the divisor is contained 3 times. Thus the quotient is \$181.41.112d. and there remains 16 farthings.

Sums of this nature may also be more expeditiously wrought, if the divisor he a commensurable number, and can be resolved into two parts, as in the following example:—

Qu. 2. If the expense of a country feast be \$631. to: 64. to be paid by \$8 stewards, what must each steward pay?—In this example I divide by 4, and the quotient thence arising by 7, which is equal to dividing by \$8, and the answer is found to be 91.81. ad. for each steward to pay.

20. a. If a gentleman spend 3471. i.g. 9d. in the space of one year and eight weeks, it is defired to know how much it is per week on an average?—Here I divide the whole sum by 5, and the quotient thence arising by 6, and that quotient by a; which is equal to dividing by 60 (the number of weeks in one year and eight weeks), and the answer is 5l. i.g. i.d. per week, as in the example.

20. 3. If the capital flock of a tentine amount to 43781. 141. od. and there be in it 160 shares, what will be the amount of each share?—In this example I divide by 4, and that quotient by 10, and the quotient thence arising by 4, which is equal to dividing by 160; as 4 times 10 is 40, and 4 times 40 is 160, and the answer is 271. 61. 7d. for each share.

Queflion 1.	Luction 2.	Luckion 3.
£. 1. d.	E. s. d. 5) 147 15 0	L. s. d. 4)4372 14 0
7) 65 17 7 8	6) 69 11 14	1011003 3 6
98 8 5	6) 11 11 10 1	4) 100 6 4 8
	5 15 11	97 () 7

To find the exact remainder in fums where there are two or more divitors, as in the foregoing ones, the rule is to multiply the first divitor by the last remainder, adding thereto the first remainder, if any, and the product will be the true remainder; as if it had been divided by the long method; thus in the first of the foregoing examples, I multiply 4, the first divitor, by 5, the last remainder, which produces so, to which adding a, the first remainder, the true remainder is found to be sa, which may be proved at leiture.

2.4. There is a piece of land, having 4 fides, containing 1398 acres, 3 roods, 35 perches, and a40 feet in breadth, it is defired to know how many feet it is in length?

2.5. There is a piece of timber, the folid contents of which is 600 feet, its length is 40 feet, and its depth 3 feet; it is required to know its superficial contents?

20	fion 4.	
A.	R. P.	Question 5.
4) 1398	3 35	3)600
6) 349	s 38	3 200
10) 58	1 6	•
5	3 18	<u>6</u>

In the fourth question I divide the contents of the land, first by 4, and that quotient by 6, and the next quotient by 10, which is the same as dividing at once by \$40; and the answer is found to be 5 acres, 3 roods, and 12 perches, for the length of the piece of land.

In the last question I divide the solid contents of the piece of timber by 3, the depth, and the quotient 200 feet, is the superficial contents, which if divided again by 40 feet, the length, would give 5 feet for the breadth.

In the same manner as the foregoing examples are wrought division of other denominations may be performed, having respect to the table of quantity belonging to the same.

But in this species of division, if the divisor be not a commensurable number, or one which cannot be divided into parts exactly, the division must then be performed by one divisor.

Division also teacheth how to bring small denominations into great ones; but as this part more properly belongs to reduction, I have deferred treating of it till I come to that rule.

#### SECT. VI.

#### OF REDUCTION.

REDUCTION is only the application of the rules of multiplication and division, and teacheth how to bring numbers of one denomination into another denomination without altering their value.

Reduction is either descending or ascending. Reduction descending is performed by multiplication, and serves to bring great denominations into small ones; as pounds into shillings, pence, or farthings; hundred-weights into pounds or ounces, &c. Reduction ascending is performed by division, and brings small denominations into great ones; as farthings into pence, shillings, or pounds; drams or ounces into pounds, hundred-weights, &c.

Rale. In reduction descending, multiply the number by the number of units of the next lower denomination which make an unit of the next greater, and multiply such product by the number of units of the next lower denomination which make one of the next greater; and proceed in this manner till the number be reduced to the denomination required.

EXAMPLE 1. Reduce 2 col. os. od. into farthings.

In this example, I first multiply the 250 by 20, which is the number of units of the next lower denomination which make an unit of the next higher; that is, the number of shillings contained

	250
Shillings in 1 pound	20
Shillings in 2501. Pence in 1 shilling	5000
Pence in 1 shilling	12
Pence in 2501.	60000
Farthings in 1 penny	4
Answer	240000

in a pound, and the product shews the number of shillings contained in 2501.; which product must be again multiplied by 12, the number of units of the next lower denomination which make one of the next greater, or the number of pence contained in one shilling, and the product gives the number

of pence contained in a 50%; which product, again multiplied by 4, the number of farthings in one penny, the product gives the number of farthings contained in a 50%; or the answer.

Rule. In reduction ascending, divide the given number by the number of units of that denomination which make one of the next greater; and divide that quotient by the number of units of the same denomination which make one unit of the next higher, and proceed in this manner till the whole is finished.

Thus, as in the foregoing example I reduced a 50% into a40000 farthings; so invertely, here I say, in a40000 farthings, how many pounds?

In this example, I first divide the given number of farthings by 4, the number of units of that denomination which are contained in an unit of the next higher denomination; or the number of farthings contained in one penny, and the quotient gives the number of pence contained in \$40000 farthings; which quotient is again divided by 18, the number of pence contained in one shalling, and that quotient gives the number of shillings contained in the given sum of farthings; and lastly, these shillings are again divided by 20, the number of shillings in one pound, and the quotient is \$501 for the answer.

Thus it may be feen, that reduction afcending and defeending prove each other. For if the turn be performed by reduction defeending, it must be proved by reduction afcending, as in the two foregoing examples; and if it be in reduction afcending, it must be proved by reduction defeending.

In reduction defeending, when the functionality of feveral denominations, the number in each denomination, after the first, is to be added to the denomination to which it belongs; as in the following example;

Example

Enample 3. In a 39/. 101. 64. how many pe	nce }—	ln t	hie
example, after having reduced the pounds	<b>3</b> 39	10	6
into faillings by multiplying by so, I add to	10		
the product the 10 shillings which stand in	4780		
the place of shillings; and having reduced	10		
the Chillings into pence by multiplying by 19,	4790		
I add to that product the 6 pence which stand	13		
•	57480		
in the place of pence; and the answer to the	6		
work is thus found to be 57,486 pence.	\$7486		

Exemple 4. In 24 tons, 10 hundreds, and 3 quarters, how many pounds?—This is performed as the 31 10 10 foregoing, but having respect to the table of 480 avoirdupois weight. I therefore multiply 10 the tone by 20 to reduce them to hundred 400 weights, as so hundred is 1 ton, and to the product I add the rocwt. I then multiply by 1000 4 to bring the hundreds into quarters, to which I add the 3 quarters; and, laftly, multiply the quarters by a8, the number of pounds 15704 in a quarter: the product is \$4964 for the 3986 answer. 64004

## Examples in Reduction Afcending.

Example 5. In 24,640,721 minutes, how many days, hours, and minutes?

Example 6. In 47,308 grains of troy weight, how many ounces, pennyweights, and grams?

Example 7. In \$9,474,986 fquare perches of land, how many acres, roods, and perches?

Example 5.	Example 6.	Example 7.
6,0) \$404973,1	a)47308	4,012047208.0
s) 410838,41	14)23600	4) 730824,20
18) 805414	2,0) 197.4 22	184800
17117,10	08 14	- ·-
20 Vo. 1	* Y	ts.

In the first of these examples I divide the minutes by 60, to bring them into hours, by cutting off the o from the 6, and dividingly 6 only, as taught in division, and the quotient is 410828 hours, and there remains 4 minutes, which, placed before the 1 cut off from the dividend, makes 41 minutes for a remainder. This quotient I again divide by 2, and that quotient by 12, which is equal to dividing by 24, the number of hours in 1 day, and the quotient is 17117 days, and there remains 10; but to find the true remainder, I multiply the 10, the last remainder, by 2, the first divisor of the hours, and the product is 20 for the true remainder: thus the answer to the question is, 17117 days, 20 hours, 41 minutes.

In the second example, I divide the grains by a and 1s, to bring them into pennyweights, as 24 grains make 1 pennyweight; the quotient is 1974 pennyweights, and 22 grains remain. The pennyweights I divide by 20, to bring them into ounces, and the quotient is 98 ounces, and 1 pennyweight remains, to which I bring down the 4 I cut off from the dividend, and the last remainder is 14 pennyweights; thus the answer is 98 ounces, 14 pennyweights, and 22 grains.

In the last example, I divide the perches by 40, as 40 perches make a rood, and the quotient is 736824 roods, and 26 perches; the roods I divide by 4, to bring them into acres; and the answer is found to be 184,206 acres, and 26 perches.

Reduction, both afcerding and descending, may be performed by one divisor or multiplier: thus, to being farthings into pounds, the pounds may be divided by 1500, the number of farthings in a pound, and the quotient will give the number of pounds, and the remainder (if any) must be resolved into the inferior denominations. And to reduce hundred-weights into single pounds, they may be multiplied by 1123, the pounds in an hundred-weight, and the product is the answer. But the method before laid down is the more regular, and at the same time the more expeditious way of performing this rule.

Ruamples

## Examples of both Kinds for Practice.

Enample 8. If 400 pieces of cloth contain 8400 ells Flemith, it is required to know how many ells English they contain?

—Ans. 5052 ells English.

Example 9. In 250 puncheons of rum how many hogsheads?—Auf. 503 hogsheads, and 51 gallons remain.

Example 10. A filverimith hath 1000 ounces of filver to be made into spoons, falts, and tankards; each spoon to weigh 2 oz. 12 pwt. each salt 3 d. and each tankard 30 oz. and to make an equal quantity of each, it is desired to know how many he can make of each i—Ans. 58 and 64 pwt. remain.

Example 8.	Example 9.	Est.	ample 10.
\$480 3 5)85860 5058	880 1760 7) 18480 9) 2640 7 293 3	58 3 80 60 30 80 600 719	1000 80 718)20000(28 1484 5700 5696 64

In the first of these examples the 8420 ells Flemish are reduced into quarters of a yard, by multiplying by 3 (as there are 3 quarters in an ell Flemish), and then brought into English ells, by dividing these quarters by 5, the number of quarters in an ell English.

The 9th example is wrought in the same manner: viz. by reducing the 250 puncheons into gallons, by multiplying by 84, and bringing these gallons into hogsheads, and by dividing them by 7 and 9, which is equal to 63, the gallons in a hogshead.

This method of reduction always takes place when the lefs

Yh

denomination

denomination is not contained any certain number of times exactly in the greater.

In the 10th example I reduce the weight of 1 spoon, 1 sak, and 1 tankard, into pennyweights, by multiplying by 20, and then add them together 1 and by the total 712, I divide the 1000 ounces of filter, which is also reduced into pwts. and it quotes 28 of each, and 64 pwts, remain.

By reduction we are enabled to reduce the coin of one country into that of another, without having recourse to the rule of three, or exchange.

Example 11. What is the value, in English coin, of 350 ducate, at 41, 26, per ducat?

Example 19. In \$461, 181, 6st Flornish money, how much English,—the course of exchange being 301, 6st per pound sterling?

Example 13. How much money English is there in 4400 pieces of eight, the course of exchange being at 401st flerling?

	Example 13.	
	30 6 246 18 6	
	19 90	
	366 4938	
Example 11.	2 4930	F .A
350	360) (4262) (461	Example 13
- 60		44:0 44:0
88) 17 6.10	300.	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\
147.84	3306	8122100 34780
dy: 174 13 4	3195	3703 12050
49. <u>A.74 13 4</u>	703	210,33
	300	2763
	330	28/214 43
	30	
	356)0730(18	3,0) 1337.84
	350,0710(13	4 \$1 11V4 VE.
	364.	***************************************
<b>•</b>	3040	
.6	2918	
	134	
	14	
	364)15344	
	1454	
	7.17	
	***	-
	3 )4)45 ~(1	
	398	
	414	Al .6.1 .9 1:
· '		we ser straff

In the 1sth example, I multiply the 350 ducats by 50, to bring them into pence, and then divide by 12, and it quotes 1458 shillings and 4 pence: I then divide the shillings by 50, and the quotient is 721. 181. 4d. for the answer.

In the 1sth example the 2461. 181. 6d. Flemish money is reduced into pence, and then divided by 366, the course of exchange; and the answer is 1611. 181. 4\frac{1}{2}d. and 114 farthings remain.

The 13th example is wrought in the same manner as the 11th: viz. by reducing the pieces of eight into pence; and for the fraction; of a penny, I multiply the given number of pieces of eight by 5, the numerator, or upper figure of the fraction, and divide the product by 8, the denominator, or lower figure of the fraction, and to the quotient I add the pence contained in the pieces of eight, and then reduce this whole into shillings and pounds, by dividing by 12 and 20, as before, and the answer is 9131. 181. 4d.

This method of reducing foreign coin into English may serve for those who are unacquainted with the rule of practice; for practice performs this much more expeditiously, as will be shown in its proper place.

Those sums in reduction, in which both division and multiplication are used, must be proved by multiplication and division; as, for example, that part which is performed by multiplication must be proved by division, and that part performed by division must be proved by multiplication.

The foregoing examples, perfectly understood, will be fufficient to give the learner a complete knowledge of this rule, and the various uses to which it may be applied.

It is absolutely necessary that the learner beperfectly acquainted with what has been delivered in the foregoing part of this chapter, as all the following rules in arithmetic are performed by one or more of the foregoing rules; I have therefore been more explicit in the former part; being the basis of the whole.

SECT.

#### SECT. VII.

# THE GOLDEN RULE OR, SINGLE RULE OF THREE DIRECT.

Thus rule, which, for its universal use in most parts of the mathematics, is called the golden rule, is also called a rule of properties, because the number sought bears a certain propertion to one of the numbers given.

It is called the rule of three, because it consists of three given numbers, from which a fourth number is to be found, which, in the direct rule, bears the same proportion to the second number as the third does to the first.

Rule. Multiply the second and third numbers together, and divide the product by the first number, and the quotient is the answer sought, or the south number.

Here the fourth number or aniwer, 36, bears the fame proportion to the fecond number 12, as 9 the third number, burge to the first-number 3, that is, it contains it three times; or it bears the same proportion to the third number 9 as the second number 12 does to the first number 3, viz. contains it four times. This proportion is called direct proportion; from whence this rule is called the rule of these direct, and is always performed as above.

But when the fourth number bears the same proportion to

the fecond as the first does to the third, it is then called indirect proportion. Questions of this nature belong to the next rule, called the rule of three inverte, of which hereafter.

In order to know which is the fecond and third number, it must be noted, that of the three numbers which are in every question in this rule, that number which asks the question must occupy the third place, and is called the third number: and that number which is of the fame nature with the fourth number or answer, must be the second number, and consequently the other number must be the first. The second and fourth numbers are therefore always of the fame nature; as are the first and third. Thus, in the foregoing example, the number o asks the question, for the question is, how much will g yards cost? g is therefore the third number. the same nature with the fourth number, being money; it must therefore possess the second place; and a the other number, must be the first, which is of the same nature with the third, viz. yards.

When either the first or third numbers consist of different denominations, they must both be reduced to the same denomination; and when the fecond number confitts of divers denominations, it must also be reduced to the lowest:this reduction must be performed before the work can be wrought; and it must be observed, that the fourth number, or answer to the work, is always of the same denomination with the fecond number to reduced.

The numbers being fo reduced, the tecond and third numbers are to be multiplied together, and the product divided by the first, as before directed; and the fourth number or answer must be brought into the proper denominations required reduction, and if any thing remain after the products of the fecond and third numbers are divided by the first, such remainder must be reduced into the next lower denomination, and then divided by the first number, as before; and if any thing full remain, it must be reduced into the next lower denomination (if there be any lower), and divided by the first number: aumber; proceed in this manner till the remainder be brought to the lowest denomination.

Example s. If 1s gallons of brandy cost 4/. 10r. what will 1so gallons cost at that rate?

In this example (the numbers being placed as before directed; the second confishing of two denominations, viz. pounds and shillings, it must be reduced to the lowest denomination (shillings), and the product is 90 shillings: the question will then be, if 12 gallons cost 90s, what will 120 cost? I therefore multiply 120 the third number, by 90 the second number, and divide the product by 12 the first number, and the quotient 900 is the fourth number, or answer to the question, which, because the second number is reduced to shillings, is shillings also, and is divided by 20 to bring them into pounds, and the quotient is 45 pounds, the true answer, or price of 120 gallons at that rate.

## The Proof.

There are feveral methods of proving questions in the rule of three, but the truest and most improving to the learner is, to back state the question: thus, to prove the last example, I state the question backwards, making that number which was the fourth number in the question the first number in the proof, and that which was the third number here I make the second, and the second I make the third.

Proof. If 451. purchates 120 gallons, what will 41. 101.

purchate? 20 900 108,00

There

1

In the proof of this example, I reduce the first number 45% into faillings, because the third number 41. 101. must be reduced into shillings, confishing of pounds and shillings; and then multiplying the second and third numbers together, and dividing by the first, the answer is 12 gallons, as in the example; it therefore proves the work right.

Example 3. If the income of a person be 3 farthings a minute, how much is it per annum?

2d number.

Say, if 1 min. produce 3 farthings, what will 365 days 6 hours produce?

24
1466
730
8766 hours
60
585960 minutes
4)1577880 farthings
18) 394470 pence
8,0) 3887,2—6

Aufwer 16431. 181. 6d.

2d number.
3d numb

More the 365 days 6 hours are reduced into minutes by multiplying first by 24 and then by 60, the product is then multiplied by 3, the second number, and the last product is the answer in farthings, which is brought into pounds and shillings by division, and the answer is 16431. 185. 6d.

In the foregoing example the first number is an unit; when this is the case, the work is performed by multiplication, and when the third number is an unit, the work is wrought by division, for a neither multiplies nor divides; questions of this fort, therefore, properly belong to reduction.

Example 4. If the effects of a bankrupt amount to \$7961. 101. and his debts be 99901. 121. it is requested to know how much he can pay in the pound?

Vol. I. Z Say,

the pound.

Say, if 9990/. 184. pay sos. in the po	ound, what will 27961. 10s
pay ?	<b>50</b>
199818	55930
	20
In stating this question, I	199812)111600(5
fay, if 9990/. 121. the whole	999060
	119540
amount of the bankrupt's	13
debts, will pay 20s. in the	199818)1414480(7
pound, as it certainly will, what	1398684
will 2756/. tos. the net value of	35796
the bankrupt's property, pay?	3374
	143184
-And the answer is 51.7d. in	141104

In performing this example, the first and third numbers are reduced into shillings, and multiplying the second and third numbers together, and dividing by the first, the quotient is 5, which is of the same denomination with the second number, viz. shillings; and there is a remainder of 110,540 shillings, which is reduced into pence, and then divided by the sustence as before, and it quotes 7 pence, and there yet remains 35790 pence, which, reduced into farthings, does not contain the divisor once; these pence, therefore, remain over and above the 5s. and 7s. in the pound which the bankrupt gays.

The foregoing examples will be found sufficient to instruct the learner in the nature and method of working this rule; I shall therefore give a few examples for practice, leaving the operation to be performed by the learner.

Example 5. If 56th, of indigo cost 111.41. what will 1008th, cost at that rate?

Say, if 5618. cost 224s, what will 100818.cost?—Aufwer
4032s. or 2011. 12s.

Example 6. If a debtor owes his creditors 593l. 12s. and compounds at 7s. 6d in the pound, what will pay his creditors at that rate?

Say, if sos. can be paid by god, what will pay 12878s. ? -Anfever 2221. 125.

Example 7. If 1001. gain 61. interest in 12 months, how much will 340% gain in the fame time at that rate of interes? If 2001, gain 61, what will 3401, gain ?- Answer 201, 81.

Example 8. A draper bought 6 packs of cloth, each pack containing 12 pieces, for which he paid 10801. being 81.44. per ell Flemish: how many yards were there in each piece?

If 100d, purchases 2grs, what will \$10200d, purchase '-Answer 7776grs. which divided by 72, the number of pieces in the whole, it quotes 102grs, or 27 yards in each piece.

The general use of this rule is, from having the rate, value, proportion, produce, interest, gain or loss of one or any other number of things, to find the rate, value, proportion, produce, interest, gain or loss of one or any other number of the fame things in a direct proportion.

#### SECT. VIII.

#### OF THE SINGLE RULE OF THREE INVERSE.

THE rule of three inverse is that which teaches how from three given numbers to find a fourth, which shall bear the fame rate or proportion to the fecond number as the first does to the third; or the third number bears the same proportion to the second as the first does to the fourth.

Rule. Multiply the first and second numbers together, and divide the product by the third.

The method of placing the numbers in this rule is the fame as that of the rule of three direct, and therefore need not be repeated.

, In order to discover whether a question belong to the direct or inverse rule, it must be remembered, that the first and third numbers are called the extremes; if, therefore, the fourth number be greater than the second, the less extreme must be the divisor; but if it be less, the greater extreme must be the divisor.

And when the first number is the divisor, the work belongs to the rule of three direct; but when the third number is the divisor, it belongs to the rule of three inverse; as in the following examples.

Example 1. If 8 men perform any certain piece of work in 6 days, how many men will perform the same work in 3 days?

If 6 days require 8 men, what will 3 days require?

In this example I confider, that if to do the work in 6 days it requires the labour of 8 men, then, to do the fame work in 3 days, it will require more men, confequently the fourth number will be greater than the second, therefore I divide the product of the first and second numbers multiplied together by the third number (the least extreme), and the quotient is 16 (men) for the answer.

The proof of questions in this rule, as well as the foregoing rule, is performed by back stating the question; but it must be observed, in all questions in the direct rule, the proof is wrought by the rule of three direct; and in questions of the inverse rule the proof is wrought by the rule of three inverse.

Thus, to prove the foregoing example, I say, if 16 men require 3 days to perform the work, how many days will 8 men require to perform it?

If 16 men require 3 days, what will 8 men require?

Example 2. If a loaf at a certain price weight 45 b. when wheat is 61. per bushel, what should it weigh when wheat is 41. 6d. per bushel?

If

pow

If 7nd. per bushel give 9 half lbs. what will 54d. give?

101

Ans. 12 half lbs. or 61b.

In this example, I multiply 72 pence, the price of the bushel of wheat, by 9, the number of the half pounds in the loaf, and dividing by 54 pence, the price of the bushel of wheat at the other price, the answer is 12 half pounds or 6 pounds for the weight of the loaf at that price of the wheat.

In London the price of the loaf is varied, and the weight continues the fame. Questions which concern the price are wrought by making the price the second number.

Example 3. If a board be 8 inches broad, how much in length will make a square foot?

If 12 in. in breadth require 12 in. in length, what will 8 in. in breadth require?

8) <u>144</u>(18 Anf. 18.

Example 4. How many yards of shalloon at 3qrs. wide are sufficient to line throughout the garments made with 1000 yards of cloth at 7qrs. wide?

If 7qrs. wide require 1000yds. what will 3qrs. wide require?

20. 5. If 150l be lent for 9 months, how long should sol be lent to gain the same interest at the same rate?—

Answer 15 months.

20.6. If a colonel be befieged in a town with 1000 men, having practitions for only 2 months, how many must be dismiss, that the provision may serve the remainder 5 months?

—Assure (12), and retain 400.

La. 7. If a person person a journey (travelling at an unisorm rate) in s4 days, by travelling as hours per day,

how long will it take to perform the same journey by travelling 16 hours per day at the same rate?—Ass. 18 days.

20.8. If a carrier carry 18 cwt. 72 miles for 51. how many miles will he carry 18 cwt. for the same money?—

After 48 miles.

This rule ferves to find a fourth number to the given three, in an inverted proportion. And it particularly answers feven forts of questions: viz. 1. Having the value of two different forts of coin, it thews how many pieces of the one are equal in value to a given number of the other. two different values of one commodity, and the value of an article made from the fame commodity at one value thereufto find the weight, measure, &c. of the same article; or, on the contrary, from the values of the commodity and the weight, measure, &c. of the article, to find the value thereof (the ad example is of this nature). 3. From the breadths of two equal rechangular figures, and the length of one of them, to find the length of the other; or, from the two lengths and one breadth, to find the other breadth (of this nature are the third and fourth examples). 4. From the given weight, expense of carriage, and number of miles carriage of any goods, to find the number of miles any other weight could be carried for the fame price; from a given weight and price, and two diffances, to find the weight anfacrable to the other diffance (of the nature is the eighth quellion). c. From two fums of money lent, and the time for which one of them is lent, to find the time for which the other should be lent; or, from the two different times, and the fum which is lent for one of them, to find the fum which should be lent for the other time (of this nature is the fifth example). 6. From the quantity of work which a given number of men can perform in a given time, to find the number of men that can perform it in any other given time; or, from the number of men, to find the time any other given number would require (of this nature # the first example). 7. From the quantity of provisions, or money, and the number of men, or other creatures, it would serve a scentain time, to find the number of men, or other creatures, it would serve any other time; or, from the quantity of provision and the number of consumers, to find the time it would serve any other number of consumers (of this nature is the sixth example).

#### SECT. IX.

#### OF THE DOUBLE RULE OF THREE DIRECT .

In this rule there are five given numbers to find a fixth, which shall bear the same proportion to the product of the fourth and fifth numbers, as the third number bears to the product of the first and second.

Questions in this rule are resolved either by two operations in the single rule of three direct, or the rule of three composed of five given numbers.

Each quettion in this rule confilts of two parts, the Suppofition and the demand.

Rule 1. By two operations. Place that number which is of the same nature with the fixth number, or answer, in the second place in the sirst operation; and the two other numbers in the supposition in the first place, the one over the other; and the two numbers in the demand in the third place, one over the other, in like manner as the two in the sirst place; observing that the bottom numbers in the first and third places be of like nature, as will also the top ones.

Some modern writers compound the two double rules of three late one; I have, however, given them diffinelly, being more conforant to the true theory of ference. In the next Section is, nevertheless, thewa an intallible method of working both by one rule.

The work is then performed by two operations in the fingle sule of three direct; the answer to the first operation forming the second number in the second operation.

s. By one operation. Multiply the two mumbers which frand one over the other in the supposition, together, for the first number: the two numbers in the demand for the third number; and the second number in the first question will be also the second number in the work. Then the answer is found by one operation in the fingle rule of three direct, as in the following example:

Example 1. If 1001. principal gain (1. interest in 1 year, what will 140L gain in 9 months?

The Queflion Rated.

If 1001. gain 41.

What will 140%.

in 12 months.

gain in a months? In this example, the numbers 100, 5, and 18 belong to the supposition, and 140 and 0 is the demand; for the

meaning of the work is, suppese 1001. gain 51. interest in se months, (then follows the demand) I demand to know how much 140L will gain in 9 months at the same rate of intereft ?

Thus the questions are stated according to the foregoing directions: the 5/. being the interest of the money (and of the same nature with the fixth number or answer) must be the second number; and the two other numbers in the supposition 100 and 12 are placed one above the other, as are the two numbers 140 and o in the demand. It matters not which of these two numbers is uppermost, provided that the numbers in each, which are of the same nature, occupy the corresponding places respectively: thus, in the supposition, the pounds principal is the uppermost number, so it is in the demand, and the number of months is undermost in both.

The question being thus stated, the work is wrought by two operations of the fingle rule of three direct. The three uppermost numbers are the numbers for the sast operation, and the fourth number, or answer to these forms, the second number number for the second operation; the bottom number of the supposition forms the first number, and the bottom number of the demand the third number; then the answer, or fourth number of this second operation, is the true answer to the question; as in the following example, which is the foregoing one at large.

First Operation.

If 1001. gain c/. what will 1401.

Second Operation.

If is months gain 7/, what will 9 months?

18)63(5 60 3 80 18)69(5

Answer 51. 51.

The answer would have been the same if the number of inouth's said been the uppermost numbers instead of the pounds principal; in which case the first question would be, if 12 months give 3/, interest, what will 9 months give 2 and the answer is 3/, 155.; then the second question would be, if 100/, gain 3/, 155. what will 140/, gain 2 and the answer is as before, 5/, 5r.

Ry one Operation.

Vol. I.

Aа

In

In this example, the work is stated as in the former; the two first numbers in the supposition are multiplied together, and the two numbers in the demand are also multiplied together, then these two products are made, the one the first, and the other the third number, and the second number in the first question is also the second number. This rule is the most sure and practical method of proving the double rule of three direct, when wrought by two single ones.

The foregoing example worked both ways will be sufficient to instruct the learner. I shall, therefore, give a few questions, with their answers, omitting the operation.

- Qu. 2. Suppose 468 men consume 175 quarters of wheat in 168 days, I demand how many quarters will serve 5612 men 58 days?—Ans. 724 quarters, and 1834 of a quarter, or a little more than half a quarter.
- 29.3. Suppose 80 acres of grass be moved by 8 men in 14 days, I demand how many acres 28 men will mow in 12 days?—Ans. 240 acres.
- Ly. 4. Suppose the wages of 12 men for 6 days amount to 71.41. what are the wages of 25 men for 40 days?—Anf-1001.
- Qu. 5. If 1501, principal put out to interest for 9 months be increased, principal and interest, to 1561, 151. I demand how much is that per cent. per annum?—Ans. 91.

#### SECT. X.

## OF THE DOUBLE RULE OF THREE INVERSE.

THE double rule of three inverse is when there are five given numbers to find a fixth, in an inverted proportion.

Rule. Place the numbers as directed in the last section. Multiply the lower number of the first place by the upper one of the third, and make the product the first number; next multiply the upper term of the first place by the lower one of the third, for the third number: then if the inverse proportion be found in the three upper numbers, the answer is given by one operation in the rule of three direct; but if the inverse proportion be found in the lower numbers, the work is performed by the inverse rule (for of every sum in this rule one question is direct and the other inverse).

Example 1. If 1001. gain 51. interest in 12 months, what principal will gain 51. 51. in 9 months?

The pounds interest being reduced to shillings, and multiplied by the number of months, the question will stand, and operation be performed as follows:

If the number of months had been made the upper terms, the upper proportion would then have been direct, and would have been required to have been worked by the direct method. It would in that case stand thus:

<sup>\*</sup> The rule laid down in this fection will be found quite general, and fufficient for working all questions in the double rule of three both direct and investe; and is so obvious, as to require no demonstration. Nevertheless, in consequence of receiving advice from some teachers (not the most competent) of the mathematics, that I had not given the improved method of working this rule, I shall state this much-approved rule, verbatin, from a well known treatife, and show its fallar.

Ly. s. If 481. ferve for the maintenance of 12 min 8 days, how long will 2881. ferve for 4 men?—Anf.: 144 days.

Ly. 3. If, when a bushel of wheat costs 61.8d. a ponny louf weighs 6 ounces, how much will a louf weigh that costs 10 dd. when the wheat is 102. the bushel?—Anj. 42 ounces.

"5. If the blank falls under the first or feword term, multiply the third and fourth terms for a divisor, and the other three for the dividend; and the quotient will be the answer.

" Proof. By two fingle rules of three.

"Reample 1. If 14 hories out 56 buffels of ours in 16 days, how many buffels will be fufficient for 20 hories for 24 days?

By two fingle rules;
bor. bu. hor. bu.

1. As 14: 56::20:80
da. bu. da. bu.

2. As 16:80::24:120

Or, in one flating, worked thus:

hor. da. bu. 14:16:56 56×20×24 20:24:— 14×16

WALKITSAME.

That this rule is not founded on mathematical principles is evident from infortion; for by a different flatement of the question though exactly agreeable to the rules, a different answer will arise. Thus, how easily might the learner, required to work this question by one sharement, order the numbers as follows:

According to this flatement the answer will be  $58\frac{4}{3}$  bushele; whereas the true answer to  $s_{20}$  bushele. The question is, nevertheless, flated n this last cute agreeable to the raise.

<sup>&</sup>quot;Rele 1. Let the principal cause of loss or gain, interest or decrease, action or pussion, be put in the first place.

<sup>&</sup>quot;a. Let that which betokeneth time, diffunce, or place, and the lifte, be in the fecond place; and the remaining one in the third.

<sup>&</sup>quot; 3. Place the other two terms under their like in the lappolition-

<sup>4.</sup> If the Mank falls under the third term, multiply the first and fecond terms for a divisor, and the other three for a divident; but,

- 23.4. If 96 pioneers in s4 days caft a trench 90 yards long, how many pioneers will caft a arench 336 yards long in 8 days?—Asf. :008 pioneers.
- La. 5. If so men mow 40 acres in 8 days, how many days will it require 3 men to mow 150 acres?—Ash soo days.

This rule may be proved by two fingle rules.

The following rules in this chapter, except vulger fractions and the extractions of ruots, are wrought either by fome of the rules of proportion, delivered in the four preceding fections, or by the rule of practice, hereafter so be spoken of.

#### SECT. XI.

#### OF FELLOWSHIP.

Fallowship is that rule whereby merchants and others, anding in company, and employing a joint capital flock, are enabled to afcertain each partner's particular lots or gain, according to his there in the tame joint flock.

This rule alto ferves to divide a bankrupt's effice among his creditors; to pay legacies, when there is a deficiency of the testator's effects: and, in fine, to divide the loss or profit of any joint concern among the laters or proprietors.

The rule of fellowthip is either fingle or double, that is, without regard to time, or with time.

Fellowship combout time, or tingle fellowthip, is when different persons employ their respective stocks for the same time.

As the whole stock of all the partners is to the whole gain or loss, so is each man's particular stock to his particular share of the gain or loss.

By adding each person's gain or loss together.

Therefore, the whole stock of all the partners is to be made the first number in the rule of three, the whole gain or loss the second number, and the particular stock of any one partner the third number; then the fourth number, or answer, is that partner's loss or gain, whose stock was the third number. This operation in the rule of three must be repeated if there be more than two partners, and performed as often as there are partners concerned.

Example 1. Three persons enter into trade together: A put into the trade 1001. B 1701. and C 2001.; at the making up their accompts, they find they have gained <<01. profit; what is each person's share?

> A's stock £.100 B's Bock

170

C's Bock 300 Whole stock & Whole Stock. Whole Gains A' i Sieck. 57%. 5501. 100/. 57,0)5500,0(46 100 513 370 342 280 20 57,0)567,0(91. 513 470 12 57/1)564,0(9d. 513 510 57,0)204,0(3 fur.

171

```
B's Stock.
           5706
                              550%
                                                   270/.
                              170
                            38,000
                     57,0)9350,0(164 0 84 390
                          57
365
                             20
                      57,0) 40. (Oc.
                             12
72 .
                     57,0)480,0(84.
                          456
                          140
                            4
                     57,0)90,0(1 /0.
                          57
390
                                           C's Stock.
       5704
                          550%
                                               300/.
                  57,0)10500,0(189 9 51 472
                       114
                        510
                        456
                         540
                         513
                         370
                          20
                   57,0)540,0(94
                        513
                         173
                         14
                  57,0)324,0(54
                       285
                        390
```

\$7,0)150,0(2 for. 114 420

## The Proof.

A's fhare B's fhare C's fhare	164			112
Whole Abck	6.550	۵	•	

If there be any remainders, fisch remainders in the proof must be added together (if they be fractions of the same denomination), and divided by the common divisor of each question (i. e. the total stock), and the quotient, which is units of the same denomination, added to the particular shapes thus, in the foregoing example, I added the three remainders, 330, 390, and 420, together, and dividing the total by 570, the common divisor, the quotient is a, which are farthings, as they are fractions of a farthing.

- 2n. 2. Four persons place their money in the public funds: A put in 360l. B 480l. C 700l. and D 860l. When the capital came to be fold out, the principal and interest amounted to 4200l. what is each man's share of the net profit?—Anfrown, A 270l. B 360l. C 525l. D 645l.
- 20.3. A bankinpt is indebted to four creditors in the following furner to A 55th St. to B 608h 14s. to C 304h and to D 208h 12s. The bankrupt's effate is worth only 337h 17s. how much will each creditor receive?—Anf. A 11th 7s. 5s. B 122h 18s. 10\frac{1}{2}sh. C 6th 8s. \frac{1}{4}d. and D 42h 2s. 7\frac{3}{4}d.
- 24. 4. A flup being lost value 1730/.; of which A paid 346. B 519/. C 692/. and D 174/. towards building her; the was infured to the amount of 1300/. What was each person's loss?—Anform, A 74/. B 111/. C 148/. D 37/.

In the fecond example, the whole stock first placed in the funds is to be found by adding each person's stock together, and that made the first number in the rule of three; the whole gain is to be the second number, the particular stock of any one person the third number, and the south number is his share.

In the third example, the whole amount of the bankrupt's debts is to be made the first sumber; the value of his effects the second number; and any creditor's real due the third number, and the fourth number is that creditor's share.

Fellowship with time, or double fellowship, is when the disferent stocks are employed for different times.

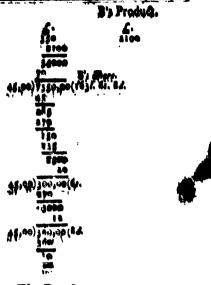
Rule. Multiply each man's particular stock by the time it is employed for; then say, by the rule of three, as the total of all these products is to the whole gain or loss, so is each man's particular product to his particular share of the total or loss.

thus the rule of three must be repeated as often as there are products or persons concerned, as in the fingle rule.

Exemple t. A put sool in a certain trade; B five months after put 300l.; at the end of one year they find they have sained 350l. profit, what is each person's share?

		٧.			
	Total	Whole	3	A'0	
	Product.		. 4	Produ <b>a.</b>	
	٠ ٤٠	£:	•	£.	
	4500	350		1400	
100		2400			
12 months.		140000			
3400 A's product	<b>.</b>	70	A's Share		
		45,00)8400,00			
300		45		•	•
• •				••	
2100 B's product	<u>.</u>	390			_
· ·		360		•	4
4500 Total of the	e producu.	300			4
		270			
		3000			- 7
•		10			Ł
. •		45,00)600,00	124.		
			(434.		
•		45			Ŧ
		150			
		. 135	•		٦
		1400			1
		18			-
		AE.00) 180.00	(ad. `		17
		45,00) 180,00	•		.6
• •	•				_
		÷	ang marija		. 4.3
1197 7					B.
Vor. L		ВР			

٠.



The Proof.
A'n there (186 19 4
B's fines 163 6 8

The method of proof in this rule is the same as in the fingle rule, as may be then above.

Le. a. A. H. and C rent a passure in common, at 406 per annum; A puts in it 3 oxen for it months in the year, B puts in 7 for 4 months, and C puts in a for the whole year; what must each person pay towards the rent? Assure, A sale 121, 746, 94; B 146, 144, ite. 94; C 126, 121, 746, 94.

Remple 3. A, B, and C make a flock for 12 months, A put in at first yast. at the end of a months he put in act. more; B put in at first 2001, and at the end of 5 months he took our 1504; C put in at first 401, and at the end of 6 months 501, more; and at the end of 10 months 501, more; at the year's end they find they have gained 5001; what is each person's profit?

In these examples, and all others of the like nature, where the different parts of the stock of each person are employed for a different time, the different parts of each person's stock are to be multiplied by their own separate times, and these products added together to make up the product of each person; and then each person's product added together to make the total product.

•	
Thus, in the last example, I first multiply the 728%.  put in by A, by s, the number of months it is  disployed alone, and the product is  Then A put in sol. more, which, added to the 728%.	L. 1456
is 748% and which multiplied by 10 months, the	0 -
product is	7480
And which two added together give A's product	8936
B put in sook for 5 months, which product is -	1000
At the end of granouths he took out 1 got, and then	4000
•	
there remained only 50% which multiplied by 7	
months, the product is	350
The two products of B added together are his true on	<b>e</b> 1350
C put in at first 40%. which continued alone 6 months,	
that product therefore is — —	9.40
<del>-</del>	-4-
At the end of 6 months he put in 50%, more, which,	
added to the former 401. is 901. which multiplied	•
by 4 months, gives —	360
The last a months he had root, in the stock, which,	
multiplied by a months, gives -	800
Therefore the product of C is -	800
•	- de
The total sum of all the products	11086

Then the work is wrought as before, faying, as 11086 (the fum of the products) is to 5001. (the total gain) so is 89361. (the product of A) to 4031. 05. 7411. 11053, the share of A of the profits; and repeat the operation twice more, to find the shares of B and C.

Anfwer.

## Answer.

The share of A B C	60	17	7‡ 9	₹₹₽ <b>₹</b> ₹₹₽ <b>₹</b> ₹₽₽ <b>₹</b>
	500	0	0	

#### SECT. XII.

### of alligation, medial and alternate.

THE rule of alligation teacheth how to mix different subflances together, and to discover the value of any part of such mixture; or to make a mixture from known substances of any value.

Alligation is either medial or alternate.

Alligation medial is that which teacheth how to find the rate or price of any mixture or compound, from having the rates or prices, and the quantities of the several substances given.

Rule. Multiply each quantity by its rate or price, and add the products together for a dividend; add the fums of the feveral quantities together for a divifor; and divide the fum of the products by the fum of the quantities, and the quotient will be the rate or price of the compound.

Example 1. A mealman mixes so bushels of flour, worth gr. per bushel, with 12 bushels worth 31.4d. per bushels what is one bushel of this mixture worth?

Price

	Price of a buffel 404.	Quantities
No. of buildels 20	No. of bulbels 12	11
1100	480	30
	1800	34
	32)1680(52	d. or 41.45d. per ballel,
	160	for the Anfwer.
	80	
	64	
	6 <u>4</u> 16	
	4 far	things
•	32) 64 (2	
	64	
well.	ō	
**	4 far. 32) 64 (2 64	things

In this example the price of the bushel is reduced into pence (as it mostly should). The answer is the price of the quantity, which is of the same denomination with the divisor, which here is bushels.

Proof. Find the value of the whole mixture from the value of any part, and if it be equal to the value of the original simples the work is right.

Thus, to prove the foregoing example, I multiply the price of one bulked of the mixture by 4 and 8, or 32, the number of bulkels in the whole, and the product, I find, is 21.; then I find the value of the several simples, by multiplying the number of bulkels in each by the number of penos in a bulkel (which is already done in the example), and the product 1680 brought into pounds, gives 71. as follows:

## The Proof.

i ilie 1700j.			
The Number of Buthels multiplied by the Pense in a Buthel.	The Price of a Bufnel of the Mixture multiplied by the Number of Buthels.		
12) 1680 pence 8,0) 14,0 fhillings 7 pounds	s. d. 4 4\frac{1}{2}		
Ains.	£ 7		

- Qu. s. A grocer mixed the following teas together, viz. s fibe. at 8s. per lb. solbs. at 7s. 4sl. per lb. solbs. at 6s. 8sl. per lb. and s 4!bs. at 4s. per lb. what is one pound of this mixture worth ?—Anfavor 6s. s \( \frac{3}{2} \) !. \( \frac{3}{6} \)
- 28.3. A vintner mixes 5 gallons of wine at 71. per gallon, with 9 gallons at 81.6d. per gallon, and 14½ gallons at 51. tod. per gallon; what is one gallon of this mixture worth?—daylour 61. to½d. {4
- 20.4. A goldfmith melts 101 ounces of gold bullion, of 14 carate fine, with 150 ounces of 18 carate fine, boss many carate fine is this mixture?—Assure 1618 carate fine.

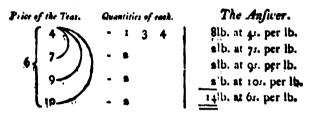
Alligation alternate is the method of finding what quantity of fimples, whose rates or prices are given, will form a mixture of a certain given rate or price.

Rule 1. Write the rates or prices of the feveral simples under each other. a. Connect with a curve line the rate or price of each simple that is less than the rate or price of the mixture, with one or more of these rates or prices that are greater than that of the mixture; and each greater rate with one or more that are less; and place the rate or price of the mixture on the less hand of the rates or prices. 3. Write the difference between the rate of the mixtures and the rate of each simple opposite the rate with which such simple is connected or linked.

Then these differences which stand opposite any rate is the quantity which that rate requires to form a mixture of the given rate; but if there is more than one difference opposite any simple, their sum is the true difference.

Gold is generally mixed with copper or fome other baff metal, which is called the allay; and the gold is fald to be fo many carats fine, as it contains pure gold; thus, if an article weight a4 carats, and contains as estats of gold, and a of allay, it is faid to be as carats time. What a carat is may be teen, page 135.

Example 1. A grocer would mix test at 41. per lb. 71. per lb. 91. per lb. and 101. per lb. in such proportion that the mixture may be worth 61. per lb.; what quentity of each must be taken?



In this example, I first state the work as before directed, placing the prices of the teas in a column over each other, with 6, the given price of the mixture, on the less hand.

Secondly, I connect the prices with each other by curve lines; 4 the top figure, being less than the rate of the mixture, I connect with 7, 9, and 10, because they are all greater than 6, the rate of the mixture.

Thirdly, I find the difference between 6, the price of the mixture, and 4, that of the first simple, which is s; I therefore place s opposite the 7, 9, and 10, as the 4 is linked to all of them. Then I find the difference between the 6 and the next figure 7, which is 1, I therefore place 1 opposite the 4, being the figure to which the 7 is linked. Then the difference between the 6 and 9 is 3, which I place also opposite the 4 (the 9 being linked thereto), and the difference between 6 and 10, which is 4, I also place opposite the 4 (as the 10 is also linked to it). These differences, so placed, contain the true proportion of each fort of tea at the price opposite to each, that should be taken to form a mixture at the defired rate.

But opposite the 4 there are three differences, viz. 1, 3, and 4, which are to be added together, as seen in the less column. Thus, there must be 81b. of teq at 41, per 1b. alb. at 75, per 1b. alb. at 95, per 1b. and alb. at 105, per 1b.; and the whole quantity of the mixture is 141b. at 65, per 1b.

These questions are proved in the same manner as those in alligation medial, viz. by finding the total value of all the samples in their separate state, and the total value of the mixture; and if these two values be equal, the work is right.

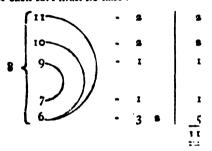
# The Proof of the foregoing Example.

81b. of tea, at 4s. per lb. is	1 18	•	ture at 6s, per lb.
3º Shillings			84 Millings, or
slb. at 71. per lb. is	0 14	0	4l. 4s.
14 Shiffings			
alb. at 91. per lb. is	0 18	•	
28 Shillings			
alb. at ros. per lb. is	1 0	•	
Shillings Total	4 4	<del>°</del>	

- La. a. A farmer mixed wheat at 4s. the bulbel, with rye at 3s. the bulbel, and barley at 18d. the bulbel, how much must be mix of each to sell the whole mixture at 22d. the bulbel?—Anform, 40 bulbels at 18d. per bulbel, 4 bulbels at 3s. per bulbel, and 4 bulbels at 4s. per bulbel.
- 2n. 3. A goldimith has gold to melt of \$4 carats fine, \$1 carats fine, 19 carats fine, and 16 carats fine, how much of each must be take to form an article of gold that shall make 17 carats fine?—Anfwer, 1 of \$4, 1 of \$1, 1 of \$5, and 13 of 16 carats fine.

When the whole mixture is limited to a certain quantity, after finding the quantity of each of the fimples as before, fay (by the rule of three), as the furn of the quantities is to the given quantity, so is the quantity of each fimple to the required quantity of each.

Example 4. A vintner is defirous to mix 5 forts of wine together: viz. at 115. per gallon, 105. per gallon, 95. per gallon, 75. per gallon, and 65. per gallon, in such proportion as to make 40 gallons of wine, worth 85. per gallon; how much of each fort must be take?



In this example, after linking the prices together, as before directed, I have the quantity of each wine to form a mixture of 8s. per gallon; but the whole quantity of the mixture thus found is only 11 gallons, whereas it should be 40 gallons, therefore I say,

Gall. As II is	Gall. to 2 fo	Gall. is 40 the quantity required		Pints. 2 1 T
11		40	7	2 12
11	1	40	3	51'5
11	1	40	3	5i'r
. 11	\$	The quantity require		0

Question 5. A grocer has sugar at 10d. 8d. 6d. and 4d. per lb. of which he would make a mixture to consist of 60lb. and worth 5d. per lb.; how much of each fort must he rake?—Answer, 5lb. at 10d. 5lb. at 8d. 5lb. at 6d. and 45lb. at 4d. per lb.

Sometimes it is required to take a certain quantity of any one fimple to mix with the others, and which generally alters the quantities of the other fimples. To find what proportion of the others is requifite, I fay (by the rule of Vol. I. Cc three).

three), so the quantity of that fimple whose particular quantity is given to to the given quantity, so is the sound quantity of any other simple to the quantity required.

Hample 6. A green would mix railing at 11d, per lb. 10d, per lb. 4d, per lb. with 12olb, at 7d, per lb.; how much of each fort must be take, that the whole may be worth 8d, per lb. ?



House the feveral quantities requifits are as placed in the example; but to find the quantities which fhould be taken of each fort, I say (by the rule of three), as glb. (the quantity there found) is to rash. (the quantity required to be taken) so is allow (the quantity at 11d, per lb.) to 7allow (the quantity that should be taken).

14.		14.	14	14,	
	the quantity required	10 7 1	129 14	An f lo to	A
75		4	187	5	
48		z.	177	5	
144		Ļ	139	5	
114	Which, with the				
459	at 4d, per 1h, lo		•.		
والأدع					

Ruefling. A vintus mixes wine at 121, 101, and 61, per gallon, with so gallons at 41, per gallon; how much of 521 for must be take to make the mixture worth 81, per gallon 2 - Anjour, so gallons at 121, 10 gallons at 101, and 10 gallons at 61,

From the foregoing examples it is evident that there are feveral ways of working this rule, according to the method

of stating the question; as may be partly seen in the fourth and fixth examples, which, though quite different questions from each other, yet could of the very same signres, and may be stated in the same manner; but are here varied for the information of the learner, and admit of still greater variety, as the learner may prove at his bessure.

All the caution that is necessary in linking the numbers together, is, that of every two numbers that are linked together, one must be greater and the other less than the rate or price of the mixture. Therefore, the first example in this rule, having but one number less than the rate of the mixture, admits of no other method of stating than that described.

## SECT. XIII.

#### OF VULGAR PRACTIONS.

Reduction, Subtraction, Multiplication, Division, and the Rule of Three.

A FRACTION is any part or parts of an integer or unit, and (in vulgar fractions) is represented by two numbers placed one above the other, with a line drawn between them.

The number below the line is called the Anominator, and flicus how many parts the integer is divided into; the number above the line is called the numerator, and flicus how many of those parts the fraction represents.

Thus the fraction to repretent three farthings is thus written Anumerster and is properly called three fourths of a penny :—a penny being the integer, or unit, of which the fraction is a part,

Vulgar

Vulgar fractions are either proper or improper, fingle or compound.

A proper fraction has its numerator less than its denominator; as, \$ two fixths, \$ three fourths, \$ three ninths; and always flands for less than the integer it is taken from.

An improper fraction has the numerator equal to or greater than the denominator, as 4, 4, 44, and always represents as much or more than the integer.

A fingle fraction is only a fingle expression of any assigned parts of an integer.

A compound fraction confifts of more than one fraction, and its a fraction of a fraction, and they have the particle of placed between them, as 4 of 4, \$ of 4, \$c.

There are also mixed numbers, which are whole numbers united with fractions, as Ma, 1847, &c.

The common mensure of two or more munhers, is that number which will divide each of them without a remainder; thus 4 is the common measure of 18 and 19.

A number that can be exactly mentured by two or more numbers is called their common multiple; and if it be the least number that can be meatured, it is called their least common multiples of both and g, but their least common multiples of both and g, but their least common multiple is ; ;

Refore the learner can proceed to reduction of fractions, it is necessary that he he able to folve the two following Problems.

# # PROBLEM L

To find the greatest common Measure of two or more Numbers.

Kulo. It there be only two minds is, divide the greater by the lefe; and if there he no remainder, the divider to the greatest common meature, but if there he a remainder, the divider by fuch remainder, and if there fill

be a remainder, the last divisor is still to be divided by the last remainder till there be no remainder; then the last divisor is the greatest common measure.

But if there be more than two numbers after having found the greatest common measure of two of them, the common measure of that common measure and one of the other numbers is to be found in the same manner; and proceed in this manner through all the numbers; then the last common measure will be the common measure of each of them.

Example 1. What is the greatest common measure of 624, 3126, and 336?

Thus 6 is the greater common measure of 624, 3126, and 336.

- 2. What is the greatest common measure of 81 and 63?

  Answer 9.
- 3. What is the greatest common measure of 720, 336, and 1736?—Anfeor 8.

#### PROBLEM II.

To find the least common Multiple of two or more Numbers.

Rule. Divide the numbers by any number that will divide two or more of them without a remainder, and fet the quotient of each number under the dividend to which it belongs; bring down the undivided numbers, or those which cannot be divided, into the fame line with the quotient. Then divide

divide the fecond line, in the fame manner, by any number that will divide two or more of them, and bring down the quotients and undivided numbers, so before. Proceed in this manner as long as there can be found any two numbers that can be exactly divided by one number.

When the numbers are to far divided that there are no two numbers that can be divided by one, then multiply all the divitors and the quotients continually together, and the product is the least common multiple.

Example 1. What is the least common multiple of 7, 8, 4, and a?

Here I divide the numbers first by a, as that number exactly measures the 8, 4, and a, the quotients I place under their dividends. I then divide the next line by a, as that measures 4 and a; the quotient I place below, and the 7 I bring down.

A hen, as there are no two others which admit of a common measure, I multiply the divisors and quotients continually together, and the product 56 is the least common multiple of them all.

Before tractions can be wrought by any of the ruler in writimeric, it is necessary to reduce them from compound to fini; le ones, and to bring them into teveral other forms; for which purpose there are eight ways or altering the form of fractions, without changing their value, as follow:

Ca, i. To reduce a mixed number to an improper frac-

R. le. Multiply the integer by the denominator of the framium, and add thereto the numerator, and the product of

will form a numerator to a fraction, whose denominator is the denominator of the former fraction.

Example 1. Reduce 103 gallons to an improper fraction.

😝 the fractions required.

Reduce 5611 to an improper fraction. — Anfauer 1225.
 Cafe 2. To reduce an improper fraction to a whole or mixed number.

This is the reverse of the former cafe.

Rule. Divide the numerator by the denominator, and the quotient will be the whole number, and the remainder (if any) will be the numerator to a fraction, whose denominator is the divisor.

Thus, so reverse the first example in the former case,

\*\* Example 1. Reducested to its equivalent, whole, or mixed

\*\* number.

4)43(10 4 3

10\$ the mixed number.

s. Reduce the second example in the former case \*\* 4.5 to its equivalent, whole, or mixed number.—Answer 56 12.

Case 2. To reduce a fraction to its lowest terms.

Rule. Divide the two terms of a fraction by any number that will exactly divide them without a remainder, and then divide the quotients by a number that will exactly divide them, and fo on till there can be found no number that will exactly divide the last quotients; then these quotients will be the fraction reduced to its lowest terms.

Ot, adly, find the greatest common measure of the numerator and denominator, as taught in the first problem in this fection, and divide them thereby; then the quotients will be the fraction reduced to its least terms.

Example

number, viz. a fraction of a yard; and inversing the first term the question will stand thus,

4 tof 1. 2. - The Augur 2.94, or 10. 111d.

Here it must be observed, that the first and third fractions must be reduced to the same denomination as in whole numbers, as seen in the foregoing example, where they are both fractions of a yard; and the fourth fraction is of the same denomination with the second.

Ly. a. If \$ of a gallon of brandy coll; of a pound, what will sa\$ coll at that rate?—//n/forr '\$5', or 71.00. \$ \$4.5

Lu. g. If the of a bule of linear cost 141, 141, what will 7 hales cost at that rate?—. Inferent 1821, 101.

Qu. 4. If saille of sugar cost 151. gd. what is the price of 48ille. 1-Anfwer 31. 01. gid. 4in

# Rule of Three inverse in Vulgar Fractions.

Eals. Prepare all the fractions as for the foregoing tale, then confider (as taught in the rule of three in whole numbers) whether the question belongs to the inverse or direct rule, and it it belong to the rule of three inverse the third fraction is to be inverted, by transposing the numerator and denominator; and the work is wrought exactly in the fame manner as in the direct rule, by multiplying the three uppermult terms of the fractions together for a numerator, and the undermost terms of the three fractions for a denominator; and the fraction thus formed will be the aniwer.

Prest. As before in whole numbers.

After disposing of the tractions as before directed, I confider that is of a year being a longer time than is, it will not require so much principal lent, therefore the greater of the first and third numbers must be the divitor (as in whole numbers); the third fraction theretors must be inverted, and the question will stand thus:

It \$ of a year \$ of 2000/. \$ of a year?
Anfour 1988, or 1581; ", equal to 158/. 141. 74.d.

Questions both in this rule and the former are proved by back-stating the question, as in whole numbers; thus the foregoing example may be proved by faying, if  $\frac{1}{12}\frac{9}{7}$  of 1000/. principal require  $\frac{9}{12}$  of a year, what will  $\frac{1}{2}$  of 1000/. require? and the an/ture is  $\frac{3}{2}\frac{1}{12}\frac{9}{12}$ , or  $\frac{3}{2}$  of a year.

Qu. s. How much findloon will it require at \ of a yard wide to line the garments made with 10\frac{1}{2} yards of cloth at 1\frac{1}{2} yard wide \( \frac{1}{2} \rightarrow Anjaver \frac{1}{2}\frac{1}{2}, \text{ or } \frac{1}{2}\frac{1}{2} \text{ equal to } \frac{1}{2}\frac{1}{2} \text{ ards.}

29. 3. If is men can mow saff acres in 103 days, how many days will 6 men require to do the fame?—Anfwer 214 days.

From what has been delivered in this fection concerning vulgar fractions, it is plain that every other rule in arithmetic may be wrought by vulgae fractions as well as by whole numbers, as the operation in both cases depends upon the same principle; thus, in the rule of three direct in vulgar fractions, inverting the first fraction, and multiplying it by the second and third, is the same as multiplying the second and third fractions together, and dividing by the first; and in the inverse rule, inverting the third fraction and multiplying it by the first and second, is equal to dividing the product of the first and second fractions by the third, as the learner may prove at his leisure.

## SECT. XIV.

## OF PRACTICE.

PRACTICE is the most expeditious rule in arithmetic, and is of general use among men of business, as it readily discovers the value of any number of integers from having the value of one.

By this rule are answered all questions in the rule of three direct that have an unit for their first number.

Rule. Divide the given number of integers by one or more aliquot parts of a penny, fluilling, or pound, or any two or three of them; and the quotient will be the answer, and of the same denomination of which the divisor is a part.

An aliquot part of a number is such a part, that being taken any number of times, will exactly measure that number without a remainder: thus a is an aliquot part of 6, for it is contained exactly 3 times in 6; and 5; is an aliquot part of a pound, for it is contained exactly four times in a pound; but 5; sel, is not an aliquot part, for it is not exactly contained any number of times in a pound without leaving a remainder.

Before the learner can perform this rule, he must perfectly understand the following tables of aliquot parts, and retain them in his memory.

		The al	iguot	Par	rls			
d.				1.	d.			
6	) (·	f half	<b>)</b>	10	ວີ	1	( ŧ)	1
4	1 1	third	i i	6	8	(	1 1	1
3	1 13	fourth		5	Ú	l		
4	> is <	flixth	}	4	0		;	2
1 }	1 1	eighth	=	•	4	} is ∢	1	<b>2</b>
1	ļ j.	/stwe-lib	ြင်း	2	6			
4,	1	hateenth.	)	3	U			
4 1	half	of a penny	, 1	1	8 (		1/2	
1 1	ourth	, Lenn)	'' }	1	ر ہ		( <u>.</u> !.	

These tables are so plain as to need no explanation; their use is to discover by what number to divide any given number of integers.

Case 1. When the price is less than a penny, divide the given number by the aliquot parts of a penny equal to the given price, and the quotient gives the answer in pence, which reduce into shillings and pounds by division; except the given price be 3 farthings, then it is brought into shillings, and answered at once by dividing by 16.

Example 1. What is the amount of 8047lb. of old iron, at a halfpenny per lb.?

Here divide the given number 8047 by s, as a farthings is the half of a penny, and the quotient 4023 is the price of the iron in pence, and 1 remains, which is 1 halfpenny, for the remainder is always of the fame name with

the divisor; I then reduce the pence into shillings by dividing by 12, and the quotient is 335 shillings, and 3 remains, which is pence; and then reducing the shillings into pounds, the answer is 161. 151. 33d.

Example 2. What is the value of 5763 yards of trimming, at 3 farthings per yard?

In this example 1 divide the given number

by 16, as before directed, as 3 farthings is the

fixteenth part of a flilling, and the quotient
is 360 flillings, which reduced into pounds is

181. os. s \( \frac{1}{4} \). for the 3 that remains in the first division is 3 fixteenths of a flilling, or 3 times

3 farthings, equal to  $2\frac{1}{4}d$ .

21. 3. What comes 445, at Id. ?- Anfaver 91. 34.1.

2n. 4. What is the value of 3370, at \(\frac{1}{2}d.\)? - Anf. 7l. 51.

Caje a. When the price is an aliquet part of a failing, divide the given number by fach aliquet part, and the quetient is the aniwer in failings, which must be reduced into pounds.

Example 5. What is the value of 2761b, of check, at 4d. per th, ?

there the given number of pounds is 3)870 divided by 3, as 4d, is 4 of a thilling, 3,0)29,4 fillings and it quotes 203 fillings, which are brought into pounds; and the defeater 13 to 241, 22.

Ly. 6. If hat is the value of apple, of tallow at 3d. per th. ?—Here the given number must be divided by 4, as 3d. to 4 of a flutting, and the Authors is 11, 14, 3d.

Krample y. What is the value of 10wt, of fugar, at far per lb ?-- Injector \$1, 81.

1.6) 16,1

Enemple 8. What is the value of a syllib. of alum, at 1 fel. per lb. 8--- Infray, 13/, 12/, 36/. 8)2178

4,0) 37,8 3 13

Example 9. What is the value of 416th, at pd. par lb, t-

4.0

Coff. A hen the price of the integer is pence and farthings, and not an aliquot part of a fluiding, find what aliquot part of a fluiding is the nearest to the given price, and lets than it, and divide the given number by that aliquot part; and for the remainder of the price consider what part it is of the given price, and divide the quotient by it; and if there be still a remainder of the given price, consider what aliquot part this is at the last, and divide the last quotient thereby; then add all the quotients together for the answer.

Enample 20. What is the value of 55cmt, of butter, at 84d, per lb.?

6d. in \(\frac{1}{2}\) of a failling a)616 equal to 5\(\frac{1}{2}\) owt.

2d. is \(\frac{1}{2}\) of 6d, therefore divide by \(\frac{3}{2}\) to 8 (equal to 4d.

25\(\frac{1}{2}\) of ad. therefore divide by \(\frac{1}{2}\) to 8 remains a, or \(\frac{1}{2}\) of 6d.

25\(\frac{1}{2}\) remains a, or \(\frac{1}{2}\) of ad.

21

Anfroer s.l. 150.6d.

In this example, I divide the given number first by s, as 6d. is the figurest aliquot part to the price, and the quotient is 308s, which is the price at 6d. per lb.: I then divide that quotient by 3, for the other ad. in the price, and it quotes zons, which is the price of the article at ad. per lb. and a remains a and for the halfpenny I divide the last quotient by 4, as one halfpenny is the fourth part of ad. and the quotient is a 5s, which is the price of the butter at a halfpenny per lb.

Example 11. What is the value of 137 yards of cloth, at 104d, per yard?

the three quotients added together give the antwer,

For the 6d. I divide by a) 137

For the 3d. I divide by a) 08 remains 1, or 6d.

For the 12d. I divide by a) 34

17

2,0) 11,9

Asfour 25

19

10

Lu. 18. What is the value of 520lb. of foap, at 71/1. per lb.?—An, wer 16/51.

24. 13. What is the value of 860 yards of linen, at 114d. per yard?—Asfewer 41h 4s. ad.

Cafe 4. When the price is any number of shillings under ao.

First. If it be an even number of shillings, multiply the given number by half the price, and double the first figure on the right hand, which will be shillings, and all the other figures are pounds.

Secondly. It the price be an odd number of fullinge, multiply the quantity by half the next less number, which will be an even number, then for the odd fluiting add to the given number to the last product, and the sum of these two quantities will be the answer.

20. 14. What is the value of 470 yards of cloth, at 46 per yard?

Here I multiply the given number 476 by s, half the price, faying, a times 6 is 1s, which doubled is 24. I fee down the 4 shillings, and carry the cound 470 9 954 Anfiver 951. 416

to be added to the next product, faying, a times 7 is 14, and a I carried is 15, 5 and carry 1; then a times 4 is 8, and 2 is 9; then I cut off the fielf figure 4 for fillings, and the reft are pounds.

Anomple 15. What is the value of 40s yards of cloth, at 31. per yard?

In this example, 7 being an add number, I take 4 for the multiplier (being the half of 6 the next even number) and multiply as in the former ex-

ample, doubling the first number for shillings, and the product is 1314.131, which is the price of the cloth at 61 per yard; then for the other shilling I take a twentieth part of the given number, and the quotient is 33.31, which is the price of the cloth at 11, per yard, and which, added to the former price at 61, gives 1614.141, the answer.

Faample

## Examples for Practice.

8,0)431 yard	s nt 13s. per yd.	2,0)324 ella	at 170. per ell.
258	10	=59	<del></del>
£. 180	3 Antever.	( 275	8 Anfaver.
A . 800	3 .14/7411.	*::	

8,0(870 yards at 31. per yd. 8,0)8880 yards at 101. per yd.

87	18	8 598	3	• •
13	19	144		
£.41	17 Antiver.	6.2736	0	Anfwer.

Lu. 17. What is the value of \$468 yards, at 51. per yard?
-Answer 6171.

Note. When the price is question, the given number may be divided by 4, as g is for a pound, and the quotient is the answer in pounds.

And whon the price is as, it is done at fight, by doubling the first figure on the right hand for shillings, and the other figures are pounds.

Example 18. What is the value of 806 gallons of cycler at an per gallon?

80/. 121. Appere

By this method of working by an a variety of examples may be wrought very expeditiontly, by dividing the given price into parts of an each, and finding the value of the overplus, if any.

Hample 19. What is the value of 414 gallons of Hollands, at cs. ad per gallon?

	444 gallons
For an per gallon, I take For the other an per gallon	441. 8
For the other as, per gallon	44 8
For the 1s, half the 2s, line	25 ¢
For the 6d. half the tr. line	11 6
For the 3.4. half the 6.4. line	5 11
And then add them together for the And	19. 15

or. I. Ff

In this manner examples in this rule may be wrought, though the price confift of any number of shillings and pence, and which would superfede the necessity of some of the following rules. I shall nevertheless insert them, that the work appear not descions.

Case 5. When the price is shillings and pence, which make an aliquot part of a pound, divide the given quantity by such aliquot part.

Example so. What is the value of \$796 dollars, at 31. 4d. per dollar?

6) \$796

Anfwer 4661.

Here I divide the given number by 6, as 31.4d. is the fixth part of a pound.

Qu. 21. What is the value of 3575 yards, at 15.8d. per yard?—Anfiver 2971. 185. 4d.

2n. 22. What is the value of \$478 gallogian spirits, at 6s. 8d. per gallon?—An/wer 826s.

2n. 23. What is the value of \$793 yards of linen, at s.s. 6d. per yard?—Anfwer 349l. 2s. 6d.

Case 6. When the price consists of shillings and pences or shillings, pence, and farthings, which do not make an aliquot part of a pound, divide the given number by the greatest aliquot part of a pound that the price contains; and for the remainder of the price, if any, consider what aliquot part it is of the former aliquot part, and divide the quotient thereby; and if there still be a remainder of the price, consider what aliquot part it is of the last aliquot part, and divide the last quotient thereby; and proceed in this manner as long as there is any remainder of the price; then the sum of all the quotients will be the answer.

Example 24. What is the value of 3726 yards of cloth, at 71. 41d. per yard? 3)2726

3) 1720 10) 1242 10) 124 4 0 7 15 3 Aufwer £ 1373 19 3

In

In this example, I divide the given number by 3, for 6s. 8d. as that is the third part of a pound; the quotient I again divide by 10, for the 8d. remaining, as 8d. is the tenth part of 6s. 8d.; and this quotient I again divide by 16, for the halfpenny, as that is the fixteenth part of 8d.: then the three quotients added together give the answer.

Or the price may be divided into the aliquot parts of a pound, and then the given number must be divided by each of them; thus, in the foregoing example, the given number of yards may be divided by 5 for 4s, the fifth part of a pound, and 6 for the other 3s. 4d. the fixth part of a pound, and for the halfpenny the given number may be divided by s4, the aliquot part of a shilling, and this last quotient is shillings; and the three quotients added together is the answer.

29.25. What is the value of 784 gallons, at 6s. 9d. per gallon?—Asswer 264s. 12s.

2n. 26. What is the value of 1464 gallons, at 12s. 7d. per gallon?—Answer 9211. 2s.

Case 7. When the price is pounds, shillings, pence, and farthings, multiply the given number by the number of pounds, and the product is pounds; then for the remainder of the price, work according to some of the former rules, as the case may require; and these sums added together will give the answer.

Example 27. What is the value of 416 cwt. of sugar, at sl. 91. 32d. per cwt.?

		416	wt.			
		•				
For the 2	. take	832	•	-		
For 8s.	_	166				
For 11.	_	20	16	0		
For 3d.		5	4	0		2. 3
For $\frac{1}{4}d$ .	_	1	6	•		j,
Au	fwer f	5.1025	14	•	•	
	F f	<b>.</b>				* on

For the st. I multiply the given number by 2, and the product 83s is pounds; then for the 8r. I multiply the given number by 4, fetting the double of the unit figure apart for thillings, as directed in the fourth cafe; for the 12. I take the eighth part of the 8s. line; for the 3st. I take the fourth part of the 12. line; and for the \$\frac{3}{2}\$ I take the fourth part of the 3st. line; and the firm of these is the antiver.

2n. 28. What is the value of 1894 pieces of linen, at 41.150. 104d, per piece?—Anjover 90771.71.94d.

Cap' 8. When the number of integers whose value is required is a whole number with fractions annexed, find the value of the whole number by some of the foregoing rules, to which add the value of the parts represented by the fractions.

Example eq. What is the value of a 78cwt. 84lb. of foapa at 12 191. 44. per cwt.?

	278		
For 11. take	a; H	v	-0
For the.	111	8	0
For 31. 44.	40	6	8
For dewt.	٥	19	8
For Jewt.	O	9	10
. જેવું જીવના	6.518	4	e Faul

In this example, after finding the value of the e78 cwt. at the given price. I find that 84th, is \$ of an cwt. I therefore take \$ of the given price, viz. 101. 8d. for \$ the cwt. and for the other \$ cwt. I take \$ of the price, 91. 10d.

Lingo. What is the value of cost pieces of cloth, as all row od pur piece? Awarer 1435/2013/6

Care q. When the quantity whose value is sought is of several denominations, sink, find the value of the greatest denomination; and for the other denominations, take an equivalent part or parts of the given price; and add the several sums together for the answer.

Example 31. What is the value of socut. agra. a sib. of tobacco, at 41. 51. 6d. per cwt.?

Fol

4	5	6 per cwt.
		10 cwt.
43	15	<u> </u>
4	3	9
0	10	81
0	5	41
3.45	14	91
	42 8 0	42 15 £ 2 0 10

The cwt. being the greatest denomination, is found first, by multiplying the price of an cwt. by 10, and for the value of the squal take half the price of an cwt. then for the salb. I first find the value of 14lb. by taking half the price of a qr. or a fourth part of squal and half this price for the other 7lb.; these sums added together give the answer.

2n. 32. What is the value of a 8yds. 3 fgrs. of superfine cloth, at 30s. per yard?—An/wer 43l. 6s. 3d.

# SECT. XV.

#### OF BARTER.

BARTER is that rule which instructs traders to exchange one commodity for another, so that neither party may sustain any loss.

Rule. Find the value of that commodity whose quantity is given, by the rule of three or practice; then by the rule of three, practice, or division, find what quantity of the other commodity should be given in exchange.

Example 1. How many gallons of brandy, at 6s. per gallon, must be given in barter for 7cwt. aqrs. 14lb. of sugar, at al. 10s. per cwt.?

In this example, I first find the value of the given quantity of sugar by the rule of practice, which I reduce into pence, and it produces 4575 pence; these pence are then divided by 7s, the pence in 1 gallon of brandy, and it quotes 63 gallons and 41 of a pint for the answer.

Thus it appears that questions that concern only one price of each fort, of two different kinds of goods, may be wrought by practice and division only, as the foregoing; but those of a more complex nature must be resolved by the rule of three.

24.2. A grocer has 120lb, of tea, which cost him 6r. Per lb. but he intends to barter it at the rate of 8s. per lb. with a distiller, for Hollands that cost him 4r. per gallon. At what price must the distiller rate his Hollands, that he may have as much prosit as the grocer; and how many gallons must be give for the 120lb, of tea?—An heer, he must rate his Hollands at 5r. 4d. per gallon, and give 180 gallons for the tea.

In refolving this question, first find what the Hollands must be rated at, by the rule of three, saying, if 6s. require 8s. what will 4s. require?—Answer 5s. 4d.—Then by practice (as in the first example) find the value of the tea at 8s. per lb. which, divided by the price of 1 gallon of Hollands, as before, quotes the answer.

Qu. 3. A vintner barters 196 gallons of wine for 14cwt. of fugar worth 6d. per lb. how much was the wine worth at that rate?—Anfaver 4s. per gallon.

Qu. 4. A barters 320 gallons of gin, at 4s. 6d. per gallon, with B for 6lb. of tea at 5s. per lb. and for fugar at 8d. per lb.; how much fugar will A receive?—Anfaver 11cwt. 19r.

24. 5. A vintner barters 608 gallons of brandy at 141. per gallon, for fugar at 31. 101. per cwt. and 1251. 121. in cash; how much fugar should the vintner receive?—Anfruer Scowt. 2013. 241b.

## SECT. XVI.

#### OF LOSS AND GAIN.

Loss and gain is that rule which discovers the loss or gain from buying and felling goods; and instructs traders how to fix their price, in order to gain or lose any certain sum.

Rule. By the rule of three direct. Though questions in this rule may often be answered by practice, or other rules.

Example 1. At how much per lb. must a grocer sell tea which cost him 4s. tod. per lb. so as to gain 27 per cent. profit?

When the gain or loss is required at any rate per cent, where the interest has a 5 or a cypher on the right hand, as is most commonly the case, the autiwer may be readily found, by adding to or subtracting from the given price such a port as the interest is of the principal; thus, if it be required to gain or lose 5 per cent. (as 5 is the twentieth part of an hundred) the autiwer is found by adding to or subtracting from the given price one twentieth part; and if the gain or lose to per cent, then it is one tenth part; and if 15 per cent, it is  $\frac{1}{2}$ ; and 20 per cent, is  $\frac{1}{2}$ ; and 20 per cent, is  $\frac{1}{2}$ , &c.

23. 2. A giver bought Hicket, of fugar, which cost 311 141.8d.; but, it being damaged, he is willing to lide 141.101. per cent. in the sale of it, at how much per lb. must be fell it?—dufoce 7.1. per lb.

In this example I inherers the loss per cent, from the principal, and the remainder is the fecond number in the rule of three, the principal the first number, the whole price of the sugar the third number; and the fourth number will be the whole price at the reduced rate, which disided by the number of pounds, gives 7% the price of the.

Lo. 3. A wholefule factor to Ireland made linen, which cost him recid, per yard, the capetile of lending it to London 14d, per visit, it was fold in London at 11, 1,d, per yard, and the retail trader was allowed 26 per cent, profit, what profit had the wholefule factor :—, day, or, 24 per cent.

In resolving this quantion, I say, as in adother expense of reaking and exporting the linen, is to in 9d the retail price, so is 1000 to 1500; thus there is 50 per cents profit, which, after deducting 26 per cent, the retail trader's profit, leaves 24 per cent, for the factor.

La. 4. A merchant bought 100 gallons of brandy; at 65, per gallon, of which quantity 40 gallons were loft; at what price per gallon must be fell the remainder, that he may gain 10 per cent. profit upon the money it cost him?——Anjure 111 per gallon.

#### SECT. XVII.

#### OF EQUATION OF PAYMENTS.

EQUATION of payments is that rule whereby is discovered the time to pay at one payment several sums due at different times, so that neither party may sustain any loss.

Rule. Multiply each debt by the time at which it is due, and add all the products together; divide the fum of the products by, the fum of all the debts, and the quotient will be the answer, or the equated time to pay the whole.

Example 1. A is indebted to B in the furn of acol. to be paid as follows: 60/. in 4 months, 40/. in 6 months, and 100/. in 10 months; what is the equated time to pay the whole?

Debts.		Months.	Products.
60/.	in		<b>\$40</b>
40		6	940
100		10	1000
800		2,0	0 14,80
Ansaver 7	a mon	th <b>s.</b>	711 11
•		C =	:25

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Ly. a. A owns B rood, of which  $\frac{1}{2}$  is to be paid in 6 months,  $\frac{1}{2}$  in 8 months, and the remainder in 10 months; what is the equated time to pay the whole?—Anfaver  $\frac{1}{2}$  months.

In this example, \( \frac{1}{2} \) of 1000/. multiplied by 6 months produces \( \frac{1}{4} \), and \( \frac{1}{4} \) (the remainder of the 1000/.) multiplied by 10, produces \( \frac{1}{4} \); and thefe three products added together gives \( 7 \) \( \frac{1}{4} \) months for the answer.

And, note, when the fums or times of payment are given in fractions, the fum of the products is not to be divided by the fum of the debts, as it is in whole numbers.

Qu. 3. A tradefman owes his creditor 1441; 441, he pays in ready money, 601, is to be paid at the expiration of 6 months, and the remaining 401, at the expiration of 8 months; but the tradefman defiring to have more time for the payment of the last 401, pays his creditor the 601, due 6 months after, in ready money; how long may be defer paying the last 401, to make him amends for this prompt payment 1—Answer 17 months.

In this example, the 441 to be paid in ready money is neglected; but for the 601 paid 6 months before due, I find by the rule of three what interest it would gain at any rate per cent. in that time, and then how long the 401 may be lent for that interest at the same rate, which I find is 9 months, and which added to 8 months, its time of payment, gives 17 months for the answer.

<sup>\*</sup> This rule, though greatly used by men of business, is not mathematically exact. The reason of the rule given by many writers, is, that for the debtor paying a sum before the time it is due, an equal turn should be sorborn, for as long a time after it is due; but this is a missale, for by the debtor paying money before it is due, he has the discount only; but keeping the money after it is due, he gains the interest, which is greater than the discount.

## SECT. XVIII.

# OF THE RULE OF FALSE, SINGLE AND DOUBLES, (GENERALLY CALLED POSITION.)

This rule teacheth to answer such questions as cannot be resolved by any direct rule in vulgar arithmetic, and must be performed by false or seigned numbers.

Position is either single or double.

Single position is when the question can be resolved by one take position or set of seigned numbers, and one operation in the rule of three direct.

Rule. Take any number, and proceed exactly the fame as if it were the true number through all the proportions mentioned in the question.

Then fay (by the rule of three) as the refult of this false operation is to any of its parts, so is the true result in the question to the corresponding part required.

Example 1. A fon alking his father his age, the father answered, I am slouble the age of your eldest brother John, and he is three times the age of your youngest brother Henry, and the sum of all our ages is 80 years; what is each person's age?

False Supposition.		The Truth.	
Suppose Henry's age is	6	Henry's ago	8
Then John's age will be	18	Joh <b>n¹</b> ≉	84
Then John's age will be And the father's age	36		48
The fum of the ages	60	The fum	80
4	==		

Here I suppose Henry's age to be 6, at which supposition John's age must be 18, the father's 36, and the sum of these three is 60, whereas it should be 80; then I say, as 60 the sum of the falls supposition, is to 80 the sum of the true one,

so is 6 the supposed age of Henry to 8 his true age; therefore John's age is 24, and the father's 48, as in the example.

Qu. s. A asked B how much money he had in his pocket; B answered, if you give me 4 guiness of the money in your pocket, I shall have 5 times as much as you will then have; but if, instead of that, I should give you a guiness of the money in my pocket, you will then these twice as much as I shall then have: how much money had each?—Answer 6 guiness.

Ap. 8. A person hired a boxse for 9 days, on the following terms: for the first 3 days he was to pay 4 of the hire for the next 3 days, and for each of the last 3 days as much as the hire for the first 6 days; the whole was at first; what was it per day?—Apsur, at per day the first 3 days, 9. per day the next 3 days, and 12. per day the 3 last days.

Double position, or the double rule of false, is when two false positions are neguiste to give an uniwer to the question.

Rule 1. Take any two convenient anothers, and mark with each of them according to the question, as in angle position. s. Find the difference hetween the result of each of these false positions and the result of the question; their differences are called the errors. 3. Multiply each error by the contrary polition, that is, the first error by the second polition, and the second error by the first position; then find the fum and difference of the products. A. If the errors are both alike, that is, if the refult of the two positions he both greater or both less than the result of the question, divide the difference of the products by the difference of the errors, and the quotient will be the aniwer. c. But if the errors be unlike, that is, if the refult of one polition be greater and the other less than the truth, then the sum of the products must be divided by the sum of the errors, and the quotient will be the aniwer.

Example t. Three persons, A, B, C, bui't a house, which soft good, of which B paid half so much again as A, and C paid as much as A and B together; what did each pay?

First Supposition.	Second Supposition.
Suppose A paid £90 Then B must have paid 135	Suppose A paid £96
Then B must have paid 135	Then B must have paid 144
And C must have paid 225	And C have paid 240
Refult 450	Result 480
First error 50	Second error so
Second polition 96	First position 90
300	Second product 1800
450	===
First product 4800	
Second product 1800	

Difference of errors 3,0)300,0 difference of the products.

B must have paid 150 for A's share, wherefore being half as much again as A, and D must have paid 250 being as much as both A and B, which added agester gives £500 the original sum.

From this example may be seen the method of working this rule, which is always the same, except when the errors are unlike, then the sum of the products is to be the dividend, and the sum of the errors the divisor as above directed.

- Qu. a. A falefman bought a number of oxen, theep, and lambs, for which he paid 1151.; for the oxen he paid 101. each, for the sheep 201. each, and for the lambs 101. each; how many of each fort did he buy?—Anfour 10 of each.
- Le. 3. Three persons, A, B, C, have equal incomes; A saves is of his income every year; B spends tol. per annum more than A, and C spends tol. per annum more than B. At the expiration of sive years, C finds himself in debt 50l. what is each person's income, and what has each saved or spent?—Answer, the income of each is 100l. per annum; A has saved 50l.: B has saved nothing; and C has spent 50l. more than his income.
- La. 4. A labourer was hired for 40 days; for every day he wrought he was to receive 2s. and for every day he was idle he was to forfeit 1s.; at the end of the time he had to receive 44s.; how many days did he work, and how many was he idle?—Anfauer, he wrought 28 days and was idle 16 days.

  SECT.

#### SECT. XIX.

#### OF EXCHANGE.

Exenance is that rule which teacheth to find what furn of the money of one country is equal to a given furn of the money of another country, the course of exchange being known.

The course of exchange is that sum of the money of one country which is proposed to be given for a certain constant sum of that of another country: thus, when we say the course of exchange between England and Holland is 34s. Flemish per pound sterling, it signifies that s pound sterling is equal to the value of 34s, in Flemish money. This course of exchange varies on the part of the foreign coins, according to the state of public affairs.

The par of eachange is that quantity of the coin of one country which is intrinfically equal to a certain quantity of the coin of another country, according to the value of the metal.

Mok foreign countries have two forts of coins, called current money and banco money; the first is that in general whe throughout the country; the latter is that kept in the banks of those places, and is finer than the other; the difference between any sum as it is valued in current money, and banco money, is called the agio.

The money used in exchange is generally imaginary, and different from that in which the accompts are kept in most places: the money used in exchange also differs from current money in its value.

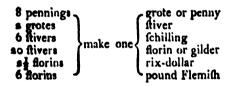
Belure

Before the learner can resolve any questions in this rule, it is necessary that he know how the country with which the exchange is to be made keep their accounts.

# Holland, Flanders, and Germany.

In these countries accompts are kept in gilders, stivers, and pennings, similar to the English pounds, shillings, and pence.

But the different denominations of their money are contained in the following table:



Note. The money of Holland and Flanders is called Flemish money, and they exchange by the pound sterling.

The course of exchange with these countries has mostly been (except during the troubles on the Continent) from 33..4d. to 36s. 6d. Flemish per pound sterling; and the agio from 3 to 6 per cent.

As the exchange with all countries is supposed to be made in banco money, the current money must be turned into banco before the exchange can be made.

Rule. By the rule of three, or practice.

Proof. By reverling the question.

To change current money into banco, and banco money into current.

Say, by the rule of three, as tool, with the agio added to it, is to tool, so is the given sum current money to its value in banco.

And,

And, as rook is to rook with the agio added to it, so is the given sum banco to its value in current money.

Example r. In 210% ton 6% seeling, how many storius, stivers, and pence current, the course of exchange being at 35% 74% Flemish per pound sterling, agin 4% per cent.?

For th take	£110 10	6
For ton take	55 5	3.
For si.	27 18	7
For 6d.	2 15	3. 10
For 11th	0 13	94 1/4
	£. 146 17	5 <b>‡</b> ‡

Then to find the value of this fum in current money. I say, as cook is to rook to is right ton 5 to sook ton the trade

Affirer 1228 flore o flive 6 pence.

1008 9 6

By the rule of practice, I first reduce 1 rol. 10s. 6d. serling, into Flemish money, and it produces 1966. 17s. 54d. 4. Then by the rule of three, as before directed, I bring this money into current money, and it produces 2046. 24s. 14d. omitting the fraction of a farthing; and this multiplied by 6, the number of florins in a pound Flemish, produces 1208 storins 9 stivers 6 pence, for the answer.

Let a. In 91st. 16s. sterling, how many rix-dellars current, agio 44 per cent. exchange 36s. 14d 1-defluer 4141 rix-dellars.

Le. 3. In 1876 forms 7 flivers 1 grote, current, egio 64 per cent. how many pounds sterling, exchange at 350. 2 ad.?

—Asfore 1651. 21. 2d.

# In Hamburgh

Accompts are kept in marks and fols lub, but the exchange is by the pound sterling, as in Holland.

a deniera

The exchange with this place has mostly been from 32 to 35s. Flemish per pound sterling, and agio from 18 to 20 per cent.

Example 4. In 886 marks 12 fols lub banco, how many pounds sterling, exchange 36 fols gros a deniers per pound. Rerling?

36 fols gros a den. 886 marks 12 fols lub 16 (218 434 887 14188 fols lub 434)28376(65% Anfwer 651. 75. 73d. 2330 30 434)3320(75. 3038 282 434)3384(74. 3038

Here the marks and fols are reduced into deniers, as are also those in the course of exchange; then the course of exchange I make the divisor, and the foreign coin the dividend, and the quotient is 651. 75. 74d. for the answer.

20.5. In 10721. Sterling, how many marks, the exchange at 361.44. Flemish per pound sterling?—Ans. 14606 marks.

24.6. In 16861.21.5\frac{1}{2}d. sterling, how many rix-dollars and fols lub current, exchange at 33 fols gros 9\frac{1}{2} deniers, agio 18\frac{1}{2} per cent. ?—An/wer 8434 rix-dollars 23 fols lub.

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## In France

Accompts are kept in livres, fole, and deniers; and the exchange is by the egu, or crown tourness.

The exchange has mostly been from 30d, to 33d, sterling per ecu ".

Example 7. In \$465 livres 18 fols 9 deniers, how many pounds sterling, exchange 31 fd. per ecu?

Here the livres, fols, and deniers are brought into crowns tournois, by dividing by 3, and that quotient divided by the aliquot parts of the course of exchange gives the answer.

3) a 465 ta 9
30d. 8) 8st 17 7
11d. so) 10s 14 81
5 s 81
Anfwer £ 107 17 5

2.8. In 15431. 15th sterling, how many French pistoles, exchange 301d. per ecu?—Answer 3600.

# In Spain

Accompts are kept in piastics, rials, and marvadies; and the course of exchange is by the piastre, and is generally from 38 to 42d sterling per piastre.

4 marvadies vellon, or 3 marvadies of plate 3 2 quartas, or 34 marvadies vellon 3 make one 34 marvadies of plate 3 pialices a pistoles	quarta  rial vellon  rial of plate, or dollar  pifo, piaftre, or piece of  Spanish pistole [eight=
--	--

The course of exchange mentioned in every part of this fetter or means the exchange as it generally flood before the late unhappy afflure on the Continent.

Example

Example 9. In 8746 risks of plate, how many pounds sterling, exchange at 414d. per plastre or piso?

Here the rials are brought into piastres or pisos, by dividing by 8, as the exchange is by that piece, and the remainder of the work is wrought as the 7th example.

	8)1	rials. B746	0	0
For 40d.	6)	1003	.5	•
For 1d.	40)	182	4	
For 🛂 d.	2)	4	11	14
		2	_5	6
Anfred	r L	189	0	9

Qu. 10. In 1781. 55. 11d. sterling how many rials of plate. Sec. exchange at 40 dd. per piastre?—Answer 8452 rials plate 8 quartas.

# In Portugal

Accompts are kept in reas and milrens; and the exchange is by the milrea, and generally from 60 to 67d. per milrea.

Example 11. In 1864 milreas 108 reas, how many pounds sterling, exchange at 53. 9d. per milrea?

For 5s. 4) 1864 0 0 For 6d. 10) 466 0 0 For 3d. 2) 46 12 0

24. 12. In 1509l. 17s. how many crusadoes, the exchange at 641d. per milrea?—Answer 14045 crusadoes.

# In Venice and Leghorn

The accompts are kept in dollars, foldi, and denari. The exchange is by the ducat and piastre, and from 52d, to 54d, per ducat, and from 45d to 54d, per piastre, and the agio so per cent.

Example 13. In 846 piastres 10 soldi 8 denari, how many pounds sterling, exchange 4°4d. per piastre?

Qu. 14. In 8311. 141. 8d. sterling, how many ducate, &c. current, exchange at 53d. per ducat, agio so per cent.?—
Anjuer 4519 ducate 14 grosse.

The foregoing examples will be found sufficient to instruct the learner in the method of performing this rule; I shall therefore insert the remainder of the tables of foreign coin, and a few questions with their answers, omitting the operation for the practice of the learner.

# In Ruffia

Accompts are kept in rubles and copees; and the exchange is by the ruble; and when made immediately with London, is from 41, to 51, per ruble; but when made by the way of Hamburgh or Amterdam is from 48 to 50 flivers per ruble.

20. 15. In \$337 rubles 73 copecs, how many pounds flerling; exchange, by way of Amsterdam, at 122 copecs per rix dollar of 50 stivers; and exchange between Holland and England at 341.7d. Flemish per pound sterling?—Answer 2301. 171. 3d.

Qu. 16. For 9431. 141. 8d. paid in London, how many rubles must be received at Petersburgh, exchange by way of Holland at 341. 9d. Flemish per pound sterling, and exchange from Holland to Petersburgh at 50 stivers per ruble?—Answer 7870 rubles 36 copecs.

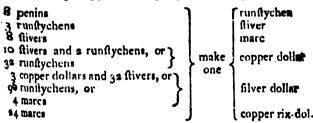
## In Poland and Prussia

Accompts are kept in florins, gros, and penins. The exchange is by the way of Holland, and from \$40 to gros per pound Flemish.

Qu. 17. In 4371. 175. 4d. sterling, how many rix-dollars Polish, exchange 290 gros per pound Flemish, and 345. 4d. Flemish per pound sterling?—Answer 2422 rix-dollars 4 gros 13 penins.

#### In Sweden

Accompts are kept in copper dollars, and corts or filver dollars. The exchange is by the copper dollar, and mostly from 46 to 50 copper dollars per pound sterling.



20. 18. In 5838 filver dollars 9 runflychens 3½ penins, bow many pounds sterling, exchange at 49 copper dollars per pound sterling?—Anjwer 3571. 81. 82d.

٠,

In Ireland, America, and the West Indies,

Accompts are kept in pounds, flullings, and pence, as in England, but the course of eachange between lingland and Ireland is from 5 to 12 per cent, in favour of England, and the course of ex hange of the paper of America and the Wen Indies is never at any certain fiandard.

20.19. If 21721, he remitted to Ireland, how much money ferling may be drawn for it, exchange at 8 per cent.?

20. 20. A merchant fells goods in London, and remits to Answer 27,451. 151. 231. his correspondent in Boston, the value amounting to 115th 19th how much must the averchant at Bofton receive in paper currency, exchange at 33 per cent. in favour of

Qualitims of the nature of these two are resolved by the England ? - Anfrect 15351. 181. 8d. rule of three; thus, in the 16th question, I say, if 1006. sequire 1081, what will 21721, require? and the answer is 03451. 151. 23d.

The arbitration of enchange is the method of finding the course of exchange between any two places, by having the conrie of exchange between earls of these two places and a third place.

By comparing the pur of exchange thus found with the course of exchange, a perion can tell which way to draw or senit his money to the most advantage.

All questions in admiration of exchange are resolved by the rule of three direct, comparing the course of exchange between any two places, with that of a third place to a fourth.

Example 21. If the exchange between Landon and Paris be 33% percent, and the exchange between London and Amflerdam be 340.6% per pound flerling, what is the par of athirration between Paris and Amilerdam?

As \$40d. London is to 34s. 6d. Amsterdam, so is 33d. Paris to

Here I fay, as a 40% the pence in a pound sterling of E-ondon, is to 34% of the Flemish exchange, so is 33% the exchange for an ecu, or crown tournois of Paris, to 56%. Say farthings the Flemish exchange for an ecu, and is the curfe of exchange between Paris and Amsterdam.

This example will be sufficient, as the rule never varies, though the course of exchange between several countries he will be not a proportional course between any two; in which case they may be resolved into as many questions as is successary in the rule of three, and all the first numbers multiplied together for a divisor, and the second and third numbers in each question multiplied together for a dividend, then the quotient will be the answer.

Pa. 22. A merchant in London is drawn upon by his correspondent in Ruffia for money to the amount of 12500 rubles; the exchange between England and Ruffia being at 50d. per ruble; between Ruffia and Holland 90d. per ruble; and between England and Holland 36s. 4d. per pound sterling; which is the most advantageous method for the London merchant to pay by; directly to Ruffia or by way of Holland, and what is the advantage?—An/wer, the London merchant will gain 23d. 17s. 204d. by making payment by way of Holland.

SECT,

## SECT. XX.

# OF THE RELATION OF NUMBERS.

Awy fot of numbers that confiantly increase or decrease a commun difference are faid to bear a relation to each other, which relation is called progression, and is divided Into two kinds a arithmetical progression and geometrical

Arithmetical progression is, when any fet or feries of mumbers continuity increase or decrease by a given numbers progration. called from thence their common difference; fuch are the matural orders of numbers, 1, 8, 3, 4, 5, 6, 7, 8, &c. each of which increases by 11 and the time in inverted order 8, 7, 6, 5, 4, &c. decreate by 11 1 is therefore their common

Again, the numbers a, 5, 8, 11, 14, 17, &c. increase by 31 and 27, 24, 19, 15, 11, 7, &c, decrease by 41 therefore 9 is the common difference of the former, and 4 that of the difference.

The numbers theintelves that form the ferres are called the biler.

Of every feries of arithmetical progression having any three of the five following terms the other two may be found same of the broducilion. readily s

- s, the first term or number } called the extremes.
- 3, the number of terms.
- 4, the common difference.

5, the fum of all the terms.

**PROBLE** 

#### PROBLEM I.

The first and last terms, and number of terms being given, to find the sum of all the terms, and the common difference.

Rule. To find the fum of all the terms, multiply the fum of the extremes by the number of terms, and half the product will be the answer; and to find the common difference of the terms, divide the difference of the extremes by the number of terms made less by 1, and the quotient will be the answer.

Brumple 1. What is the fum of the feries, and the come on difference of that progression, whose first term is 3, last term of, and number of ferms 33 h

. pumbe

last term 67	last term 67 33	•
first term 300	first term 3 i	
70	difference 64 33	
er of terma 33	—————————————————————————————————————	
819	32)64	٠
210	common difference	8
2)2310		
1155 Anfr	ver, sum of the series. 🛬	

In the first operation, 70, the sum of the extremes, is multiplied by 33 the number of terms, and half the product 1155 is the sum of the series, or sum of all the numbers, 3; 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35, 37, 39, 41, 43, 45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67, added together.

In the second operation the difference of the two extremes 67 and 3, or 64, is divided by 32, which is one less than the number of terms, and the quotient 2 is the common difference.

#### PROBLEM II.

Having the two extremes and the common difference, to sad the number of terms.

Rule. Divide the difference of the extremes by the com-

difference, and a added to the quotient will be the wample s. What is the number of terms of that progref. A whole extremes are 3 and 67, and common difference 3

Thus 64, the difference of he extremes, divided by s. the common difference, quotes 33, to which adding a there is 33, the number of terms ; so

33 number of terms.

In every arithmetical progression the Sum of any two terms is const to the fam of suh two other ferms sayen at su const may he feen annexed. distance from the former, and on opposite sides; thus, in the totekonik hodiction 12 and 18 is ednal to 33 and 18 i Aiw And 31 and 33 is equal to \$3 and 41, vis. 64. the double of any oun term is ednal to the fum of any two terms taken on each fide of it, and at an equal diffance from it; thus the double of a 5 is equal to 19 and 31, viz. 50.

24.3. How many firokes does an English clock Brike in

The travellet go a journey of to days travelling 3 miles the first day, and increasing 3 miles every day, how 8 days ? - Jajauer 1348 Arokes. many miles will be travel in the 10 days and how many miles the last day?—Assur, 165 miles in the whole, and 30 miles the laft day.

Geometrical Progression. When any feries of numbers increase or decrease by a enu-State multiplication or division, they are faid to be in grown

Thus the numbers 4, 6, 16, 32, 64, &c. and 243, 81, 87, 3. 1. are in Beometrical brokeeffour, the former jacreaffag Bulliflying each preceding number by s. and the li si ical progression. decreating by dividing each preceding number by 3.

:۲:

£ . Thus, in geometrical progression, the numbers are increased by multiplication, and decreased by division; whereas in arithmetical progression they are increased by addition and decreased by subtraction.

The number in geometrical progression by which the series are multiplied or divided, is called the ratio; whereas an arithmetical progression the number by which the series are increased or diminished is called the common difference.

In geometrical progression, as in arithmetical progression, having any three of the following terms, the other two may be readily found.

- i, the first term } the extremes
- s, the last term
- q, the number of terms.
- 4. the ratio.
- 5, the fum of all the terms.

#### PROBLEM I.

Having the first and last term and the ratio, to find the fum of the terms.

Rule. Multiply the last term by the ratio, and from the product subtract the first term, and the remainder divided by one less than the ratio will quote the sum of the series.

Example 1. What is the fum of the feries of a geometrical prescrition whose extremes are z and 65536, and the ratio 4?

last term 65536
ratio 4
a63144
first term 5
one less than the ratio 3)263143
the sum of the series 87381

Here the last term is multiplied by the ratio 4, the first term 2 subtracted from the product, and the remainder divided by 3, which is 1 less than the ratio, and the quotient \$7381 is the sum of the series.

Au. a. What is the fum of a facility of numbers, in geometrical progression, whose extremes are ross and 59049, and the ratio 2 ! - Anfauer \$8061.

#### PROBLEM IL

Having the first term and the tatio, to find any other term remired.

Rule. Write down a few of the leading terms of the feries, and place their indices over them, beginning with a cypher ..

Then add any of those indices together, which will make an index an unit los than the number which expectics the place of the term required.

Multiply the terms of the feries together belonging to those indices, and the product will be a dividend, to be divided by the product of the first term, multiplied by a number an unit less than the number of terms multiplied; and the quotient will be the antwer.

Example 3. What is the last term of that geometrical forces whole first term is 3, ratio a, and number of terms 10 ?

<sup>\*</sup> I he configure of the feethe if eith if entre de explant at t grouped that he feelth account not for mit material cortex of muthiliata a flow "the index of the full take in 6, that if the favored term to the in it. term of the bourth of here; him a lent fie fieft turm of the feries to aqual by the below the indices might begin with an unit, and the product or the terms will be the antwee, without dividing by the product of the for term, as discred alone .

In this example, the indices 4 and 5 added together are 9, which is a loss than the number of the term tought a then the term belonging to these indices, 48 and 96, are multiplied together for a dividend, the first term 5 multiplied by a less than the number of terms, which are multiplied together, is the divisor; and the quotient 1536 is the answer.

Now. The number of terms multiplied together in this example are a; therefore 3 the first term multiplied by a less than a, or z only, produces 3...

Emanyle 4. What is the 19th term of a feries whole firk term is 3, and ratio 3?

Here, as the first term is equal to the ratio, the indices must begin with s, instead of o; and as many indices must be taken as will make the entire index to the term tought, viz. 15, and the product of the terms must not be divided, as in the former case.

- Qu. 5. What is the last term of that geometrical series where the first term is 1, ratio 2, and number of terms 23?

  Agree 4194304.
- 2s. 6. A person having an elegant house to dispose of, coffered it to sale on the following terms: for the first window the purchaser was to pay: farthing, for the second window a farthings, for the third window 4 farthings, and so on, dou-

new dividor: then I feek how aften the dividor 48 is contained in 174, and the aniwor. I place both in the quetient and dividor as before, and multiply the dividor also thereby, and the product 1449 placed under and subtracted from the special of. I have agree for the last reference, and the double of 430 or 486 for a divitor: this last quotient is 6, which I place in the quotient and divitor, and multiply the divitor thereby, and the product is aqual to the last resolvend: thus 436 is the answer.

- Lu. a. What is the square root of 132399021 imageher
- 20.3. What is the fanare root of \$2071204?—. Infever 4608.

#### To extract the Cube Root.

- Rub 1. Divide the given number into periods of three figures each, by placing a point over every third figure, beginning with the unit figure,
- 3. Find the greatest cube in the first partial, and place its cube root on the right hand of the given number.
- 3. Subtract the cube from the taid period, and to the remainder bring down the next period, which is called the resolvend.
- 4. Place three times the root under the refolvend, and also share times the fquare of the root, the latter being removed one place to the left; there two added together form a divitor.
- s. Seek how often this divitor is contained in the refulsend, exclutive of the place of units, and place one less than the answer in the quotient.
- 6. Under the divitor place the cube of the last quotient figure, the square of it multiplied by three times the rest of the quotient, and three times the root multiplied by the square of the quotient; each of the two latter numbers being removed one place farther towards the left hand than the sources.

foregoing, and the fum of these numbers is called the subtrabend.

7. Then fubtract this fubtrahend from the refolvend, and to the remainder bring down the next period for a new refolvend, with which proceed as before, and so on till the work be finished.

Example 4. What is the cube root of 164,66502 ?

```
164566592(548
                 cube of the first period
      185
                 first resolvend
 765) 30566
                 three times the root &
           15
                 three times the iquare of 5
          75
         765
                 first divisor
                 cube of 4 . .
          64
                 square of 4 multiplied by 3 times 5
        810
       300
                 three times 4 multiplied by the square of 5
                 fubtrahend
       98464.
86744)7102592 second resolvend
            16a three times 54
                 three times the square 54
         8748
         87612 fecond divisor
            (12 cube of 8
                 fquare of 8 multiplied by 3 times 54
        10368
                 three times 8 multiplied by the square of 34
       60081
        102502 fecond subtrahend
           Aufwer 5.48 the cube root required.
```

2n. 5. What is the cube root of 389017?—Answer 73.

2n.6. What is the cube root of 405 12t ? - Answer 73.

There are many other methods of extracting the cube root given by different mathematicians; but none of which I have feen are so simple and easy to be remembered as the method here laid down.

After what has been faid, it need hardly be mentioned, that the extraction of the iquare root is proved by multiplying the root into itself: and the extraction of the cube root, by multiplying the root three times into itself.

CHAP.

#### CHAP. IV.

#### Or DECIMAL ARITHMETIC.

#### SECT. 1.

#### REDUCTION OF DECIMAL PRACTIONS.

A DECIMAL fraction is that fraction whose denominator has an unit in the first place on the left hand, with as many cyphers annexed as necessary: thus to the fractions are usually expressed in writing without a denominator, by writing the numerator, and presixing as many points or cyphers before it on the left hand, as there are more places of figures in the denominator than in the numerator. Thus the foregoing fractions are written .5, .25, .048, .0572, and expressed five tenths, twenty-sive hundredths, forty-eight thousandths, &cc.

Cyphers placed on the right hand of decimal fractions make no alteration in their value: thus, if a cypher be annexed to the foregoing fraction.5, it will be then .50 fifty hundredths, or half an integer, as before; if two cyphers .500 it will be five hundred thousandths, or §, and the same of the others.

But cyphers placed on the left hand of a decimal fraction decrease their value, every cypher decreasing it in a tenfold proportion: thus .5, .05, .005, are five tenths, five hundredths, five thousandths parts respectively.

The

The value of every figure in a decimal fraction increases in a tenfold proportion from the first place on the right hand, as in whole numbers.

The figures in the first place of a decimal fraction on the left hand are called *primes*, those in the second place feconds, those in the third place thirds, &c.

#### DECIMAL TABLES

or
Coin, Weight, and Meafure.

TA Engli	A C	nin.	English Long M	Coin 11. Coin 11. eaf. 1 foot cight 102.	Grains.	,016666 ,0145 ,008333 ,0041666	6 5 4 3 2	,0125 ,013416 ,008333 ,00625 ,004166 ,002083
SA. Dec 19 ,95 18 ,95 17 ,85 16 ,8 15 ,75 14 ,7 13 ,65 12 ,6 11 ,55 10 ,5	98 40 54 34	145 135 135 125 125 105	Farths.	Decimals •5 •41666 •333333 •25 •106666 •88333 Decimals •0625 •041666 •020811	12 11 10 9 8 7 6 5 4 3 2	,001083 ,001910 ,001736 ,001362 ,001315 ,001042 ,000694 ,000521 ,000173	Avoir	I.E. IV. dup. Wt. he Integer Decimals .75 .5 .25 Decimals .125
5 4 3 4 1,	,025 ,016 ,016 ,008 ,004	833 666 5 333	Troy	Weight. e Integer. Decimals	Penny w	e Integer. eights the es Shillings First Table Decimals.	13 11 11 10 9 8	,116071 ,107143 ,048214 ,089286 ,080357 ,071428
Farths: 3 2 1	,001	mati. 125 0833 0416	9 8 7	,0375 ,033333 ,024166 ,025 ,020833	11 10 9 8 7	,015 ,012916 ,020833 ,01875 ,016666 ,014583	5 4 3 2 1	053571 ,044643 ,035714 ,016786 ,017857 ,008928

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10.00	B. 88.1 W . 54					P'' N	\$ :- 1. Table 4 12

Coff r. To reduce a vulgar fraction to a decimal our of the fame value.

Rule. Divide the numerator by the denominator, and the quotient will be the decimal fraction required.

If the numerator be too fmall to be divided by the denominator, add one or more explicits thereto, in which eate as many places must be reparated from the quotient for decimals as the difference of the number of places of decimals in the dividend and the divitor, and the remaining figures in the quotients (if any) are integers.

For it the number of places in the quotient be less than the required number of decimal places, as many cyphers must be prefered on the left hand thereof as are needfary.

Except to What is the decimal fraction of a pound equal to \(\frac{1}{2}\)?

Here

Here two cypliers must be added to the namerator, which divided by 4 quotes 75, which I .75 mark for decimals, as there are two decimals added to the dividend, and the quotient is the feventy-five hundredth part of a pound, or 3, equal to 156.

Example 2. What is the decimal fraction of a pound equal to 9d.?—Anfrwer .0375.

As there are but three places of figures 24,0390000(.0375) in the quotient, I place a cypher on the left thereof, for there should be four figures pointed off for decimals, being so many cyphers annexed to 9; thus the quotient is 18785 of a pound.

- Example 3. What is the decimal fraction of a pound for 3 farthings?—Anfaber 1.003125.
- : Here the vulgar fraction for 3 96,0)300000,0(.003125) farthings is why; I therefore place
- as many typhers as are necessary to the numerator 3, which in this tile is 6 cyphers, and the quotient is 3125, but there must be 6 decimals in the quotient, as there are 6 in the dividead and none in the divisor; I therefore prefix two cyphers to the left hand thereof as before directed.
- \* Example 4. What is the decimal fraction of a year for 73 days?—Anfaver .2, equal to 305. 365. 365.730(.2)
- Cafe 2. To find the value of a decimal fraction in money, weight, or measure.
- \*Rule. 'Multiply the decimal fraction by the number of parts of the next inferior denomination, and from the product cut off as many figures from the right hand fide as there are decimal places in the fraction.

Then multiply these figures so separated on the right hand by the number of parts of the next inscrior denomination, and from the product cut off as many figures as this saft soultiplicand has decimal places, as before.

Proceed in the same manner through all the denominations, then the separated figures on the left hand side will be the answer.

Example 1. What is the value of . 564 of a pound ferling?

Here I multiply the given decimal by ao, the number of parts of the next lets denomination, viz. shillings, and from the product I separate the three sigmes on the right hand, also, as there are three places of decimals in the given number.

I then multiply these separated figures 380 by 18, and from the product 3360. I separate the three first figures 360, as before, to be multiplied by the parts of the next denomination, viz. 4; then the figures standing on the lest hand of these separated figures will be the answer.—111.33d.

The same rule serves to discover the value of any other integers, having regard to the number of parts contained in each inferior denomination.

Thus to find the value of a decimal fraction of a pound troy, I first multiply the fraction by 13 to find the ounces, then the separated sigures by 30 to find the pennyweights, and lastly by 34 to discover the grains.

28.3. What is the value of .6s of a ton of wine?—

Coje 3. To find the value of a decimal of a pound fletling, by infpection.

Rele. Double the first figure of the decimal on the left hand for shiftings; and it the next figure be 5, or above 5, add a shifting more to it; then call the figures in the second and third places farthings (after deducting 5 from the second figure it necessary), and if the number of farthings be above is above 1, and if above 37 above 3. The other figures in the fraction, if more, are neglected.

Example 1. Find the value of .564 of a pound by inspection.

Here I take the double of 5, the first figure, for shillings, which is 10, also I shilling more for the 5 contained in the 6, and the remaining 14 (viz. I in the 6, and 4) I consider as farthings, abating I because they are above 18, which make 3½d.: thus the decimal .564 of a pound is 111.3½d. as may be seen in Case 4.

20. s. Find the value of .7880 of a pound by inspection.

—Assure 14. od.

Ls. 3. Find the value of .24789 of a pound by inspection.

—Answer 22. 1214.

Cafe 4. To find the decimal fraction of a pound equal to any given number of shillings and pence.

Rule. Write half the greatest even number of shillings for the first figure in the decimal, and the number of farthings in the pence and farthings for the second and third figures, observing to add 5 more to the second figure, if the number of shillings be odd; also add x more to the third figure, if the farthings exceed 12, and add x if they exceed 37.

Estample 1. Find the decimal fraction of a pound equal to 11s, 32d.

Here for the 11s. I take  $\frac{1}{2}$  of the next greatest even number, which is 5, for the first figure of the decimal, and for the odd For the odd shilling
For the 3\frac{1}{4}

failling, place 5 to be added to the fecond figure; then for the 3 d. I take 14 to be added to the fecond and third numbers, as there are 13 farthings in 3 d. and 1 is added, as the farthings are above 18; thus, the decimal is .564 of a pound.

Lu. s. Find the decimal equal to 18s. 4\frac{1}{2}d.\to Anfwer .919.

Lu. 3. Find the decimal equal to 17s. 6\frac{1}{2}d.\to Anfwer .878.

Vol. I.

Ll

SECT.

#### SECT. II.

#### OF ADDITION OF DECIMALS.

Approximated in the fame manters, except in the dispofilm of the figures.

Rule. Place the figures exactly under each other, according to the value of their places, that is, the whole numbers (if any) under each other, as in addition of whole numbers, and the fractions are also to be placed according to their values, viz. primes under primes, seconds under founds, and

Then find their fum as in whole numbers, and point off as many places for decimals as are equal to the greatest number of decimal places in any of the given numbers.

Enample 1. What is the fam of \$2.5709, \$.63, \$445.001, \$.071, .00756?

Here the numbers are olded together like

whole numbers, and the number of places

pointed off for decimals are r, equal to the

greatest number of decimal places in any of
the green numbers. The figures on the left

hand of the decimal point are whole numbers of integers.

### More Examples.

2.211	22.179	754.010
84/008	.53	.150
.185	317119	2.24
74002	41.2278	118 91
11.11.111.7	112.00%	y Mais
211.4492	175 7544	347 2478

#### SECT. III.

#### OF AUSTRACTION OF DECIMALS.

DECIMAL fractions are subtracted in the same manner as whole numbers, but the numbers are placed and the decimals pointed off according to the rule given in the foregoing section.

Example 2. What is the difference of \$47.0789 and \$746.805738?

Here the uppermost number confists of 6 places of decimals, wherefore the remainder fought must have as many decimal places; in avery other respect it is wrought like subtraction of whole numbers.

#### Examples.

50.0198	988,12004	3.7031
14-159738	400 003	.008197
5.889468	528.11804	3.700-03

#### SECT. IV.

#### OF MULTIPLICATION OF DECIMALS.

RULE. Multiply the given numbers one by the other, as in whole numbers.

Then point off as many figures for decimals as there are decimal places in both the numbers; but if there be not formany places in the product, as many cyphers must be presented on the left hand thereof as will make up the number of decimal places required.

Lle

Example 1. Multiply 2.03271 by .0056.

In this example the number of decim legisters in both the multiplier and multiplicand is 9; but the product confider of only 8 figures, therefore I must prefix one cypher on the left hand thereof, which makes the true product.

<b>8.</b> 031
1919(
.011383

### Examples.

\$7.0\$943 4.300\$6
\$40 58860 \$10882 900
10811779
216.23195 48960

43970
154 39340
1 54 303 60 1983 900 6013 08
88172 6
-06924 85980

Thus it appears that in multiplication of decimal fracti there is no necessity for placing those figures of the same viunder each other, as in the two foregoing rules.

#### SECT. V.

#### OF DIVISION OF DECIMALS.

This rule is also performed as division of whole numb but from the quotient point off as many figures for decir as the decimal places in the dividend exceed those in divisor. But if the places in the quotient be not so man should be pointed off for decimals, as many cyphers must placed on the left hand as necessary.

<sup>\*</sup> There is a contracted method of working both this and following rule given by many writers on arithmetic. They are, hever, not very fimple, and may very well be superfeded, by omit forms of the decimals in both numbers, and working according to general rule.

If at any time there be a remainder, and if it be required to have an answer to a greater degree of exactness, as many cyphers may be affixed to the right hand of the dividend as is thought proper.

Engaph 1, Divide 1836.88305 by 23.15.

quotient.

83.15)1836.88395(79.347 1680 S 416 38 108 35 In this example there are 8 033 three more decimal places in the dividend than in the 9860 divifor; there must therefore ibeoc be three decimals in the

Eramoles.

	i dolo i oo i
2	3
146)\$7.0084(.1849	.1087)478.0000(4595
146	410 8
18 40	61 80
21 68	51.35
788	9859
584	9 #43
1384	6070
1314	5135
	915
L.t.	

In the fecond example there are 4 decimal places in the dividend, and none in the divisor, therefore there must be 4 places of decimals in the quotient.

And in the third example as the number of decimal places in the divisor and dividend are equal, being 4 in each, there and be no decimals in the quotient.

Every other rule in arithmetic may be performed by decimal fractions as well as by whole numbers, as the same rule serves for both; thus in the rule of three direct in decimals. the second and third numbers are multiplied together for a dividend, and the first number is the divisor as in whole numbers; and the like may be observed of every other rule.

CHAP.

# CHAP. V.

#### SECT. I.

#### THE WATURE OF THE PUBLIC STOCKS.

THE public flocks of Great Britain is an invention in imitation of the flate of Florence, which, in the year 1344, owing 60,000L and being unable to pay the principal, converted the debt into a public flock, transferable from one individual to another, with interest at 5 per cent.: these public flocks were called a hank or mount, and the prices varied according to the state of public affairs.

In imitation of this, foon after the revolution in Great Britain, the expenses of settling the new establishment, carrying on long wars on the Continent for reducing the French monarchy, securing the Dutch barrier, settling the Spanish succession, &c. increased to such a degree, that it was thought advisable to draw upon posterity, rather than reduce the state by an immediate payment.

It was therefore the policy of ministers of that day to raife a public stock with transferable shares, thus converting the debt into a new species of property, for the security of which Parliament pledged their faith; and this example has been elosely followed ever since.

This fystem laid the foundation of what is called the mational debt, to which every stock-holder is a creditor.





Thus the property in the kingdom in idea has been greatly Increased, compared to that of former times; but if we inquire into the nature of this property, we shall find it exists only in name, in paper, and public faith; but that is fufficient for the public creditor to rely upon, for the pledge is nothing less than the land, the trade, and personal industry of the subject, from which sources the money must arise to pay the interest; in these, therefore, the property of the public creditors does really exist, consequently the value of the land, the trade, and industry of the subject, are diminished in proportion as the debt increases.

To demonstrate this, if a debtor ower 100% the creditor has a demand upon him to that amount, and though he may not call upon him for the principal, yet fo much of the debtor's estate is always transferable to the creditor: and the fame principle holds good with regard to the public creditor.

Therefore the property of every stockholder consists in a certain portion of the national debt.

To pay the interest, and, if required, the principal of this debt, certain taxes are appropriated: these taxes were originally separate and distinct funds, and each of them was a fecurity for a certain fum advanced; they were afterwards united together in three capital funds, which are the principal funds of any account, called the general fund, the aggregate fund, and South Sea fund; and the funds thus united together are become mutual recurities for each other, and the whole produce of them liable to pay the interest charged upon each.

The furpluffes of these three funds, over and above the interest charged upon them, are directed to be at the dispofal of the Parliament, and are usually called the firking. fund, because originally defigued to reduce the national debt: to this have late y been added feveral other duties granted. id later years.

This finking fund, with the other duties added thereto, is the last refort of the nation, on which must depend all our.

١.,

hopes of discharging our incumbrances. But by a statute passed in the aoth year of Goo. 111. Parliament vested one million annually in commissioners for the reduction of the debr; in which act several provisions are made to prevent this fund from being appropriated to any other purpose at any future time. In consequence of this act 8,200,000/. had been redeemed in February 1792.

Since which period imposts have been applied to the same purpose, particularly the redemption of the land-tax; and several new loans have been opened on different conditions.

#### BECT. II.

#### SIMPLE AND COMPOUND INTEREST.

SIMPLE interest is the allowance made by the borrower of any firm of money to the lender, according to a certain rate per cent, per annum, which is limited by law to 5 per cent, per annum, that is, 5/. for the use of 100/, for one year, and 10/, for the use of it for two years, or 10/, for the use of sool, for one year.

Principal is the fum of money lent.

Interest or rate in the fum agreed upon for the use of the principal.

Awonne is the principal and interest added together ..

<sup>&</sup>quot;In the courts of law interest for money lent is computed for years, quarters in years, and fingle days. But for the interest on public bonds belonging to the flouris Nea and India Companies, and the fecurities of the Hank of England, the time is generally computed in calendar modifies and days, and on Enchanged bills in quarters of a year and days.

#### Simple Interest.

Rule. Questions that concern interest are resolved by the rule of three; thus-

Multiply the principal by the rate of interest, and divide the product by 100, and the quotient will be the interest for one year.

Then multiply the interest for one year by the number of years given, and the product is the interest for that time.

But when parts of a year are given, then find what aliquot part or parts of a year such part is, and take an equivalent part of the interest for one year; or find the interest for such part by the rule of three direct.

Example 1. What is the interest of 245l. 10s. for 2 years 4 months and 50 days, at 31 per cent. per annum?

In this example I first multiply the 2451. row. by the rate per cent. 34, and the product divided by roo quotes 86. row, row, for the interest of one year. Then by the rule of three direct I find the interest for 50 days, which is 16, 30, 646.

And by the rule of practice I find the interest for a years 171, 31, 8d, and also the interest for a months, or one third of the year, 11, 171, 38d, which three added together, the fund is 111, 42, 98d, for the uniwer.

Queflions concerning latered also are resolved by the double rule of three; thus the foregoing example may be wrought, saying, if root, gain 3t. ros. per cent, in 1 year, what will \$45t. ros. gain in a years 4 months and 20 days?

20. s. What is the interest of 4011, for 1 year, at 4 per cent, per annum? - Anfour 181, 81, 941.

My, 3. What is the amount of 3451, for 3 years, at 44 per cent, per mindin? Anti-on 3911, 111, 64.

24. 4. What is the interest of 4111, 101, for 3 months, at 4 per cent, per annum? - Anjour 41. 81, 3\frac{1}{2}d.

29. 5. What is the amount of 2411, for st years, at 42 per cent, per annum !- Anjour about 121, 44.

my, 6. What is the amount of 400 guiness for 4 years 7 months and 25 days, at 4½ per cent, per annum?— Impur 5071. 181-94.

Lu. 7. What is the interest due upon an Exchaquer bill of 1901, at 3\frac{1}{2} per cent, per annum, for \$\frac{1}{2}\$ years and \$67\$ days \$\frac{1}{2} \cdot \langle \langle

#### A TABLE

#### SHEWING

The Sumber of Days from any Day of one Month to the fame Day of another Month.



The rife of this table is, to find how many days are consained from any day of one mouth to the fame day of any officer amount; thus, to find how many days there are from the roun of March to the runh of Officener following. I look an that column which has March at the top, and in that line much has Officher on the left hand, and in the junction of these two sines I find \$14 for the answer.

#### Compound Interest.

Compound intereft is that intereft which arifes from the principal and a former interest taken together as a principal:

[min, if food be put out to interest for any number of years

Min a

at fumple and compound interest, the interest as it srikes is added to the principal, and their fum becomes a new practical; and the interest due upon this is called compound interest.

Rule. Find the amount of the given principal and the first payment of interest, by the rule of simple interest. Then this amount will be the principal for the second payment of interest, which second payment of interest being added to the last amount forms a third principal, and so on through all the payments to the last, always accounting the last amount the principal for the next interest.

Enample 1. What is the amount of \$401. tor, for \$ years at \$ per cent, per annum, compound interest?

first year's principal first year's interest (econd year's principal (econd year's interest
third year's principal third year's interest.
fourth year's principal fourth year's interest
fitth year's principal fitth year's interest the Aupwer,

After finding the first year's interest by the soregoing rule of simple interest, I add it to the principal; thus I have 5671. 101. 6d. for the second year's principal, the interest of which is 281. 71. 641. and which added to its principal gives 5951. 181. 041. for the third year's principal, to which is also added its interest 291. 151. 1041. and the turn 6251, 131. 111. forms a principal for the squith year, which is also added to its interest 311. 51. 841. and the sum 6561, 191. 741, is the principal for the fifth year, which added to the last interest gives 6891, 161, 71, for the answer required.

Le. 2. Wint is the amount of 500. In Lymns, as 22 per sons, per sonne compount amorals — Al. 1.0406.22

La.z. When aster announced antennicotypication symme, a 4 per vant per announce—Administry operations.

#### laveret of Income Fration.

Simple inveres: a also wrongen of netween frattages, as well as so where numbers.

Ena. Milityry the principal the rate, and the time appother and the product will be the interest requires.

Ratio is the fimple immedial in the present the same agreed open; thus the entire

7.	per oeur. i	e av
14		
15		ACC
124		NES NB
5 <u>£</u>		4532
	<del></del>	104
بر الم		545
æ^		105 1055
1.6		206
14		2003
7		107 1075
		45
4		as .
2		.096 .096
10		.1

The lending opposite each rate per cent, is the definal of a point, open to the inscrete of at for a year; it also them the dominal years the inscrete is of the process.

Tana, 203 of a point is the assemble of a point for one year at 3 per cone, semigroupol to 12.3 it also there exist the instability.

interest of any processal for one year, at 5 per cent, is of parts of the principal.

Example 1. What is the interest of 6461, 151, for 3 years,

at 4 per cent, per annum, fimple intereft ?

Here for the 151, in the principal, I take the equivalent fraction 175, as taught in Cafe 4 of reduction of decimal fractions; then multiplying the principal by the ratio, and the product by the number of years, I have 101.61001 for the interest.

Principal Ratio	946.75
Number of years	33.8700
Pounds	101.0100
Shillings	12 2000
Pence	£.4000
Farthings	1,6000

Then I find the value of the decimal .6:00 in shillings and pence, by the rule in Case a, of reduction of decimals, and it produces 121.2\frac{1}{2}d.; thus the answer is 1011. 121.2\frac{1}{2}d.

Lu. s. What is the simple interest of \$541. 171. 6d. for 5 years, at 4 per cent, per annum? - Aufwer 501. 191. 6d.

20. 3. What is the simple interest of 1760s, for 21 years, at 41 per cent, per annum?—Answer 1541.

Compound interest is also wrought by decimal fractions.

Rule for which is, to find the amount of 11. for 1 year, at the given rate per cent. Then raife the amount to fuch a power as is expressed by the number of years. Multiply this power by the principal given, and the product will be the amount, from which if the principal is extracted the remainder will be the interest.

Enample 1. What is the compound interest of 5201, for 4 years, at 4 per cent. per annum?



1.04	
1:04	
4 16	
: 5_	
1.06 16	the fecond power of 1.04
1.04	
4 12 6:	
1 0816	
1.1248 64	the third power of 1.04
1.04	
44444 56	
1 12 4864	
1.16 9858 56	the fourth power of 1.04
520	the principal
2 33 971- 120	
58 44, 2428 0	
606.9 2045 126	the whole amount
52 0	_
86.32645 120	Influer, or interest required.
	_

In this example I ratio the amount of 11 for 1 year, 1004, to the fourth power, and multiplying the power by the game principal, the product in 602/32645120 for the whole amount of principal and interest, and interesting the principal therefrom, the remainder in 88/32645120 or 88% 61.62d.

Du. 2. What is the amount of 450... io 5 years, at 4 per cent, per annum :—Anhor (47), 9: 10/6.

Most writers on compound interest give to have to discover at once the compound interest of any sum for any certain time, at different rates per cents; I finally therefore, give one to show the manner in which they are constructed.

Compound Interest, at 3h per Cent. per Annum, cales without the Loss of a single Fraction, for Twenty Years.

```
F-108747574
      A 8801185615
      040141105011870
     1.18YERBYGERASHYE
      DATASUSANSOYSACSAS
 6th 1.239355320344516645
      .OALUESUEGEEEEEEEE
 7th 1.272279262766273671878
     -D44520774195810098515616
 8th 1.316809036961403750390635
      .046058916191719111161671875
 9th 1.161897141137111881664196575
     047701407161999100847900190625
toth : 416498760611121182512197265624
     .049370956611739276387026904296875
11th 1.449959717141861458900114169931875
     .051098940101500151061504145947165625
tath 1,511068657546361609961628515869140625
     .051887401007111656148656998055419911875
1 3th 1.46394606014348426631028441 1924460446876
     .05473846211237194932-859992987359619140625
14th 1.618694522465856215631145506911920166015625
     .056654308286304967547090092741917205810546875
Egth 1.675348830752161183178235599651837371826#71875
     -058037109076315641411138145987884308013916016616
16th 1.733980039828486824589473845641721679840087890625
     060689611393997038860631584597460258794403076171875
17th 1.794675551222483863450195430239181938634490966796875
     062843644191786935120753690058371367852207183837890645
18th 1.857489195515270798670859120297553306486698150634767625
     .0650121218430344779534800692104143657270344352722167966
roth 1.92250131735830627661433918950796767221373258590698241185
     .06718754610754068468185187163277886851748064050674438476
20th 1.98978886346584596130619106114074654074121322641372680664
```

The foregoing table thews the amount of in principal as 3½ per cent, per amount, compound interest, for my number of years not exceeding 20: thus, to find the amount of its for 15 years, I feek in the table in the first line of the lifeteenth year, and the answer is \$1.675344, Sec. equal to 14.131.6d.

Though the table be formed only far 1/2 principal, yet questions that concern 10/2 tool. 1000/2 or any multiple of 10, may be readily answered by it, by only removing the decimal point as many places further towards the right hand as the pounds principal contain cyphers: thus, to find the amount of 10/2 for 15 years at 3½ per cent. compared imporest, I place the decimal point one place farther towards the right hand, and the answer is £16-7-53, fac. or 16/2 15/2 of 1/2 and for 100/2 the answer is £16-7-5348, fits or 16-7/2 tags fight inspection, for.

#### The Confirmation of the Table.

The foregoing table, and all others of the fame insture, are formed by multiplying the principal by the ratio, and the product gives the fample interest for one year, which added to the principal, the sum is the amount or principal for the next year; which is to be again multiplied by the ratio, and the product again added to the last principal for a new principal, &c.: thus, in the foregoing table, I multiply the principal rile by 1035, the ratio at 3½ per cent, and the product is 1035, for the interest for one year, which added to its principal sile is 1.035 for the second year's principal, which is again multiplied by the ratio, and the product is 1.036225, which is again added to its principal 1.035, and the sum is 1071225 for the principal for the third year, &c.

In forming tables of compound interest, it is sufficient, in general, if there be only three places of decimals, which will give the answer to a fartning.

Vol. I. Na SECT.

#### SECT. III.

#### OF DISCOUNT OR REVERSION.

Dracount is that allowance which is made for the payment of any fum before it is due, according to a certain rate per cent.

Difcount may be wrought either by whole numbers or declinal fractions. 3

The prefent worth of any sum which is due some time hence is that sum which if put to interest for that time, at the same rate per cent, will amount to the sum or debt then due, whether the interest be simple or compound. Discount is wrought by the rule of three.

Rub. As the amount of 100h at the given rate and time is to 100h so is the sum given to the present worth. Then subtract the present worth from the given sum, and the remainder is the discount required.

Or, as the amount of tool, at the given rate and time, is to the interest of tool, for that time, so is the given turn to the discount required.

Example 1. What is the discount of 5731, 151, due 3 years hence, at 4\frac{1}{2} per cent, per annum, simple interest?

In this example, the amount of 100% for 3 years, at 4½ per cent, is made the first number in the rule of three direct, the interest for the 100% for that time, at that rate per cent, is the second number; and the given sum, whose discount is required, is the third number; and the fourth number is the answer.—68% 4x. 102%.

#### Discount by Decimals.

Rule. As the amount of 11. for the given time, at the given rate, is to 11. to is the interest of the debt for the same time to the discount required.

Example 1. What is the discount of \$734, 154, due 3 years bence, at 41 per cent. per annum?

Nns

68.643, equal to 68/. 41. 108d. the Aufwir.

In this example, I find the amount of 11. for the given time, at the given rate per cent, which is 1.135, and the interest of the debt for the given time, at the given rate per cent, is 77.4565. I therefore divide this interest of the debt by the amount (as it is the second number of the rule), and the quotient is 68.643, or 68/. 41, 102d.

Qu. c. What is the discount of 1401l. 121. for 10 months, at 31 per cent. per annum?—Anfauer 43l. 161. 11d.

20.3. What is the prefent worth of 75% due 15 months hence, at 5 per cent. per annum, fimple interest?—Anfewer 70% 111.94.

Luckims

<sup>\*</sup> Discount is that allowance required for paying a debt before it becomes due, and is tounded upon this supposition, that the debtor paying a turn of money before it is due lake that intend which the money would otherwise gain him from the time of paying it till it is due, and consequently the orestor has that advantage; therefore it is plain, that the heach's from discharging the debt before it is due, by a profest payment, should be the fame as employing the whole turn at interest till it becomes due; for it the discount he put out so interest the

Questions concerning the laying and folling of Stock.

Example 1. What is the purchase of 2200, 100, Bank Stock, at 105 per cent.?

\$\begin{align\*} \begin{align\*} \begi

Arfum.

the given time, its amount will be the interest of the whole debt for the fame time.

In the method of discounting bills bankers commit a great error, for they reckon the interest of the sum drawn for from the time the bill is discounted till it becomes due, including the days of grace; thus they take the interest instead of the discount, and make it more than it should be.

To make this more plain: -- A had a bond of 1000/ due 1 year hence, which he offers to B to discount for him at 4 per cent. 1 B, in imitation of the cuftom of bankers, aiked A 50/ to different the bill; but, tays A. god, is the interest of toook for I year, at 5 per cent, therefore who is to have the interest of the 50% you or 1? If you will return me the interest for the god which is ad tor. I will agree to your terms. A added faither, If you will give me as much money for my bond as with the interest will make up 1000% at the year's end, I will deal with you-otherwise not; to which B agreed, and A calculated the interest thus: as 1.05 is to 14, fo is 10004, to 47.019 or 474 120 43d which is the diffount, and which subtracted from 1000/. leaves 951/. 71. 74.1. the present worth.—Thus B got all the money he ought to have; for if B lends out the discount at g per opat. it will bring him just al. 7: 74d. and the amount will be just 50% at the year's end, and supporting A put out the 952% 7s. 7fd at 5 per cent. it will just bring in 47% 12s. 4fd. the money paid in hand to B, and he would have his 1000/. entire at the year's end.

But for goods bought or fold, when payment is made in ready money, without any regard to time, one year's interest of the turn is generally estermed the different.

Here it muß be noted, that in compound interest, if the interest be paid half yearly, it increases the amount to somewhat more than when paid annually; and also if the dispount be subtracted every half year; it makes the reversion somewhat less than when computed annually.

Quellions

Questions of this nature are resolved by the rule of practice: thus, in the foregoing example, I take the principal sum of sasol. 10s. for the price of the Bank stock, at 100s, per cent. and for the other 5 per cent. in the price of the stocks, I take a twentieth part of the above sum 111s. 0s. 6d. and for the remaining & per cent. I take a tenth part of the gl. line, which is 11s. as. 0 dd.; and these three lines added together is the answer.

Lu. s. What is the purchase of 19751. 101. India Rock, a \$134 per cent. ?—Anfwer \$2491. 121.

Le. 3. What is the purchase of 16331. 4s. Bank annuities, at 891 per cent. ?—Asfwer 14591. 13s. 54d.

20.4. What is the purchase of 41091. 121. in the 3 per cent. consolidated Bank annuities, at 55% per cent. ?—Anfwer 226.81.3%d.

# CHAP. VI.

## Or MERCHANTS ACCOUNTS.

#### SECT. 1.

OF BOOK-KEEPING THE ITALIAN WAY; OR, DOUBLE ENTRY.

THERE are several books used by mercantile which the principal are the scaffe-book, the journal, bedger. These books are generally used by all

bufine(s) I shall therefore give an example of the use of each of them.

## Of the Waste-Book.

This book, by some called the day-book, is used to note down whatever occurs in the way of trade, as buying, felling, paying, receiving, delivering, &c. &c. without omitting any one thing.

This book has one marginal line on the left hand, and three lines for pounds, shillings, and pence, on the right hand; the day of the month and the date of the year are interted in the middle of the page.

#### Of the Journal.

Every thing which is written in the waste-book must be transcribed into the journal in the proper mercantile terms, and in a fairer hand; and every article is to be set down according to the order of time, without any intermission, to make the book of more validity in case of any controverty or dispute.

In this book every article bought or fold is diffinguished by the name of debtor or creditor, and to this book recourse must be had for the particulars of any account.

In the journal, the day of the month is also placed in the middle of the page; it is ruled with three lines, for pounds, failings, and pence, as the waite-book is, and one, and sometimes two marginal lines on the left-hand, to refer to the ledger.

# Of the Ledger.

Fvery article is posted into this book from the journal, but in short, in one line; every lest-hand page of this book is called the debtor page, and each right-hand page the creditor.

ereditor. Intery debter page must have a creditor page of the tame number; thus, the articles or pertons which are sailed the debters (in the mercantile pluste) must be entered on a page of the time number with their called the creditions.

The day of the month, in this book, is fet in a narrow column on the left hand; at the top of each page is the name, the place of residence, and the year of our Lord.

I that give a few examples of the nie of each of their books; but it mult first be observed, that in the waste-book every article is written down in ordinary plain language, and entering the same articles into the journal is nothing more than the tetting them down in the mercanide phraie, diffusquishing each person or article by the name of debtor or creditor, sor which the following rule must be strictly observed.

All things received, or the receiver, are debutes to the delivered, or the deliverer.

## Examples of the Up of the Hade Roak.

Baught of Henry Sa	il ad, 1803. nih, of Cheaptide, 1 an 62. per vard, to	on yards be part	
in 4 months	<del></del>	-	2 10
iold to John Jones,	bound to shing be	cloth, at	1.5
this per yard, to b	edinour o ur bied ×		0 8
Bought of William \	Nulliams, rente		1.1
of lugar, at 1 . 18:	. 141 641	13	
thought of John Edi	naide, Collina	- 40	1 4
ten, at so, per the	4.15	0	1 -1
Ť		A 9	181

Jone nat 1 mily.	
April od, 1804.  Then delite to Henry Smith, 100 rose for the 100 varies of a code por road, to be paid in 3 months.  The force delication to broad cloth for an paids, at 180 per yard, to pur in 6 months.	]_
at 19s. per yard, to pay in 6 months	-

	Lisbon sugar debtor	to W	illiam Wi	illiame	6	£.   s.	d.
	1cwt, at 11. 181. per Green tea debtor to						0
3	at s. per lb.	—		ACM X	- J	15	0

In the first of these examples I make Irish linen the debtor, as that is the article received, and Henry Smith creditor, as he is the deliverer.

In the second example John Jones is the debtor, as he is the receiver, and broad cloth the creditor. The same may be observed in all the other examples which follow.

Thus an experienced person may keep a journal without a waste-book, as they both import the same thing.

I shall, however, give a few more examples of each: and first the form of an inventory, as that is always taken down.

#### Waste-Book.

#### London, January 1st, 1803.

An inventory of all the money, goods, and debts, belonging to me, A. B. of London, merchant: viz.

In cash In Canary w In French b In Florence In 1000 ells per ell Due from J	randy oil of Irith lind —		116	9 13 0	3			
hand		— —	. 50	0		6292	1	5
puncheon pay in 6 n	January 20, 1803.  Received from Benjamin Hughes, in Jamaica, 50 puncheons of rum, at 18/. per puncheon, to pay in 6 months — 900 of						0	
Vol. L		Oo				Jan	uar	7

January 30, 1803.	4.	1.1	ď.
Bought of Henry Jones, 20 yards of broad cloth, at 171.6d. per yard  Bought 20 yards of ferge, at 31.6d. per yard, to pay in 6 months  3 10	21	0	0
February 3, 1803. Sold to Henry Brown 20 gallons of rum, at 8s. per gallon, in 3 months	8	0	0
February 4, 1803. Received of George Jones 1001. 101. due upon bonds	100	10	0
March 4, 1803. Paid to Thomas Williamson 501. due by note of my hand	50	0	0
March 5, 1803.  Bought of John Edwards 2 pipes of Madeira, at 301. per pipe, to pay in 3 months		0	0
March 6, 1803.  Sold to Henry Williams 40 gallons of brandy, at 120 per gallon, to pay in 6 months	24	0	0
March 6, 1863.  Bought of John Thomas, 12 purcheons of Hollands, at 15% per puncheon, 15 be paid in 9 months		0	0
March 6, 1803.  Bought 2 pieces of mullio, at 4/, per piece, for ready money	8	0	

## Journal.

	Inventory, &c. London, January 1, 18	103.		
š	Sundry accounts Dr. to flock £6292 1 5	_	5-	d.
Ĭ	Cash - 4250 5 0		Ì	
	Canary wine - 1124 0 10			
	French brandy — 526 13 3			
	Florence oil — — g24 o o			
	1000 ells of Irish linen, at 2s. 4d.			
•	per ell — — 116 13 4			
ŧ	Note of hand of John Smith 50 0 c	6000		
-		6292		_ 5.
3	January 20, 1803. Rum Dr. to Benjamin Hughes, in Jamaica, for		- 1	
7	50 puncheous, at 18% per puncheon, to pay in		- 1	
	6 months — — —	900	0	O
	January 30, 1803.	العجز .	Ĭ	•
10				
• •	Broad cloth, for 20 yards, at 171. 6d.			
	per yard —			
	Serge, for 20 yards, at 3s. 6d. per			
	yard, to pay in 6 months — 3 10			
_		21	0	0
	February 3, 1803		١	
+	Henry Brown Dr. to rum, for 20 gallons, at 8s			
_	per gallon, to pay in 3 months	8	0	
	February 4, 1803.			
.; ;	Cash Dr. to George Jones, for 1001, 101. due			
_	upon bonds — — -	100	10	_0
<b>2</b> 3	March 4, 1803.			
14	Thomas Williamson Dr. to cash, for 501. due by note of hand	-	0	0
•				
3.4	March 5, 1803. Madeira Dr. to John Edwards, for 2 pipes, at			
13	30% per pipe, to pay in 3 months		0	0
-	March 6, 1803	-		-
34	Henry Williams Dr. to brandy, for 40 gallons,			
,,	at 12s, per gallen, to pay in 6 months	24	0	0
_	March 6 1803.			_
14	Hollands Dr. to John Thomas, for 12 puncheons,			
- ,	to pay in 9 months — — —	180	0	0
•	March 6, 1803.			_
13	Muslin Dr. to cash, for 2 pieces, at 41. per piece	. 8	0	0
,	O o s	I	.edg	cr.

,	4 4 4 4	10   de m 14	0000
	15 T 100	957 5	0 6 0 6 0
	4 1 2	21+1	+ + % +
(1)	Per contra.  By fundry accounts  By profit and lofs gained —	Per contra By fundity secours paid this month By fundity accounts paid this month By fundity accounts paid this month By balance remaining on band	Per contra Cr. Piper. Mt.  18y Thomas Jones, at 50t. per contra pipe contra pi
H	5 m	THE RESERVE THE PARTY OF THE PA	0 0 H W
	1803 Jan. 17 Feb. 28	Jan. 31 Feb. 28	Pab 1 Ba
	The second second	00  0	000
	- m 40 1 80	4.0 1.0	0.00
	6920 5 1 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0.00
	6613 6920 5 700618	\$ 100 100 100 100 100 100 100 100 100 100	4004
	fock 3 69.20 5	\$ 100 100 100 100 100 100 100 100 100 100	4884
	f my flock 3 6920 5	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	Ce of my flock 3 6920 5	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
•	foduce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	Dr. 66,13 ett produce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	Counts — B6 13 he nett produce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	Dr. 66,13 ce the neut produce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	fundry accounts 86,13 balance the nett produce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	To fundry accounts  To balance the nett produce of my flock 3 6920 6	\$ 100 100 100 100 100 100 100 100 100 100	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	Cath Dr. Cath Bolt To fundry accounts BR To balance the nett produce of my flock 3 bases Brown Brook 3 bases BR To balance the nett produce of my flock 3 bases BR To balance the nett produce th	Cath  To flock — 1450 ff  To fundry accounts received this month	Dr. 19 Mr. 18 1 1114 9 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
(1)	1803 Cath Dr. 1 To fundry accounts 86,13 Feb. 28 R To balance the nett produce of my flock 3 6940 Feb. 28 R To balance the nett produce the nett produc	\$ 100 100 100 100 100 100 100 100 100 100	Dr. Pip Mr. 1 40l. 31. 24d. per   p. Mr. 1 40l. 32. 24d. per   1.28   1 B. 1 1114 9 1 4 50l. per pipe

_		0	P MI	RCHAI	OA STE	OUNTS	•	291
(*)	Cr. Pres. Mt.	Perchena — 0.30 × 244 0 0 per perchena x 434 10 0 — 1/A B × 304 10 0		Jan. 3 2 By John Jones, at 261, per jar   4   1A   3 104, c   0	- 4   1 A 3 120 0 0 0 121 0 0 0 0 0 0 0 0 0 0 0 0 0	Jan. 7 4 By John Edwards, at 3s. per	the Thomas, at 21. 64, per 500 CD 5, 62.10	For contractive in fall — C. 65000
	1863 102 2 201	<u> </u>		Jap 3	ă.	Jan. 7, 494	1	
		m 6\	0      <u>0</u>	0 0 712		**		0 0 0
		37 16	01 + C	7	-	4 11.911		2 2
	A = =	¥   1   1   1   1   1   1   1   1   1   1		Je Wi.		Dr. E't. Wk. Irood BE. r		Ä
(*)	1803   French brandy P. Jan. 1 To foot, se 40. 104.34. per	To profit and lofs		Jan. 1 To floch, at 182 per jar		Inch linen Jan. 1 170 flock, at 21. 44. per ell		John Smith Jan. 1 1 To flock, by none of head
•	itos.			i di		Jan. 1		į

Dr. 1   L.   L.   L.   all all all all all all all all all a	Par Mr.  For Mr.  Jan. 22 a fly W Janes, attgl per panelston  10 0 0 2 a fly John Williams, at 2d, per punchena  Punchena  R fly ishneet unfall, at 2d, per punchena  R fly ishneet unfall, at 184 per punchena	- 96. Fr.	D. 18 13 G Feb. 3 a By Heavy Brown, 123 3 8 10 G	1 1
Rum ( )	Jan. 2. (To Benjamin Highes, at 187 per   purcheon, to paying mostis   AB   Profit and lots gained by this account.	Sundris, pr. 170 Henry Jones, viz. To Broad cloth, 22 yds, at 170 ff per yd. To ferge, 22 yards, at 50 eff per ydd, to jayin 5 mont, 8 To jayin 5 mont, 8 To profit and loss galacelly, this account	Henry Brown Garlen, to pay in 3 months	Fcb. 4 7 To George Jones, due on bond

1803   Per contra C.	4 <del>-1</del>	f, By balance, remaining unfold   1/0 H   1/1 C   C   C   C   C   C   C   C   C   C	Estion  For contra  C.  For contra  For contra	60	Mar. 6 2 By mulita unfold, at 4/ per pree 2,02 2 8 0 0
1803	Nat.		Mar. 6	Nar. 6	Mar. S
.: <b>::</b> ::::	0 1 0 0	<del>                                    </del>	<del>نید</del> بد. ا		0 0 1
- Z	6   0 0 8   0 0		., -		·
S	8.   26.4	22	11		a • i
· ,			(4)		
Ďí.		, ,	17 1 V	1	ali i i dalif ama menderi
	1 3 3	33		<u> </u>	. O
A	P. Constitution		, a	E I	P.c. Mt
A	Dr.		, c	E I	P.c. W1
	Dr. Dr. C. Syrthis sectoral	7	, c	E I	'   '
	of hand  Dr.  p. z. p.º es  guard by this account		, c	E I	'   '
	note of han 1 Dr.  Trick, 2 pi es Dr.  Linguated by this account		, c	E I	'   '
	ta note of han 1  ta  Exercise a pires  Far in guard by this account		, c	E I	'   '
	cafe, on note of hand  Addeira  John Edwards, a pices  proof and the generally this account		, c	E I	'   '
	To cafe, on note of hand  Madeira  To John Edwards, a pires  To proct and its genetaby this account	Henry W. Jams Jr.	, c	E I	'   '
( † ) admilianton	dwards, a pires		E E E E E E E E E E E E E E E E E E E	Thomas, at 15% per 118	
	To cafe, on note of hand  Madeira  To John Edwards, 2 pices  To pront and the general by this account		, c	E I	

Every article in the journal is posted into the ledger, and shoft persons or things to which the other party is said to be debtor are entered on the debtor side, or less hand page, with the word To; and those persons or things belonging to the same account, to which the other party is said to be creditor, are entered on the right-hand side, or creditor page, with the word Mr, as may be seen in the foregoing examples.

The figures in the narrow column in the ledger after the day of the month, both in the debtor and creditor fide, there what pages in the journal the entries are taken from; and the letter R in these columns fignifies the remainder on the balance of that particular account. Those figures in the sarrow column on the debtor fide, before the money, there in what page of the ledger that entry stands on the creditor fide; and the figures in the like column on the creditor fide them what page of the ledger the entry stands in on the debtor fide.

Each delitor page of the ledger must be numbered the same as that part of the ledger where the creditors to the same accounts are entered.

The finall figures at the beginning of each journal entry flow in what pages of the ledger tuch entry is polled; the upper figure thews the debtor fide, and the lower figure the creditor.

Thete three books are or may be uted by every man of butinets, in any line whatever, as well as by the merchant.

There are feveral other books used by merchants, as follows:

birth, the deletest, in which is entered the day whereon all turns become due, whether to be paid or to be received, by bills of exchange, notes, bonds, &c. that by comparing receipts and payments together, providen may be made in time.

See and

Second, the cash-hook, which is ruled and paged like the ledger, wherein all receipts of money are entered on the left-hand folio, and all payments on the right, with the day of the month (the year being fet on the top of the page), for whose account the money was received or paid; and the total debit or credit on each side is usually once a month posted into the ledger to the account of cash therein, with references in the cash-book to the several folios in the ledger.

Third, the invoices of goods thipped, and also of goods received from abroad, which must always be entered on the left-hand side, leaving the right-hand side blank; and on the advice of the sale of goods which are sent abroad, and also on the sale of goods received from abroad; which are to be entered on the blank or right side. The use of this book is, to save the journal from any erasures, which would be amavoidable in taking invoices of the several goods received, sent, or fold.

Fourth, the receipt-hook, wherein are given receipts for money paids the receipt to be given by the receivers for whose account or use, or for what it is received, and the day of the month, and date of the year.

Fifth, the book of charges of merchandile, wherein are entered all the charges and expendes of any goods bought, fold, received, or thipped; such as porteinge, wharfage, warehouse-room, &c. &c; the whole account is once a month transferred into the cash-book, on the credito side, with references to the book of charges; and the same in the debtor side on the same account in the leager.

Sixth, the book of lampelold expenses, wherein are entered the charges of what is expended in houtekeeping, such as apparel, houte-rent, servants wages, pocket expenses, victuals, &c. &c.: this is once a month summed up, and carried to the cash-shook.

Seventh, the letter-back, which contains copies of all letters fent or received from abroad, and also inland letters.

Vol. I. Pp Laftly,

Lattly, the note or memorandum book, wherein are interted affairs that occur, for the help of memory, and of great wie where there is a multiplicity of business.

#### General Rules.

The principal rule in book-keeping has already been delivered, in the beginning of this fection, viz. To make all things received or the receiver debtor to the delivered or the deliverers. But I shall add a few more rules, which may ferve to exemplify the foregoing rule more fully.

First, flack is debtor to profit and loss for all money received and nothing given for it; as the profit of every commodity in the trade, legacies left, money received with an apprentice, &c. &c.

Per contra oreditor, by profit and loft, for all money paid and nothing received for it; as the discount of money received before due, lofs of goods uninfured, lofs by accidents, abatement by composition, household expenses, gifts, &c. &c.

becouldy, for money received make cash debtor to the party that paid it, and the party creditor by cash.

Thirdly, for money paid make the receiver debtor to caft, and eath creditor by the party.

Fourthly, For goods bought for ready money make the goods debtor to call, and call creditor by the goods.

Fitthly, for goods fold for ready money make caffi debtor to the goods, and goods creditor by caffi.

Sixthly, goods bought on credit, make the goods debror to the feller, and the feller creditor by the goods.

beventhly, goods fold upon credit just the contrary; that is, the perion who buys them must be debtor to the goods, and the goods creditor by the party.

Eighthly, for goods bought part for ready money and the sell on credit; first make the goods debtor to the party for the whole; secondly, make the party debtor to cash for the money paid him in part of these goods, and cash creditor by the party.

Ninthly,

Ninthly, for goods fold part for ready money and the rest on credit; first make the party debtor to the goods for the whole, and the goods creditor; secondly, make casta debtor to the party for the money received of him in part of these goods, and the party creditor.

Tenthly, when discount is allowed for money paid before it is due, make the party who receives the money debtor to cash for so much as is paid him, and stock debtor to profit and loss for the discount.

## To remove an Account full written to another Folio.

First, if the debtor side be more than the creditor, make the old account creditor by the new; but if the creditor side be more than the debtor, make the old account debtor to the new, and the new account creditor by the old for the remaining sum.

Secondly, in an account of company, wherein there is placed more received of another than his flock amounts to, as much must be added to the debtor side as there is placed on the creditor side, in order that in the new account there may be as much debit as was put in, and as much credit as was received.

Thirdly, in all accounts of merchandife, the gain or loss must be entered before the old account is made creditor by the new, and the new debtor to the old.

#### To balance or clear an Account when full written.

Find the sum of the debtor and creditor side, and the difference place to its opposite: thus, if the creditor side exceed the debtor, then she line is to be written in the old account to balance on the debtor side, to answer the line on the creditor side in the new account.

Pp 3

How

# How to lalance the Account at the Year's End, and thereby to know the State of Affairs.

First, even the account of cash and bear the nett remainder to balance debtor.

Secondly, find the value of all goods bought and fold; and for goods bought which remain unfold, value them at prime coft, and hear the nett remainder to balance debtor.

Thirdly, find what all the goods cost which are bought, and also how much they were fold for, and bear the next gain or loss to the account of profit and loss.

Fourthly, even all personal accounts with your debtors and creditors in the order in which they are wrote down, and bear the nett remainder to balance, &c.

Fifthly, even all voyages and factors accounts wherein there is either gain or loss, and bear the nett gain or loss to the account of profit and loss, and the goods unfold to balance.

Sixthly, even the account of profit and lofs, and bear the nett remainder to flock.

Seventhly, even the flock, and bear the nett remainder to balance creditor.

Lastly, find the sum of both the debtor and creditor sides of the balance, and if they be both alike the account has been kept truly, otherwise not.

If the debtor and creditor fides of the balance be not both alike there is an error, which must be found by pricking over the books again, so fee whether every debtor and creditor is entered in the ledger.

Pricking over the books is comparing every article of the femmal with the fame in the ledger, and marking it thus? and on the second examination thus?, &c.

## The Form of an Invoice.

#### March 6, 1803.

Invoice of rooque, of wheat in facks, shipped on board the good ship Neptune. William Brown master, and configued to Henry Jones of Jamaica, for the account and risk of John Dalton and Thomas Edwards of London, merchants, marked and numbered as per margin:

			€.	8.	d.
	100 grs. of wheat, at 12s. per quarter 200 facks, at 1s. cach	1	60	이	0
A DW	200 facks, at is. each —	-	10	0	0
BO	Meterage — —	-	2	o	•
	Meterage — — — Porterage, at 11.64. per quarter	-	7	10	0
No.	Cartage -	-	5	181	4
<b>\$0</b> 100	Lighterage — —	_	3	0	0
	Lighterage — — — — Freight, at as. per quarter		10	어	0
			98	B	4
The	commission on 981. 81. 41. at 1 per cen	t.	່າ	19	ò
	•		99	7	4
		~		_=	=

#### The Form of a Bill of Lading.

Shipped by the grace of God, in good order and well conditioned, by Henry Williams of London, merchant, in and upon the good ship called the Mercury of London, whereof is maker under God for this present voyage John Dickson of London, mariner, and now riding at anchor in the port of London, and by God's grace bound for Antigua; to fay, One bale of Irish linen, and one bale of men's moes, and five hundred pair of filk flockings, No. 3, 4, 7. contents, &c. as per invoice, being marked and numbered as per margin, and are to be delivered in the like good order at the aforefaid place (Antigua), the danger of the fea only excepted, unto Mr. Edward Brown. merchant there, or to his affigns, he or they paying freight for the faid goods, three pieces of eight per cwt. with primage and average accustomed. In witness whereof, the master or purfer purier of the faid flip hath affirmed to three bills of lading, all of this tenour and date, one of which three bills being accomplified the other two to fland void; and to God tend the good flip to her defired port in fafety. Amen.

Dated in London, the 6th of March 1803, infide and contents unknown to Yoke Diskler.

## An Account of a Sale.

#### London, March 6th, 1803.

Account of a fale of two thousand four hundred yards of mullin, two thousand two hundred yards of dimity, two hogheads of rum, five ewt. of sugar, and five hundred pair of cotton slockings, received from on board the suip Maria, Captain Thomas Jones commander, for account of Edward Wills of Jamaica, merchant, is debtor

To porterage of ditto  To commulion of fales  To florage, at 1 per cwt.	£ d. £ d.
To the nett product, bad debta es	scepted - 10 4 B
•	0.0
Per contra . By two thoutand four hundred y	Cr. aids of mullin,
by two thoutand two hundred 32 fold Henry Brest, at 11, 2d, per	varid is \$1 for it.
By two highleads of time, at also, by Henry Jones, for five ewt, of the time, for five in By Henry Williams, for five in	lugar, at 1/, to.
cotton florkings, at 11, 61, per	patt - 1100
	114

Frince excepted, London, 6th March 1803.

Per Joba Smith.

Mud

Most writers on merchants accounts give a variety of examples and rules to inform the learner how to state the feveral articles according to debtor and creditor; but the foregoing examples, and a strict attention to the general rules before delivered, will be sufficient for any ordinary capacity.

## Concerning the Exporting and Importing of Goods.

Goods to be exported must have a bill of entry, in the following form:

In the Maria, Captain Thomas Jones, for Jamaica, John Smith.

Two thousand four hundred yards of multin.
Two thousand two hundred yards of dimity.
Two hogsheads of rum.
Five cwt. of jugar.

Five hundred pair of cotton flockings.

There must be seven of these bills, one of which must be in words at length, the others may be in figures; these bills are entered into books by the clerks of the Custom House. When some goods pay custom and others do not, there shuft be two entries made, one for those which pay custom, and the other for those which do not pay.

#### Importing Goods.

When goods are to be landed from any ship arrived, the entry-book of the Custom House must be searched, to find the names of the ship and the captain, as also the waiters that are to attend the landing of the goods, &c.

The Form of a Bill of Entry inwards.

In the Maria, Captain Thomas Jones, from Jamaica.

Fifty hogheads of fugar.

Twenty bags of cotton.

**Forty** 

Cafe 4. When there is an allowance made for tare, trett, and cloff.

Rab. After the tare and trett are deducted as before, divide the remainder or futtle by 168, and the quotient is the cloff; then subtract the cloff from the suttle, and the remainder is the nett weight.

Example 6. What is the nett weight of 27 bhds. of tobacco, weighing 140cwt. 2qrs. 201b. groß, tare 14lb. per cwt. trett

Cut. qrs. B.

For 14lb. per cwt. tare, divide by 8) 140 a 20 groß

17 a 0 tare

26) 123 0 11

4 2 25 trett

169) 118 1 14 futtle

2 22

117 2 20 nett weight.

24. y. What is the value of 58hhds. of fugar, each hhd. weighing 6cwt. 19r. grofs, at a guinea and a half per cwt. tare 8lb. per cwt. trett and cloff as ufual?—Anf.5051.141.7 d.

## Commission, Brokerage, and Insurance.

Commission is an allowance of a certain sum per cent. to an agent abroad, for buying or selling goods for his principal.

Brokerage is an allowance to a broker for affifting a person in procuring or disposing of goods, as auctioneers, stockbrokers, &c. And the allowance is generally at a certain rate per cent.

Insurance is a premium at so much per cent, given to certain offices or individuals who engage to make good the loss of any ship or merchandise, which may happen from storms, fire, &c. &c.

Rule. Questions concerning these rules are resolved in the same manner as those in simple interest, viz. by multiplying

the principal fum by the rate per cent, and dividing the product by 100.

Example 1. How much is the commission of 5401. 121.6d. at 41 per cent.?

Qu. 2. What is the commission of 1059l. 16s. 10d. at 22 per cent.?—Answer 22l. 16s. 11d.

2x. 3. What is the brokerage of goods fold to the amount of 10171. 5s. 8d. at 14 per cent.?—As/wer 151. 5s. 2d.

2n. 4. What is the infurance of a thip and her cargo, valued at 17862l. 18s. 9d. at 174 per cent. ?—Anfaer 3193l. 3s. 63d.

#### SECT. XXI.

PRECEDENTS OF RECEIPTS, PROMISSORY NOTES, BILLS OF EXCHANGE, BILLS OF DEBT, BILLS OF LADING, BILLS OF PARCELS, &c. WITH THE LAWS CONCERNING THEM.

#### Bills of Parcels.

It is usual in some cases for shopkeepers to deliver to their customers a bill of the articles sold them, with the total value cast up at the bottom; these are called bills of parcels.

Qq 2 A Linen-

Cafe 4. When there is an allowance made for tare, trett, and cloff.

Rule. After the ture and trett are deducted as before, divide the remainder or futtle by 168, and the quotient is the cloff; then fubtract the cloff from the futtle, and the remainder is the nett weight.

Engaple 6. What is the nett weight of solids, of tobacco, weighing 1400wt. sqrs. solb. grais, ture 14th, per cwt. trett as inform?

Cous. qrs. lb.

For 14lb. per cwt. tare, divide by 8)140 s so gross
17 s y taro
20)183 0 11
4 s s5 trett
168)118 1 14 futtle
8 s8
117 s so nett weight.

Qu. y. What is the value of 58hhds. of fugar, each hhd. weighing 6cwt. 1qr. grofs, at a guinea and a half per cwt. fare 81b. per cwt. trutt and cloff as ufual !-- Anf. 5051.141.73d.

Commission, Brokerage, and Insurance.

Commission is an allowance of a certain fum per cent, to an agent abroad, for buying or felling goods for his principal.

Brokerage is an allowance to a broker for affilling a perion in procuring or disposing of grads, as auditoneers, stock-brokers, sec. And the allowance is generally at a certain rate per cent.

Infurance is a premium at fo much per cent, given to certain offices or individuals who engage to make good the lofs of any flip or merchandile, which may happen from florms, fire, &c. &c.,

Rule. Queficing concerning these rules are resolved in the fame manner as those in simple interest, viz. by multiplying

the principal fum by the rate per cent, and dividing the product by 100.

Example to How much is the commission of \$406 tas. 6d. at 44 per cent.?

Qu. s. What is the commission of 10591. 16s. 10d. at s. per cent. 1—Anfour s.31. 16s. 11d.

Let 3. What is the brokerage of goods fold to the amount of 1017/, 51. 8d. at 1 per cent. ?—An/iver 15/, 51. ad.

2n. 4. What is the infurance of a thip and her cargo, valued at 178631. 18s. 9d. at 174 per cent. ? — Anfour 3 1931. 3s. 62d.

#### SECT. XXI.

PRECEDENTS OF RECEIPTS, PROMISSORY NOTES, BILLS OF EXCHANGE, BILLS OF DEST, BILLS OF LADING, BILLS OF PARCELS, &c. WITH THE LAWS CONCERNING THEM.

#### Bilk of Parcels.

It is usual in some cases for shapkeepers to deliver to their sustainers a bill of the articles fold them, with the total value saft up at the bottom; these are called bills of parcels.

# A Linen-draper's Bill.

Mr. Francis,	March 10, 1803.							
	Bought of John Green.							
		s.	J.		L.	ı.	2	
as yards of dowlass	at	ļ	6	per yd.	1	17	6	
30 yards of disper	-	1	6	do.		5	0	
so yards of Holland	_	5	6	do.	5	10	•	
40 yards of Irish cloth	-	4	6	do.	5	0	0	
10 yards of muslin		7	0	do.	3	10	0	
5 yards of cambric	_	15	0	do.	3	0	0	
so yards of printed cotton			6	do.		10	0	
							<del>-</del>	
					<b>(23</b>	18	-6 	
A Woo	llen-dr	арет	's 2	Bill.				
Mr. Wm. Smith,				March 18	, 18	03.		
·	Bought of Henry Jones.							
		· ,.	d.			s.	٨	
17 yards of fine ferge	at	4	0	per yd.	3		0	
18 yards of drugget	-	8	0	do.	7	4	0	
25 yards of fuperfine fearlet		7	6	do.	1	•	6	
r6 yards of fuper black cloth		18	0	do.	14	8	0	
as yards of shalloon		2	0	do.	•	10	0	
17 yards of drab		18	0	do.	15	6	0	
					643	18	<del></del>	
				,	٠ <del>٠ .</del> ) ==		_	
	Hofter	's Bi	u.			_		
Mr. Holmes, March 14, 1803.							•	
Bought of James Richards.								
16 pair of worsted stock		. s.	d. 6	!-	-			
16 pair of do.	ings at			per pair	-	4		
6 pair of black filk do.	-	- 3		do.	8	10		
•		- 14	0	do.	4	4	• '	
•		. 6	0	do.	3	18	•	
8 pair of cotton do.		- 8	0	do.	3	4	0	
4 yards of time flannel	-	- 1	8	per yd.	0	6	•	
					ود ک	-,	-	
				•			<del>-</del>	

Received of Mr. William Morgan. this on of February 1803, fix pounds, for one quartef's rent, due at Christmas last, for my master, Robert Kerr. Per

<u>£6 0 0</u>,

Richard Heath.

Received, February 10th, 1803, of Mr. Samuel Wilkinson, twenty-nine pounds fix shillings, in part of a bill of fixty pounds, due the 3d of May next, to Mr. John Lewis. Per

£29 6 0

Nicholas Manfel.

A Receipt on the Back of a Bill of Exchange.

March 1st, 1803. Received the full contents of the within mentioned, being 500 pieces of eight. Per

500 pieces 8

John Wilson.

#### PROMISSORY NOTES.

I promise to pay to Mr. Edward Brown, or order, the sum of fixty pounds, on the 29th of this instant March. Witness my hand-this 6th day of March 1803.

£60 0 0

Edward Jones.

March 10th, 1803.

I promise to pay to the Honourable the East India Company, or bearer, upon demand, two hundred pounds, for Edward Williams.

£200 0 0

Henry Smith.

March 12th, 1803.

I promise to pay to Mr. Joseph Brown, or order, five months after date, ten pounds ten shillings, for value received.

£10 10 0

William Holmes.

March 14th, 1803.

I promise to pay to Messes. John Edwards and Co. or bearer, the sum of twenty pounds ten shillings, on demand.

£20 10 0

Robert Marian.

A Note

Kereived, January 13th, 1863, of Mr. Ceorge Common, filty-five pounds fixteen faillings and none peace, in part too telesco fold him the 64th of December latt. For

155 16 6

Sumuel Thumpfon.

Received, January 14th, 1804, of the Himmurable link India Company, three hundred and filtern pounds on that-lings, per order, and for the account of Philip Fox. For

£311 10 0

Henjamin Hamilton.

Received, January 16th, 1863, of the Clavernor and Company of the flank of England, one thouland his hundred pounds ten failings, for felf and company. I'm

Z1666 10 6

Hispien Harber.

Received, January 16, 1803, of the Worthipful Company of Grucers, forty-nine pounds fifteen fullings, in full payment, for my father, John Harrison. Yes me,

LAG 16 0

John Harrison, June

Reserved, January 17th, 1814, of Dichard Clarks, Step chamberlain of Landon, the four of fixty pounds, for the also of the Worffipful Company of Johnson, 1881

1. 10 11 11

Rubard Stevens, Clarks

# A Mont gutherer's Mereipt.

Received, Paliciary 7th, 1812, of Mr. Staphen Dicklon, in money, eighteen pointels, and allowed him for land-tax five pointels, and for repairs two pointels, in all twenty-five pointels, in full for half a year's cent due at Christmas laft; I say received for the nic of Thomas Cox, 1644, by virtue of his letter of attention, 1'or

106 0 1

Francis H'ard.

Heraived.

Received of Mr. William Morgan, this 9th of February 1803, fix pounds, for one quarter's rent, due at Christmas last, for my master, Robert Keir. Per

4600.

Richard Heath.

Received, February 10th, 1803, of Mr. Samuel Wilkinfon, twenty-nine pounds fix fhillings, in part of a bill of fixty pounds, due the 3d of May next, to Mr. John Lewis. Per

(24 6 v

Nicholas Manjel.

A Receipt on the Buch of a Bill of Exchange.

March off, 1804. Received the full contents of the within mentioned, being 500 pieces of eight. Per

goo pleans &

John Wilson.

#### PROMISSORY NOTES.

I promife to pay to Mr. Edward Brown, or order, the fum of fixty pounds, on the soth of this inflant March. Witness my hand-this 6th day of March 1801.

¥00 0 0

Edward Joves.

March 10th, 1801.

I promise to pay to the Honourable the East India Company, or bearer, upon demand, two hundred pounds, tor Edward Williams.

Cave e a

Henry Smith

March 19th, 1803.

I promife to pay to Mr. Joseph Brown, or order, five months after date, ten pounds ten fhillings, for value received.

\$10 10 0

William Holmes.

March 14th, 1801.

I promise to pay to Messie, John Edwards and Co. or bearer, the sum of twenty pounds ten shillings, on demand.

610 10 0

Robert Martin.

A Note

#### A Note from two to one.

We or either of us promife to pay to Mr. Robert Stokes, or his order, on demand, twelve pounds ten shillings, for value received. Witness our hands.

/18 10 0

Thomas Williams. Edward Morris.

#### BILLS OF EXCHANGE.

A Bill payable at Sight.

London, March 5th, 1803.

At fight hereof pay Mr. Robert Winds, or his order, the fum of twenty-five pounds, for value received of Edward Mills, and place it to account, as per advice from

To Mr. John Willis, Merchant, High Street, Briftol. Your liumble fervant, John Miller.

Dover, March 13, 1803.

Ten days after fight hereof pay to Mr. Thomas Trust, or his order, fifty pounds ten shillings, and place it to account, as per advice from

To Mr. John Francis, Linen-draper, Cheapfide, London. Your humble fervant, Henry Hill.

Foreign Bills of Exchange.

London, March 6, 1803, for 540 crowns, at 504/l. flerling per crown.

At usance \* pay this my first bill of exchange (my second and third not being yet paid) unto Mr. Henry Brown, or a order, five hundred and forty crowns, at \$6\frac{1}{6}d\$, per crowns for the value received here of Mr. Edward Wills, and place it to account, as per advice from

To Mr. John Edwards, Merchant in Amfferdam. Your humble fervan

<sup>•</sup> Utance between England and France, or Lugland and Hollar and, is one calendar month; between England and Spain, or Portugal, t and months; between England and Italy, three months; and between England and Turkey, four months, &c.
Nantas

Naples, March 18, 1803, for 6404 101.

At three usances pay this my first bill of exchange, unto Mr. John Stocks, or order, fix hundred and forty pounds ten shillings sering, for value received of himself, and place it to account, as per advice from

To Meffre. Bardy and Edwards, Merchants in London. Your humble fervant, John Smith.

Liverpool, March 14, 1803, for 6000 pieces of eight, at 534d. per piece.

At double usance pay this my fourth bill of exchange, unto Mr. John Jervis, or order, fix thousand pieces of eight, Mexico, at-53\frac{1}{4}. Sterling per piece, for value received of Mr. Joseph Hunt, and place it to account, as per advice from To Mr. Matthew Marsh,

Your humble servant,

Merchant in Leghorn.

Henry Edwards.

## A Bill of Debt.

Larry all men by these presents, that I John Briton, of London, merchant, do owe and am indebted unto Henry Haynes, of Southwark, salter, in the sum of sour hundred and forty-nine pounds, of lawful money of Great Britain; which said sum I do hereby promise to pay unto the said Henry Haynes, his heirs, executors, administrators, and assigns, on or before the twenty-sourth day of September next ensuing the date hereof. Witness my hand and seal, this sourteenth say of March 1803.

\*\*John Briton, (18).\*\*

Sealed and delivered William Smith.
An the presence of us, I Thomas Harrison.

#### A Bond.

Know all men by these presents, that I John Drew, of the sparish of St. Giles, in the county of Middlesex, carpenter, are held and firmly bound to Samuel Price, of the city of Westminster, in the county aforesaid, vintuer, in the sum of one hundred posinds, of good and lawful money of Great Britain, to be paid to the said Samuel Price, or to his certain Vol. I. Rr attorney

If a receipt be given in full, though there be a condition annexed to it specifying a former debt between the parties, yet the receipt stands as a receipt in full.

# Of Promiffory Notes and Bills.

A promiffory note is an engagement for a fum of money to be paid at a certain time, or on demand; when the fum is to be paid on demand, it is the prefeatly, and there needs no actual demand; but it is otherwise where the money is in be paid to a third person, or where there is a penalty, for in that case there must be a demand.

A bill is a fingle bond, without any condition. If a person acknowledges himself indebted to another by bill in the sum of fifty pounds, and by the same bill binds himself and his heirs for the payment of the said sum, in a hundred pounds, without inferting the person's name to whom he is bound in the penalty, it shall nevertheless be taken as a bond against him for the said sum and penalty.

If a man intervine a bill these words: I do ever and promise to pay to AB  $_{S}A$  Sec. for the payment subserved I bind inself to CD, Sec. (another person), yet this is a good bill by the words of the first part, and the words obligatory to another person, CD, are yord.

If a man fays in a bill, That I AB had received of CD the fum of viventy pounds, which I provide to pay to EF; or if the bill be, I shall pay to CD 201.; or if it be, I owe to CD 201 to be paid at, Sec.; or, I had of CD 201. Sec.; to be repaid him again; or, I AB do hind myself to CD, that be shall receive 201.—either of these phases binds the drawer of the bill, and constitutes a good bill.

# Of Bills of Exchange.

A bill of exchange is a writing given among merchants and traders for money, and by the credit of the drawer generally

them, or each or either of their heirs, executors, adminifirators, or affigns, shall well and truly pay, or cause to be paid unto the above-named Thomas Smith, his executors, administrators, or affigns, the sum of one thousand pounds, of lawful money of Great Britain, on or before the twenty-fifth day of December next ensuing the date hereof, then this obligation to be void, otherwise to remain in full force and virtue.

#### A Penal Bill.

Know all men by these presents, that I Andrew Jones, of the borough of Southwark, do owe unto Edward Mills, of the parish of St. Clement Danes, Westminster, the sum of one hundred pounds, of lawful money of Great Britain, to be paid unto the said Edward Mills, his executors, administrators, or assigns, on or before the fifth day of November next ensuing the date hereof, for which payment well and truly to be made, I do hereby bind myself, my heirs, executors, administrators, or assigns, to the said Edward Mills, his executors, administrators, or assigns, in two hundred pounds, of like lawful money of Great Britain, firmly by these presents. In witness whereof, &c.

Andrew Jones, (A).

#### Of Receipts.

A receipt is a discharge for money owing, and is a bar to all suits in law and equity. When given in full of all demands, at discharges all debts between the two parties prior to the state thereof.

If a receipt be given, it is good, though no money be paid, except it be obtained by fraud, in which case relief may be had in equity.

A fervant may give a receipt in his own name for his master, if he be accustomed to receive or pay money for his master's use, or a wife may give a receipt for her husband in her own name, and it is equally valid.

If a receipt be given in full, though there has a condition annexed to it specifying a former debt between the parties, yet the receipt fands as a receipt in full.

# Of Promiffing Notes and Bills.

A promitiony note is an engagement for a furn of money to be paid at a certain time, or on demand; when the form is to be paid on demand, it is observable where the money is to be paid to a third perfon, or where there is a penalty, for it that eals there mult be a demand.

A full is a lingle bond, without any condition. If a performacknowledges himfelf indebted to another by bull in the fum of fifty postule, and by the fame bili bonds himfelf and his helts for the payment of the faid fum, in a hundred pounds, without inferting the parlon's name to whom he is bound in the penalty, it fhall nevertheless be taken as a bond againft him for the faid fum and penalty.

If a man intert in a hill the to words I do one and gramife to pay to All god the, for the payment coherent I hind respect to CD, the (another perton), yet time is a good tool toy the words of the first part, and the words of hydroxy to another perton, CD, are word.

If a man lays in a hill, That I All had received of C.D the fun of twenty pounds, which I provide to pay in E.F., or if the hill be, I fhall pay in C.D and, in it is he, I was in C.D and it he paid ut, have in, I had of C.D and, have in he refull him uguing in, I All do hind myfelf in C.D, that he shall receive able wither it these physics hinds the drawer of the hall, and constitutes a grant hill.

# Of Wills of Fachunge.

A full of exchange is a writing given among merchants and tradets for money, said by the chall of the drawer generalized

nerally palles as money a thefe bills are drawn fometimes mayable at fight, tometimes at a certain time. An inland bill of exchange is of the nature of a letter, and is drawn by one merchant upon another in the fame country, as, by AB of Brithol upon C D of London; but a foreign bill of exchange is drawn by a merchant of one country upon a merchant of another country. These foreign bills are of more confequence in the eye of the law; a foreign bill being refused to be accepted, an action may be had against the drawer, and every person who indortes a toreign bill becomes liable to the ...ayment as if he were the drawer, because every indorsement is in the nature of a new bill; but the indorfer is not liable to pay if the drawer can be found; but if the drawer's hand cannot be proved, the accoptor may come upon the laft indorter. If a perton only figns his name at the back of the bill, the acceptor of the bill may fill up the indorfement, or the bare figuature will pais in law for an indorfement.

There is a material difference between a bill of exchange payable to a person or beaver, and one payable to a person or water. A bill payable to a person or beaver is not assignable, so as to enable the acceptor to bring an action if the drawer resuses payment. In a bill payable to AB or beaver, the acceptor may sue in the name of him to whom it is made payable. If a bank bill payable to AB or beaver be lost, and found by a stranger, payment to the stranger will indemnity the Bank, yet AB may have an action of trover against the sinder, but not against any person to whom the sinder has paid it for valuable consideration.—A bill of exchange payable to a person or order may always be assigned, and the acceptor can bring his action in his own name. A bill payable to order is within the custom of merchants, and may be negotiated and assigned by custom.

If a perion accepts a bill, though the date of payment be pall, he cannot return it, but he may bring an action for the money, if the bill be tendered in time.

A fervant cannot accept a bill for his mafter, except there

A bond may be good though it contains false Latin, or false English, or though it be of a doubtful interpretation, as, if A binds himself to B to pay a sum of money to A (whereas it fisould be to B), here the obligation is good, and the followndom void. If a bond be interlined in a place not material, it will not hurt the bond; but if it be in a material part, it will make the bond void. In thort, all bonds, obligstions, bills, promiffory notes, &c. when any doubt arifes, are always interpreted in favour of the party to whom the money is one.

These are the principal legal precedents used by mercantile men, to which I shall add a power or letter of attorney, as being in most general use by all descriptions of people.

# A Letter of Attorney from one, or two, to fettle Accounts and receive Money.

Know all men by these presents, that I Edward Stokes, of the parish of St. Andrew, Holborn, London, chinaman for Edward Smith and John James, upholiferers, of the parish of St. Luke, Middle fex I have made, ordered, conflituted, and appointed, and do by these presents make, ordain, constitute, and appoint my friend Henry Brown, of the parish of St. James, Cierkenwell, in the faid county of Middlefex, watchmaker, my [or out] true and lawful attorney for me, in my name, and on my behalf [or for us, in our names, and on our behalf], to adjust and settle ail and every account and accounts with all and every perfen and perfons with whom I for we I have had, or fhall or may have any transactions or dealings whatfoever, and to compromife, agree, and determine all disputes and differences that have or shall arise between me for us ] and any other perion or perfons whom foever, and to execute all fuch decos, inferument, and writings, as he the faid Henry Brown In all judge necessary, and to ask, demand, sue for, recover, and receive, to and for my [or our] ule, of and from all and every perion 3

it is not good; thus a condition not to use a trade, till or flow ground, &c. is unlawful, being against the public good, and therefore void. When a bond depends upon a deed, and the deed becomes void, the bond is void also; a condition to indemnify a person from any legal prosecution is void, being against law. Conditions of bonds are to be not only lawful, but possible: if no time is limited in a bond for payment of money, it is due presently, and payable on demand.

In a bond where feveral persons are bound feverally, the obligee has his option, either to sue all the bondmen together, or all of them apart, and have several judgments and executions, but he can have satisfaction but once; but if a bond be made to three to pay money to one of them, they must all join in the action. An heir is not bound by a bond, unless he be expectly named, but the administrators and executors are.

A bond may be made from one to any number of persons, or from any number of persons to one. If the surname only of the drawer be subscribed, it is sufficient, though there be a blank for his Christian name. If a bond has no date, or a salie date, or an impossible date (as the thirtieth day of February), yet if it be sealed and delivered it is good; a person cannot be charged by a bond without delivery of the bond to a creditor.

Where a bond is made for the payment of a fum of money by instalments, the holder of the bond in some cases may come upon the drawer for failure of the first payment, but in other cases he cannot sue for the money till the last payment becomes due; as for instance, if A gives a bond to B to pay sol, in the following manner: viz. 10l, to be paid at a certain day, and 10l, at another certain day; in this case B cannot sue for the debt till the last payment becomes due, as the sol, is mentioned as an entire debt; but if it be expressed to pay 10l, at a certain day, and 10l, at another certain day, making in all sol, the creditor may sue upon the bond on failure of the first payment.

A bond may be good though it contains false Latin, or false English, or though it be of a doubtful interpretation, as, if A binds himself to B to pay a sum of money to A (whereas it should be to B), here the obligation is good, and the solvendum void. It a bond be interlined in a place not material, it will not hurt the bond; but if it be in a material part, it will make the bond void. In short, all bonds, obligations, bills, promissory notes, &c. when any doubt arises, are always interpreted in savour of the party to whom the money is due.

These are the principal legal precedents used by mercantile men, to which I shall add a power or letter of attorney, as being in most general use by all descriptions of people.

# A Letter of Attorney from one, or two, to fettle Accounts and receive Money.

Know all men by thefe prefents, that I Edward Stokes, of the parith of St. Andrew, Holborn, London, chinaman for Edward Smith and John James, upholflerers, of the parish of St. Lake, Middlefex | have made, ordained, conflituted, and appointed, and do by these presents make, ordain, construte, and appoint my friend Henry Brown, of the parish of St. James, Cierkenwell, in the faid county of Middlefex, watchmaker, my [or our] true and lawful attorney for me, in my name, and on my behalf [or for us, in our names, and on our behalf], to adjust and fettle all and every account and accounts with all and every perfen and perfons with whom I [or we] have had, or shall or may have any transactions or dealings whatfoever. and to compromife, agree, and determine all disputes and differences that have or shall arrise between me for us I and any other person or persons whomsoever, and to execute all such decas, inferuments, and writings, as he the faid Henry Brown thall judge necessary, and to ask, demand, sue for, recover, and receive, to and for my [or our] use, of and from all and every

perion of perfons, that how in the, or how may become indebted to me [of to] by any ways or memo whatfoever, all and tytry the debt and debts, furniand fishs of money by them respectively due and owing, and to some pound for any fuch debt or debts, and to take left thus the whole for the same, or otherwise to adjust and settle the same in fuch manner and upon tuch terms as he the faid Henry Brown shall in his discretion think fit; and for non-payment thereof, or of any part thereof, to take such course for recovering the same as to my [or our] said attorney shall feem meet a and upon receipt of the faid debt or debts. fum or fuths of money respectively, or any part thereof, acquittances or other fufficient discharges for me, and in my name for for us, in our name. ], or in his own name, to make and give for what he shall so receive, and generally to do, negotiate, transact, and perform all fuch other acts, matters, and things, for the. and in my behalf for for us, and on our behalf?, in and about the premises, as fully in every respect as I [or we] might or could do if personally present; hereby ratifying and confirming, and agreeing further to ratify and confirm all and whatfoever my [or one] faid attorney shall lawfully do, or cause to be done, in and about the faid premifes, by virtue of these presents. In witness whereof, I for we have hereunto fet my hand and feal for our hands and feals this twentieth day of March, in the year of our Lord 1803, and in the fortythird year of the seign of our Sovereign Lord George the Third, &c. \*

Edward Stokes, (E. S.)

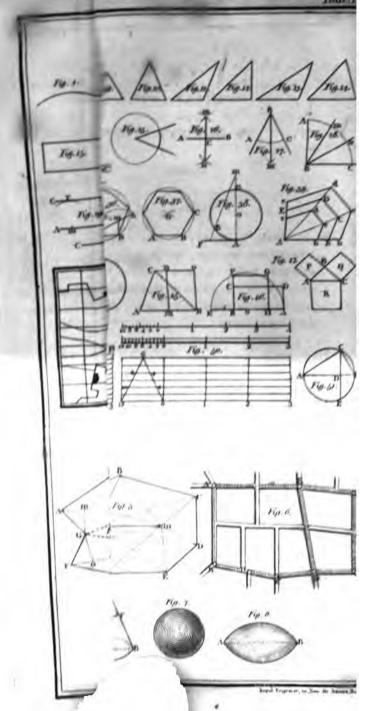
[or, Edward Smith, (E. s.)

John James, ] (J. J.)

A letter of attorney may be executed by any person, if of full age; and a man may give a power of attorney to his wife,

The words included in crotchets belong to the power when given by Edward Smith and John James; in other respects the power is the same as when given by Edward Stokes.

Vol. I.





# CHAP. VII.

# OF MENSURATION.

# SECT. L

OF SUPREFICIAL MEASURE, WITH THE METHOD OF MRASURING MASONS, BRICKLAYERS, CARPENTERS, SAWYERS, PLASTERERS, PLUMBERS, PAINTERS, AND GLAZIERS WORK, AND THE PRICE OF EACH; ALSO THE PRICE OF RACH COMMODITY, AND THE WAGES OF JOURNEYMEN.

BEFORE the learner proceeds to mensuration, it is necessary that be should understand duodecimals, or, as it is generally called, cross multiplication.

This rule is called duodecimais, because the numbers decrease from the left hand in a twelve-fold proportion; the first number being feet, the next number makes, and the next number the tweltth parts of an inch. Sec.

By this rule workmen and artificers cast up the contents of their work, and multiply feet, inches, and parts, by test, inches, and parts, without reducing them to one denomination, as in common arithmetic. In this rule inches are formetimes called *primes*, the parts are call d *seeman*, the next division thirds, &c.

Rele 1. Under the multiplicand, write the correspondent demoninations of the multiplier: viz. feet under seet, in a sinder inches, &c.

S . .

2. Mu.

- a. Multiply every term in the multiplicand, beginning at the lowell, by the feet in the multiplier, and write the refule of each under its respective term, observing to carry a for every 12 in the product to the next higher denomination.
- 3. In the fame manner multiply every term in the multiplicand by the inches in the multipliet, and fer the product of each term one place further to the right hand of that term in the multiplicand, observing to carry t to the next higher denomination for every to as before.
- 4. Proceed in the fame manner with the feconds, and the other denominations, if there be any more, and the fum of the products will be the product required.

Example 1. Multiply 10 feet 4 inches and 5 parts by

Feet.	Inches-	Parts,	SHEEK.	218	241 2
7	\$	5		433	6000
0	2	11		SOR.	HOU!
2	4	0		22	
79	0	.0		-4	1-51
0	0	3	4		-
6	2	8		ų.	X
6	8	0			
0	0	0	2	6	
0	0	2			
0	5	0			
79	11	0	6	6	Answer.

In this example the 5 parts are first multiplied by 7 feet, and the product is 2 inches 11 parts; then the 4 inches are multiplied by the 7 feet, and the product is 2 feet 4 inches; then the 10 feet are multiplied by the 7 feet, and the product is 70 feet. Then I multiply by the 8 inches, saying 5 times 8 is 40, which is 3 twelves and 4 over, the 4 I set one place further towards the right hand than the multiplicand 5, and the 3 I place under the seconds; then I multiply the 4 inches, saying 4 times 8 is 32, which is 2 twelves

and 8, the 8 I fet under the parts and the 2 under the inches; then I say 8 times to is 80, which is 6 twelves and 8, the 8 I set under the inches and the 6 under the seet. In the same manner I multiply by the third and last figure 6, saying 6 times 5 is 30, which is 2 twelves and 6, the 6 I placeane place further towards the right hand than the first figure of the last product, and proceed in the same manner as before,

I have given this example at formewhat an unnecessary length, in order to instruct the learner more fully in the nature of the rule; but it is generally performed in three lines only, when consisting of feet, inches, and parts, as in the following example:

and the fam of all the products will be the answer.

Example 2. Multiply 6 feet 4 inches and 5 parts, by 4 feet 6 inches and 9 parts.

Feet. 6 4	Inches. 4 6	Parts. 5			
25	5 2	8	6		
ŏ	4	9_	3	_9	
29	0	5	9	9	Anstue

Note. As the foot is divided into 12 inches, so each inch is subdivided into 12 parts, called seconds, and each second is again subdivided into 12 thirds, and each third into 12 fourths, &c.

28.3. What is the superficial content of a square piece of ground, measuring 39 feet 10 inches and 7 parts in length, and in breadth 18 feet 8 inches and 4 parts?—Answer 745 feet 6 inches 10 seconds 2 thirds and 4 fourths.

Qu. 4. What is the area of a floor in length 24 feet 10 inches 8 feconds 7 thirds and 5 fourths, and in breadth 9 feet 4 inches and 6 feconds?—Anfwer 233 feet 4 inches 5 feconds 9 thirds 6 fourths 4 fifths and 6 fixths.

Seconds.

Seconds, thirds, &cc. are usually marked by two or three floor strokes placed over the figures: thus, the answer to the last question is expressed, 233 feet 4 5 6 6 4 6

# Superficial Meafure.

Menforation, in general, is the art of measuring and estimating the magnitude and dimensions of bodies or figures, and is divided principally into three parts, called lineal measure, fure, superficial measure, and solid measure.

# Definitions.

- Lineal measure is simple measure in length, without breadth or depth.
- 2. Superficial measure confids of length and breadth taken together.
- 3. Solid measure confists of length, breadth, and depth; of which hereafter.
- 4. A point has no parts nor dimensions, neither in length nor breadth.
  - 5. A line his only length, without any other dimensions.
- 6. A right line lies all in the fame direction, and is the flortest way between its two extremities.
- 7. A curve line continually changes its direction. See fig. 1.
- 8. Parallel lines are always at the fame diffance from each other. See fig. 2.
- 9. Oblique right lines change their distance and meet in an angle. See fig. 3.
  - 10. An angle is the meeting of two lines. See fig. 5.
- 11. If the two lines which form an angle be perpendicular to each other, they then form a right angle. See fig. 6.

- 13. But if the two lines be not perpendicular to each other they form what is called an oblique angle, which is either greater or lefs than a right angle. See fig. 9 and 10.
- 13. If an angle be less than a right angle, it is called an acute angle. See fig. 7.
- 14. An angle that is greater than a right angle is called an obtuse angle. See fg. 8.
- 15. A triangle is a figure contained under three lines, and has various names, according to the fize of its angles.
- 16. An equilateral triangle has its three fides, and consequently its three angles, equal to each other. See fig. 9.
- 17. An isosceles triangle has only two sides equal. See fig. 10.
- 18. A fealene triangle has its three fides and angles unequal to each other. See fig. 11.
- 19. A right-angled triangle has one right angle. See fig. 12.
- 20. An obtule-angled triangle has one obtule angle. See fig. 13.
- 21. An acute-angled triangle has all its angles acute. See fig. 14.
- as. A figure of four fides is called a quadrangle, or a quadrilateral figure, and is either a parallelogram, a square, a rhomboid, a rhombus, a trapezium, or a trapezoid.
- 23. A square is an equilateral rectangle, having all its sides equal, and all its angles right angles. See fig. 16.
- 24. A rhomboirt is an oblique-angled parallelogram. See fig. 17.
- 25. A rhombus is an equilateral figure, having all its fides equal, but its angles are oblique. See fig. 18.
- 26. A trapezium is a quadrilateral figure, but its opposite sides are not parallel. See fig. 19.
- 27. A trapezoid has only two opposite fides parallel. See fig. 20.
- 28. Plane figures having more than four fides, are generally called polygons, but they receive particular names, according

to the number of their fides i thus a polygon of five fides is called a praingen, a figure of fix fides an bezagen, a figure of feven fides an bezagen, eight fides an offagen, nine fides a senagen, ten fides a decagen, eleven fides an endetagen, and twelve fides a decagen.

ag. A circle is a plain figure bounded by one circular line, called the ci cumference, which is every where equally diffant from the centre. See fig. at.

30. The radius of a circle is a right line drawn from the centre to the circumference.

31. The diameter of a citele is a right line drawn through the centre, and bounded at each end by the circumferences

34. An arc of a circle is any part of the circumference.

33. A chord is a right line joining the two extremities of an arc.

34. A fegment of a circle is any part thereof.

35. A femicircle is half a circle.

36. A fector is a part of a circle contained under part of the arc, and two radii drawn to the centre. See fig. 42.

37. A quadrant is a fector of a circle, having one quarter of the circumference for its arc, and its two radii are perpendicular to each other. See fig. 23.

38. The circumference of every circle in geometry is fupposed to be divided into 360 equal parts, called degrees, and each degree subdivided into 60 minutes, each minute into 60 seconds, and so on; hence a semicircle contains 180 degrees, and a quadrant 90 degrees, which form a right angle, and half a quadrant, called an octant, contains 45 degrees; for the measure of every right-line angle is an arc of a circle contained between the two lines, which form the angle, the point of the angle being in the centre of the circle, and the number of degrees contained in the arc of the circle gives the measure of the angle. See fig. 25.

39. In every right-angled triangle the fide opposite the right angle is called the hypothenuse, and the other two fides, the legs of the triangle.

- 40. The height or altitude of a figure, is a line drawn from the uppermost fide or angle, perpendicular to the base.
- 41. An angle is generally described by three letters: that letter which stands in the middle snews the angle intended. Thus, in figure 24. EAC represents an angle formed by the line EA, and the line AC; and the letters DAE in the same sigure snew the angle formed by the two lines DA and EA.

#### Problems.

#### PROBLEM I.

TO DIVIDE A GIVEN LINE INTO TWO EQUAL PARTS.

Fig. 26. From B as a centre with the compasses opened to any greater length than BC describe the arcs at m and n; then (the compasses being still at the same width) from A, as the other centre, describe two arcs cutting the former arcs in n; from the intersections of these arcs draw the straight line m C n, and it will divide the given line A B into two equal parts, at the point C.

## PROBLEM II.

TO DIVIDE A GIVEN ANGLE INTO TWO EQUAL PARTS.

-Fig. 27. From B as a centre with the compasses describe the arc AC; and from A and C with the radius describe two arcs intersecting each other at m, then draw the line mB, and it will divide the angle ABC into two equal parts.

#### PROBLEM III.

TO DIVIDE A RIGHT ANGLE INTO THREE EQUAL PARTS.

Fig. 28. From B as the centre describe the arc A C. Then with the same extent of the compasses, from A as the centre, cross the arc A C in n, and with the same radius from C, as the centre, cross the arc in m: from the points of in
Vol. I.:

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terfection m and n, draw the right lines m B and n B, and they will divide the right angle A B C as required.

# PROBLEM IV.

TO DRAW A LINE PARALLEL TO ANOTHER GIVEN LINE, AND AT A GIVEN DISTANCE.

Fig. 29. Let the given line be A II: then from the points m and n with a radius equal to C, the given diffance, describe the arcs r and o, upon which draw the line C D, and it will be parallel to the line A B.

## PROBLEM V.

IN A STYEN LINE.

Fig. 30. Let the given line be BC, and the given point A. Take two equal diffunces Am and Au, and with a radius greater than Am, from m and u as centres, describe two ares, cutting each other at r 1 from A draw Ar, and it will be perpendicular to the line BC: thus this perpendicular forms a right angle with each part of the line BC. There are many other ways of drawing perpendiculars to a given line, but the best way is to draw them by a square, or other mathematical instrument for that purpose: I shall, however, give another Problem, to draw a perpendicular from a given point out of the line.

#### PROBLEM VI.

IO ERI VALLA PERPENDICULAR FROM A GIVEN POINT,
BEARLY OFFONTE TO THE END OF A GIVEN LINE.

Fig. 31. Let the given point be A, and the given line B D; then from A draw any line A m, to meet B C: bifect A m at n, and from n as a centre, with the radius A n, deferibe the are A D m, cutting B C in D; then draw a line A D, and it will be the perpendicular required.

#### PROBLEM VII.

TO DIVIDE A GIVEN LINE 2NTO ANY NUMBER OF LQUAL PARTS.

Fig. 32. Let the given line be AB, then from A draw a line AC, and from B draw BD parallel to AC: on each of these parallel lines point off as many parts as the given line is to be divided into, beginning at A in the first line, and at B in the second line; then join the opposite points of division in each line, by the lines A 5, 1 4, 2 3, Sec. and they will divide the line AB as required.

#### PROBLEM VIII.

AT A GIVEN POINT IN A GIVEN LINE, TO MAKE AN ANGLE OF ANY PROPOSED NUMBER OF DEGREES.

Fig. 33. Let the given point be A, and the given line AB; then from A, as a centre, with a radius of 60 degrees taken from a line of chords, describe an are mn, outting AB in m; then take the proposed number of degrees with the compasses from the same line of chords, and apply the compasses from m to n; through the point n, draw the right line An, and it will form an angle with the line AB, of the number of degrees required \*.

Angles of more than 90 degrees should be taken off the line of chords at twice.

Or, the angle may be made with a divided arch, by laying the centre to the point A, and its radius on the line A B, and

A line of chords is always described upon the plain scale, which is an inflrument of buss, ivery, or wood, about every inches long, to be had at the mathematical inflrument makers: there are also other lines agon the scale of use in Geometry, as a line of sums, of tangents, secures, semitangents, risombs, and a line of equal parts; I shall give the figure of one of these scales, and the method of constructing the several lines upon it, with the uses for which they are applied, when I come to treat of Trigonometry.

mark at n, the number of degrees proposed from the arch, and draw the line A n, as before.

#### PROBLEM 1X.

# A .. TO MEASURE A GIVEN ANGLE.

Fig. 39. Describe the arc min, with the compasses opened to the radius of 60 degrees in the line of chords, take the width of the arc min, and apply that distance to the line of chords, and is will show the number of degrees in the angle.

If the arc of the angle exceed 90 degrees, it must be taken off at twice, as before.

Or, the angle may be measured by means of a divided arch as the angle in the last problem was constructed.

# PROBLEM X.

# TO PIND THE CENTER OF A CIRCLE.

Fig. 34-110 the circle ABC, describe any line, as AB, which is called a cheed, from the middle of which line draw the perpendicular CD, which will be the diameter of the circle, and bifect CD in the point Q, which will be the centre.

#### PROBLEM XI.

# TO DESCRIBE THE CIRCUMPERENCE OF A CIRCLE, THEOLOGY THREE GIVEN POINTS.

Fig. 35. Let the given points be A B C; then from the middle point B, draw two chords, or two right lines to the other two points A C; bifect these two lines by perpendicular lines meeting each other in the point O; O will then be the centre of the circle; and with the radius O A, or O B, describe the circle ABC, and it will pass through the three given points.

# PROBLEM XII.

TO MAKE A REGULAR PENTAGON ON A GIVEN LINE.

My. 96. Let the given line be AB. Draw B na perpendicular to AB, and equal to half of it. Draw A m, and produce it till m n be equal to B m. With a radius equal to B n describe two arcs, intersecting each other in a point O from A and B, as centres. With the same radius, from the point of intersection O, describe the circumscribing circle AB and about the circumsterence of this circle apply the distance AB sive times, and it will describe the figure required.

## PROBLEM XIII.

TO DESCRIBE AN HEXAGON UPON A GIVEN LINE

Fig. 37. Let the given line be AB. Then with a radius equal to AB, from A and B as centres describe two interfecting arcs. From the point of intersection O, with the same radius describe the circle ABC; then apply the line AB fix times round the circumference, and it will form the figure required.

If each fide of the above figure be divided into two parts, a figure of twelve fides may be formed; and if each fide be divided into three parts, a figure of eighteen fides may be formed; thus it appears that the radius of a circle will divide the circumference into fix equal parts; half the radius will divide it into twelve equal parts; and twice the radius will divide it into three equal parts.

# PROBLEM XIV.

TO PIND A RIGHT LINE BOUND TO ANY GIVEN ARC

Fig. 38. Let the given are be A.B: through the point A, and the centre of the circle, draw A m, making m n equal to 3 of the radius n O. Draw a line A P perpendicular to A m, then through m B draw m P; then A P will be equal to the arc A B.

# PROBLEM XV.

TO MAKE ANY REGULAR POLYGON ON A GIVEN

Fig. 36. Let the given line be C D: draw CO and DO, making the angles at C and D, each equal to half the angle of the polygon: from the centre O with the radius OD describe the circle ABCD, then apply the line C D continually round the circumference, and it is done.

Need. The angles of a polygon are found in this manner: divide the whole 300 degrees, by the number of fides in the polygon, and the quotient will be the angle at the centre, which angle subtracted from also degrees, the remainder will be the angle of the polygon.

# and all comments A TABLE

Containing the Number of Degrees in the Angle, and at the Centre of every regular Polygon, from three Sides to twelve.

No of Sides.	Name of the Polygon.	Angle at the Centre.	Angle of the Polygon.	Angle ODC or OCD.
3	Trigon	1204	609	300
4	Tetragon	90	90	45
15	Pentagon	72	108	
6	Hexagon	60	150	54
171	Heptagon	514	1281	647
8	Oétagon	45	135	674
9	Nonagon	40	140	1 70 1
10	Decagon	36	144	73
111	Endecagon	32	1477	731°c
18	Dodecagon	1 30	150	75

#### PROBLEM XVI.

TO MAKE A FIGURE SIMILAR TO ANY OTHER GIVEN

Fig. 39. From any angle, as suppose A, draw diagonals to each of the other angles; then to b c, one side of the sigure, draw a parallel line BC; and CD parallel to cd, and ED parallel to ed; and it will be the figure required.

#### PROBLEM XVII.

TO REDUCE A COMPLEX FIGURE FROM ONE SIZE TO ANOTHER, BY MEANS OF A SCALE.

Fig. 40 and 41. Divide the given figure into squares, by cross-lines, then divide another paper on which you intend to draw your figure, into the same number of squares, and observe what squares the several parts of the figure fall in, and draw familiar parts in the corresponding squares of the other figure.

### PROBLEM XVIII.

TO DRAW A TRIANGLE EQUAL TO A GIVEN TRAFE-ZIUM.

Fig. 4a. Let the trapezium be ABCD; draw the diagonal BD and CE parallel to BD, meeting AB, produced in the point B; join DE; then the triangle ADE will be equal to the trapezium ABCD.

#### PROBLEM XIX.

TO MAKE A TRIANGLE EQUAL TO A FIGURE OF FIVE SIDES.

Fig. 43. Let the figure be ABCDEA; draw the two diagonals DA, DB, and the lines EF, CG, parallel to them, and produced till they meet the base AB, produced to F and G; join DF and DG, and DFG will be the triangle required.

In the same manner a triangle may be made, equal to any right-lined figure whatever.

#### PROBLEM XX.

TO MAKE A TRIANGLE RQUAL TO A GIVEN CIRCLE.

Fig. 44. Let the given circle be A, draw the radius A O, and the tangent AB, perpendicular to it; on the line AB, take AB equal to the circumference of the circle; join BO; then will the triangle ABO be equal to the circle.

#### PROBLEM XXI.

TO MAKE A RECTANGLE, OR A PARALLELOGRAM, EQUAL TO A GIVEN TRIANGLE.

Fig. 45. Let the given triangle be ABC, bifect the base AB in m, through C; draw C no parallel to the base of the triangle AB; draw the line m n and BO parallel to each other a and the rectangle m n OB will be equal to the triangle ABC.

#### PROBLEM XXII.

TO MAKE A SQUARE SQUAR TO A GIVEN RECTANGLE.

Fig. 46. Let the given rectangle be A B C D: produce the fide A B, till B E be equal to B C: bifect A E in the point O, on which as a centre, with the radius O A, describe a semi-circle A G F E, and produce B C to F, on which describe the square B F G H, and it will be equal to the rectangle.

In this manner any right-lined figure may be reduced to a fquare.

#### PROBLEM XXIII.

TO MAKE A FIGURE FOUND TO TWO OTHER SIMILAR FLOWERS.

Fig. 47. Let the two fimilar figures be P and Q, which are squares: let the two sides A B and B C be perpendicular to each other; join their extremities A C by a right line, on which describe the square R, which will be equal to the two squares P and Q taken together.

All fimilar figures may be added together in the same manner: for any two similar figures, constructed upon the legs of any right angle, are equal to a similar figure constructed upon the hypothenuse.

#### PROBLEM XXIV.

TO MAKE A SQUARE EQUAL TO ANY NUMBER OF SQUARES TAKEN TOGETHER.

Fig. 48. Draw two lines Am, An, perpendicular to each other: on one line mark AB equal to the fide of one of the given squares, and on the other line mark AC equal to the fide of another given square: then draw the line BC, which will be equal to the fide of a square, equal to the two somer given squares taken together: then mark AD equal to BC, and AE equal to the fide of a third given square; then DE will be the side of a square, equal to the sum of the three given squares taken together.

Thus any number of fimilar figures may be added together.

#### PROBLEM XXV.

TO MAKE PLAIN DIAGONAL SCALES.

Fig. 49. Draw a line of a convenient length as AB, and divided into eleven equal parts \*; form each of these parts into a rectangle of a sufficient height, by drawing parallel and perpendicular lines; divide the aititude into ten equal parts, if it be for a decimal scale—but if it be for feet and inches, divide into twelve parts; through these points of division draw parallel lines the whole length of the scale; then divide the length of the first large division AC into ten equal parts, both at the top and the bottom of the scale, and connect these points of division by diagonal lines as shown in the sigure, and the scale is sinished.

<sup>\*</sup> Only four parts are laid down in this scale for want of soum.

The use of these diagonal scales is, to take off the dimensions of three figures; and if the first large divisions in the scale from B to C be units, the second set of divisions from C to A will be the tenth parts of an unit, and the divisions in the altitude from D to A will be hundredth parts: if BC be tens. AC will be units, and AD tenth parts: if CB be thousands, AC will be hundreds, and AD tens: for example—if it were required to take off \$42 from the scale, fix one foot of the compasses, at the figure a of the largest divisions at the bottom of the scale, and extend the other foot to 4 of the second smaller divisions, and on the bottom of the scale; then for the three units slide up both points of the compasses in a perpendicular line, till they fall upon the third longitudinal line, and on that line, with one foot of the compasses remaining fixed, extend the other foot to the third diagonal line, and you will have the extent of the three figures as required.

# To meafure the Longth of any Line.

Take the length of the line, between the compasses, and apply it to the scale: suppose it contains above three of the large divisions, then set one foot of the compasses on the point 3 of the large divisions, and suppose the other foot of the compasses to fall between 4 and 5 of the second divisions; stide up the compasses by a perpendicular motion, keeping one foot on the line of the large division 3, till the other foot fall on the intersection of one of the diagonal lines, which suppose to be four; this shows that the length of the line measured is 344.

#### PROBLEM XXVI.

#### TO MAKE PLAIN SCALES FOR TWO FIGURES.

Fig. 50. If the scale be a decimal one, after dividing it into any proposed number of large divisions, one of those divisions must be subdivided into ten parts: but, if it be a duodecimal scale, one of the large divisions must be divided into twelve parts, and serve to take dimensions for seet and inches.

The most proper form for a scale of equal parts is that where the divisions are marked on the very edge; and are generally made of ivory, the edge being made thin for the purpose of pricking off divisions on the paper, without the help of the compasses.

#### PROBLEM XXVII.

TO MAKE A RIGHT LINE, THAT SHALL BE A MEAN PROPORTIONAL BETWEEN TWO GIVEN LINES.

Fig. 51. Let the two given lines be AC, CB; foin them to each other so as to form a right angle at the point C: join the points AB, which will be the diameter of a circle; then describe the circle BCAE, draw CD perpendicular to AB, and in all the the mean proportion required.

Note. The angle ACB, described in a semicircle, is always a right angle.

The chord AC is a mean proportional between AD and AB, and the chord BC is a mean proportional between BD and AB.

The square of the hypothenuse of a right angled triangle is equal to the squares of both the sides, as seen in Problem XXIII.

The three inward angles of a triangle are equal to two right angles.

Triangles that have each angle equal to each other are called fimilar triangles.

# To find the Area of Supercial Figures.

The area of a figure is the measure of the furface, without any regard to its thickness or depth.

The area of a superficial figure is the number of square inches, feet, yards, &c. contained on its surface.

Square yards, feet, inches, &c. differ from the same meafures in length, as seen in the following table:—

Uu 2 Lineal

Lincal Meafures.	Square Meafures.
12 Inches i Foot 3 Feet i Yard 6 Feet i Fathom 164 Feet or } i Pole 54 Yards } '' or Rod 40 Poles i Furlong 8 Furlongs i Mile	

#### PROBLEM XXVIII.

TO FIND THE AREA OF A PARALLELOGRAM, A TOUTARR, A RECTANGLE, A RHOMBUS, OR A RHOMBOID.

The area of any of these figures is found by the following rule:

Rule. Multiply the length by the breadth (or, if it be a rhombus or a rhomboid, by the perpendicular height \*) and the product will be the area.

Fig. 40. What is the area of a square, one side whereof is 6 sect, and the other side 7 sect? Answer 48 sect.

#### PROBLEM XXIX.

Fig. 18. What is the area of a rhombin, the length whereof is 12 feet, β inches, and the perpendicular height 6 feet, 10 inches?

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	6	10	
	74	6	
	10	4	7
Antwer	Ĥ	10	,
			<b>-</b>

The perpendicular height of a parallelogiam, a rhombus, A. ia a bine drawn from the uppermoft fole, perpendicular to the Lafe, and the perpendicular height of a triangle, is alto a line drawn from the upper anoth angle, perpendicular to the hate.

#### PROBLEM XXX.

Fig. 17. What is the area of a rhomboid, whose length is 5 chains, and 20 links; and perpendicular heighth 20 chains 5 links.

In this problem the chains and links are multiplied by each other as decimals, as the links are always decimal parts of the chain, as will be shown hereafter, and the product is the antwer in square chains and links, which is divided by to to bring them into acres, as there are to square chains in an acre; and the decimals are multiplied by 4 for roods, and

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10) 104, 20	000
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	4
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	40
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5,80

those decimals again multiplied by 40 for perches, because 4 roods make one acre, and 40 perches one rood.

#### PROBLEM XXXL

#### TO FIND THE AREA OF A TRIANGLE.

Ftg. 9. The area of all triangles is found by the following rules:—

RULE 1. Multiply the base by the perpendicular height; and half the product will be the area. But when only the three sides of the triangle are given, the area is found by the following rule:—

RULE 2. Add the three sides together, and from half the fum subtract each side separately; multiply the half sum by the remainders of the three sides continually together, and the square root of the product will be the area of the triangle.

BEAMPLE

Example 1. What is the area of a triangle, whole bale is 40 feet, and perpendicular height so feet?

49 49 4) Nos

Aniwer 400 heet

Example a. What is the area of a triangle whole a fulca

Antiver 130,78 feet

#### PROBLEM XXXII.

FOURTH ANY ONE SIDE OF A RIGHT ANGLED TREAMGER,
HAVING THE OTHER TWO SIDES.

In every right angled triangle, the figure of the hypothemic is equal to both the figures of the two legs, as fhown in Problem XXIII.

Therefore, to find the hypothemith, add the figures of the two legs together, and extract the figure root of the turn.

And

And to find one leg, subtract the square of the other leg from the square of the hypothenuse, and the square root of the difference is the leg required.

Example 1. What is the hypothenuse of a right angled sriangle, whose base is 33 feet, and perpendicular 56 feet?

5 <b>6</b> 56	33
(6	33
136	99
€ 8U	49
3136	1089
1089	====
4295(65 feet.	Aniwer.

EXAMPLE 8. What is the perpendicular of a right angled mangle, whose base is 40 yards, and hypothenuse 50 yards?

2a. 3. What is the height of a fealing ladder to reach the top of a wall all feet in height, and across a ditch 45 feet in breadth? Answer 50 feet.

Questions of this nature are resolving by the foregoing Problem, the height of the ladder being confidered as a hypothenuse of a right angled triangle, and the height of the wall and breadth of the ditch as the two other legs of the triangle.

#### PROBLEM XXXIII.

#### TO FIND THE AREA OF A TRAPEZOID.

RULE. Multiply the fum of the two parallel fides by half the perpendicular diffunce between them, and the product will be the area.

EXAMPLE

EXAMPLE 1. What is the area of a trapezoid, whose two parallel sides are 8 sect and 18 sect, and perpendicular distance 10 sect?

#### PROBLEM XXXIV.

#### TO FIND THE ARRA OF A TRAFEZIUM.

RULE. Divide it into two triangles, by a diagonal line drawn from any one angle to the opposite angle, then find the area of these two triangles, by Problem XXXII. and add them together.

Note. Two perpendiculars drawn from the diagonal line to the other two opposite angles will be the perpendiculars of the triangle.

#### PROBLEM XXXV.

TO FIND THE AREA OF ANY IRREGULAR FIGURE OF ANY NUMBER OF SIDES.

All irregular figures contiffing of more than three fides are to be divided into triangles or trapeziums, then find the area of each of these triangles or trapeziums separately, and add them together, and the sum will be the area of the whole figure.

Note. Every figure may be divided into as many triangles, except two, as the figure has fides.

Thus, a figure of five fides may be divided into three triangles; a figure of fix fides, into four triangles; a figure of eight fides, into fix triangles, &c. En. s. How many square feet does a circle contain, the circumference of which is 10.9956 yards? Answer 86.19266.

The operation of these problems is purposely omitted for the exercise of the learner.

#### PROBLEM XXXIX.

TO FIND THE LENGTH OF ANY ARC OF A CIRCLE.

RULE 1. As 180 is to the number of degrees in the arc, to is the product of the radius multiplied by 3.1416 to the length of the arc.

RULE s. As 3 is to the number of degrees in the arc, so is the product of the radius multiplied by .05236 to the length of the arc.

Qu. 1. What is the length of an arc of 1s degrees 10 minutes, the radius being 10 feet? Answer s.1s34<sup>2</sup> feet.

Lv. s. What is the length of an arc of 30 degrees, the radius being 9 feet? Answer 4.7184 feet.

#### PROBLEM XL

TO FIND THE AREA OF A SECTOR OF A CIRCLE.

FIG. 22. RULE 1. Multiply the radius by half the arc of the fector, and the product is the area.

RULE s. As 360 is to the degrees in the arc of the sector, so is the whole area of the circle to the area of the sector.

Note. For the semicircle take one half of the whole circle; for a quadrant, one quarter; for the sextant, one sixth, &c.

EXAMPLE. What is the area of a fector of a circle, whole, radius is 15 feet, and the are 30 feet?

# PROBLEM XXXVII.

TO FIND THE DIAMETER OF THE CIRCUMPERENCE OF A CIRCLE, THE ONE FROM THE OTHER.

RULE r. As 7 is to sa, fo is the diameter to the circumference.—As sa is to 7, fo is the circumference to the diameter.

RULE s. As 113 is to 355, so is the diameter to the circumference.—As 355 is to 113, so is the circumference to the diameter.

RULE 3. As 1 is to 3.1416, fo is the diameter to the circumference.—As 3.1416 is to 1, fo is the circumference to the diameter.

Qu. 2. If the diameter of the earth be 7958 miles, as it nearly is, what is the circumference, supposing it were exactly round? Answer \$5000.8528 miles.

24. 2. What is the diameter of the earth, supposing the circumference 25000 miles? Answer 79571 miles.

# PROBLEM XXXVIII.

TO FIND THE AREA OF A CIRCLE.

RULE 1. Multiply half the circumference by half the diameter, and the product is the area.

RULE 2. Multiply the fquare of the diameter by .7854.

RULE 3. Multiply the square of the circumference by 07958.

RULE 4. As 14 is to 11, fo is the square of the diameter to the area.

RULE 5. As 88 is to 7, fo is the square of the circumference to the area.

24. 1. What is the area of a circle, whose diameter is 7 feet? Answer 38.4846 feet.

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#### PRINCE XXX

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RULE 2. As 3:3 TO THE THIRD IN the product of the Thin in might of the are.

# PHOBLEY T

TO FIND THE AREA IN . FOR THE P. ....

Fig. 22. Rule: Materials the sales of the fector, and the sandar's the same

RULE 2. As its is in the suggestion where it is a configuration of the street of the content of

Note. For the feministre time and the for a quadrant, one quarter; the the feministre cc.

Example. What is the sense of a common of a normal sense of a common of the sense o

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Answer 20, See

24.2. What is the area of a quadrant, and a semicircle, whose radius is 13 feet each? Answer, the quadrant 132.7326 feet, and semicircle 265.4652 feet.

# PROBLEM XLI.

TO FIND THE AREA OF A SEGMENT OF A CIRCLE.

RULE. Find the area of the lector of the circle by the last problem.

Find the area of the triangle formed by the chord of the

fogment, and the radius of the fector.

Then the fum of these two will be the answer, if the segment is greater than the semicircle; but if the segment be less than a semicircle, the difference will be the answer.

The foregoing problems will be found fully fufficient to instruct the learner in the method of measuring every kind of superficies whatever, as there is no figure but may be reduced to one or more of the foregoing figures.

# OF MEASURING ARTIFICERS' WORK.

# Mafons' Work.

To masonry belong all forts of stone-work, and the measures of it is by the foot, either superficial or solid. Stone walls, columns, blocks of stone, &c. are measured by the solid foot; but slabs, chimney-pieces, pavement, &c. are measured by the superficial foot.

The Prices of Majons' Work.			
Newcastle stone, per foot cubic		i id	
Workmanship to ditto, per superficial foot, from			
6d. to	0	1 (	5
Portland stone, per cube foot	0	3	4
Workmanship to ditto, per foot superficial, from			
10d. to	0		6
	F	avin	g

Paving in Pertland floores floright, of inch			
thick, per foot superficial	Ð	:	ю
Ditto 2 inch thick	Ð	2	9
Purbeck stone, paving, per foot superficial,			
from 11d. to	0	1	4
Bremen flone, paving in terraces, per foot			
superficial	0	1	6
Portland ftone, chimney-pieces and flabs, from			
11 inch thick to 3 inches, per foot superficial, from			
15.6d. to	0	2	5
Marble chimney-pieces veined, per foot cube	I	15	0
Workmanship to ditto, per foot superficial, from			
31.6d. to	0	8	6
Blue and white marble, an inch thick, per foot			
superficial	0	5	6
• •	=		

# Bricklayers' Work.

Brick-work is measured by the square rod of 16 feet and a half, and the brick-work estimated at a brick and a half thick; if a wall be more or less than this standard thickness, it must be reduced to it, by the following rule:

RULE. Multiply the superficial content of the wall by the number of half bricks in the thickness, and divide the product by 3, and the quotient will be the superficial contents of the wall, at the true standard thickness of a brick and a half.

To take the dimensions of a building, it is usual to measure half round the outside, and also half round the inside; the sum of these two measures multiplied by the height, gives the superficial content, which must be reduced to the standard measure, in order to ascertain the price.

Chimnies are sometimes measured as if they were solid, deducting only the vacuity from the hearth to the mantle; and sometimes they are measured round for their breadth, and the height of the story is their height, and the depth of the jambs is their thickness; in this case no deduction is made for the sire place.

The chimney flasts, which appear above the building, are measured round for their breadth, and multiplied by their height for the superficial content; and the thickness is accounted half a brick more than it really is, on account of the scasfolding, &c.

All windows, door-ways, &c. are to be deducted in meafuring for the materials, but not in measuring for workmanfaip. There are also some other allowances, as double measure for feather'd gable ends, &c.

All the following brickwork is measured by the rod square of 165 feet, which contains 272 square feet; bence, when the contents of brick-work is found in square feet, it is divided by 272 (the fraction being neglected), and the quotient is the number of square rods; which is to be reduced to standard measure by the surmer rule.

Tiling is measured by the square of 10 feet, making one hundred square seet to each square.

## Prices.

Brickwor	k, 1	it p	er'	rod.					6	. t.	Z
New-place bricks							mor				
in wells, &c									8	8	•
Rough greyflock	brid	ck-v	voi	k, i	ո բ	arty	/-wa	ılls,			
&c. from 101. to .									12	0	0
Labour and morta											
31. to									3	15	0
Labour only to dit	to,	fro	m	ı <i>l</i> . 6	s. to						
Plain tiling		•									
New plain tiling,											
Labour only, from	n 4	. to	•	•	٠	•	•	•	•	5	0
P	ice	of	M	late	rial	١.					
Lime, per bundred									٥	14	•
Sand, per load.											
Mortar, per load											
·										oint	

Pointing mortar, per load	•	1	18	9
Bricks, per hundred, according to the quality				
from gs. to	•	0	10	6
Bricklayer, per day, in fummer	•	0	4	0
Ditto, in winter				
Labourer, per day, in summer, from as. 6d. 1				
Ditto, in winter		0	8	6
• • •		=		=

# Carpenters' and Joiners' Work.

Most large and plain articles are measured by the square of 10 feet, each square being 100 feet; but mouldings and other ornaments are generally measured by the soot, running measure.

In measuring flooring, no deductions are made for hearths, on account of the trouble.

Partitions are measured from wall to wall, and from floor to floor, and no deductions made for door-ways.

In measuring roofs, the length of the house in the infide with two thirds of the thickness of one gable, is considered as the length: and the breadth is equal to twice the length from the ridge to the end of the rasters.

For staircases, take the breadth of all the steps by a string from the top of the staircase to the bottom, which multiply by the length of one step.

For wainfcoting, take the compass of the whole room for the length; and the height from the floor to the ceiling for the breadth, deducting doorways, windows, &c. from the materials, but not from the workmanship.

For doors, shutters, &c. These are measured by the foot square, allowing for their thickness, the number of pannels, &c.

#### Prices.

Roots, at per square.				
Labour and nails only, from 51.6d. to .	•	0	1 5	0
Partitions, at per square.				
Labour and nails, from ss. 6d. to	•	•	15	•
Doors, at per foot square superficial.				
Deal ditto		0		Ç
Two-pannelled ditto, according to the thic	k-			
nels, from 7 d. to		9	0	1 1
Four-pannelled ditto, from ofd. to		0	I	٥
Safa-frames and fafties, at per foot superficial.				
Deal ditto, fingle hung, with weights, pullie	u.			
Rec. from 21.4d. to	•	0	8	•

# Plaisterers' Work.

Plaisterers' work is of two kinds: viz. plaistering upon laths, and rendering, which is plaistering upon walls.

They are valued differently;—the contents are either found by the square soot, or the square of 10 sect, or the square yard; but mouldings, &c. are measured by running measure.

Deductions are always made for door-ways, fire-places, &c. but not for windows.

## Prines.

	•	., .					L.	1.	J.
Lime whitening once,	pe	r yarıl				•	~	0	
Colouring, common,									
Rendering rough, on	c (	coat, per	yaı	rd			0	9	3\$
Lathing only, per yar	.1			•			0		6
Lathing and plaistering	g,	per yara	/, f	ron	194	:0	0	ı	4
Ditto, to ceilings, fro	m	11.24.10		•	٠.		0	I	6
Outfide lime and hair									•
Plaister, per cent								8	
Vir laths, per bundle							0	1	6
Size, per gallon .							0	0	4
Whitening, per doxes							ø	ω	8
								TIPL	

•		Sai	11216	2.5	Pri	ices			••	•		,
Twelve feet	امما		•					مار س		٤٠	s.	d.
							•					
cuts, from as you												
Ten-feet dit	io, f	rom	<b>2</b> 5.	7.J.	to	•	•	•	•	0		10
- ••		_			_			_	_			

All extra cuts are charged after the rate of three shillings per square of 10 feet.

# Plumbers' Work.

Plumbers' work is rated by the cwt. and fometimes by the fingle pound, for there is no method yet discovered whereby lead can be cast of an uniform thickness.

Sheet-lead is of two forts, called cast sheet-lead, and milled sheet-lead.

Solder is charged by the pound, and leaden pipes by the yard or foot running measure.

Sheet-lead used in roofing, guttering, &c. is from 7 to 18lb. weight in each square foot.

Prices.			
New sheet-lead, cast at 71b. weight to the foot,	∡.	.••	d.
per cour. and labour to ditto	I	9	0
Sash weights, per cent	1	9	
Solder, per lb. tod.; or, per cwt	4	13	4
Leaden pipes, ser cwt	1	10	0
Small cast pipe, from half an inch to two			
inches diameter, per foot, from od. to	0	2	10
The new patent copper sheets, coverings, per li			
	==		

#### Painters' Work.

Painters' work is measured by the square yard: and the measuring-line is forced into all the mouldings, and wherever the brush goes. Windows

Υy

Windows are done by the piece, and fash-squares by the dozen.

Chimney-pieces, variegated or fancied colours, &cc. by the foot square.

Ornamental figures, mouldings, &c. by the foot running.

		P	rice	5.					r		ı
Common	pa	i <b>a</b> tir	ıg iı	a oi	l				_	۶.	
Once, per yard	•	•	•	•	•	•	•	•	0	0	3
Ditto, twice .											
Ditto, three times	4	•		•	•	•	•	•	0	0	7
Sash frames, once	in	oil,	rak:	b	•		•	•	0	0	8
Ditto, twice in oil											
Safh fquares once	in	oil,	pèr e	desc	146		•		0	0	8
Ditto, twice .											0
Casements, .					•				•	0	6
									-		_

# Glaziers' Work.

Glaziers take their dimensions in feet, inches, and parts, and compute their work by the square foot.

In taking the length and breadth of a window, the crossbars between the fquares are included; and windows of an oval or circular form are measured as if they were fquare, taking the greatest length and breadth, on account of the waste in cutting the glass.

Prices.	^	_	,
Plate-glass, cut from 1 foot to 2 feet, per feet	۲.	3.	•
superficial	0	5	6
Ditto from 2 feet to 3 feet	0	6	6.
Rest Rateliffe crown glass, per fest freereial .	<u>-</u>		4
•	S	EC.	T.

# SECT. II.

#### OP MEASURING LAND; OR SURVEYING.

Before I proceed to the practice of furveying, it is necessary to mention the instruments used in measuring land.

# 1. Of the Chain.

The chain, called Gunter's chain, confifts of 100 equal links, each link being  $\frac{25}{100}$  of a yard, or  $\frac{66}{100}$  of a foot, that is 7.9s inches long; and the whole chain is 4 poles or 25 yards in length.

An acre of land is equal to 10 square chains.

An acre is divided into 4 equal parts, called roods, and each rood into 40 parts, called perches or poles.

The length of lines measured with the chain are set down in links, as integers, every chain being 100 links in length; therefore, when the content of a piece of land is sound in square links, cut off 5 of the figures on the right hand for decimals, and the rest will be acres: those decimals are then multiplied by 4, to bring them into roods, and the decimals of the product multiplied by 40, for perches, as in the sollowing example:

EXAMPLE. What is the area of a rectangular piece of ground, the length of which is 1300 links, and the breadth 240?

# 2. Of the Plain Table,

This infirmment confills of a plain is tangellar bond of any convenient like, fixed to a familiat three legs, by means of a ball and locker, by which the table is inclined in any direction; it has also a frame of would to fit round in edges, which can be taken off, for the purpole of frame a direct or poper on the table. One tide of the frame is divided into fiveral equal parts, for the purpole of drawing lines a role the paper, and the other tide of the frame is divided into 100 degrees from a centre in the middle of the table, for the purpole of taking angles, &c. There is also a needle and a compals on one tide of the table, to point out the directions, and fix the table in the fame position, with regard to the points of the table in the fame position, with regard to the points of the compass at every remove.

There is an index alio, which is a brais two-frant take, with two open lights, one at each end; thele fights, and ense edge of the feals, are in the fame plane, and that edge as called the fiducial edge of the index.

In thing this table, a fluct of paper is to be wetted and foread fmonth, with the frame of the table prefed down close, to be path paper flendy, which is to remain till it is dry, that it may then hattelf foundly; upon this paper the plan is to be drawn.

In taking a furry of any place, a point is to be made on the paper to denote that that which the table is fixed, which is called the flaces; then in that point his a pin, or one foot of the compalies, and to it apply the fiducial edge of the and be, moving the other part of the index about, till through the lights you preserve one angle of the field you havey, or form other remerkable object; and, from the flation point draw a line along the flation found as a centre, till you perceive another angle, or form other the, till you perceive another angle, or form other the. It among point along the edge of the males, as before, continue to do the fame, till you have dreve lines from the

flation, to reprefent the bearings of as many angles, or objects as may be necessary, and no more; then measure from the flation where the table is fixed to every object which you have viewed, and lay the measures down upon their respective lines on the paper.

If it be required, as it fometimes is, to take a furvey from more than one flation; remove the table, and by the help of the compass, fix the table in the same position as before, and mark another point on the paper, for this second station point; and from thence draw lines to as many objects as smay be necessary, marking the distance from the station as before.

In using the plain table, choose such a point for your station as shall have an object both before and behind the station point, if it be possible: and in moving the table from one station to another, it will be necessary to prove that it be straight in the line towards the object, and also that the distance be rightly laid down on the paper. To know whether the table be set straight in the line, move the table about till through the sights of the index, you can perceive either the fore or back object; then go round the table, and look through the sights at the other end of the index, to see if the other object can be perceived; if it can, the table is in the line, but if not, the table must be shifted according to your judgment.

Fo know if the table be in the right part of the line, that is, if the distance has been rightly measured, six the table in the same position as at first, and lay the index along the station line; then turn the table about, till the fore and back objects appear through the sights, and the needle will point to the same degree as at sirst; then lay the index over the station point, and any other point on the paper representing an object which is seen from the station, and if the same object appears straight through the sights, the station may be depended upon as right, but if not, the distance must be examined and corrected till the said object can be seen.

## Of thifting the Paper on the plain Table.

When the paper is full written, and it is necessary to continue the plan upon another sheet, draw a line through the tarthest point of the last station line, then take the sheet off the table, and fix another sheet on, drawing a line upon it in the most convenient part for the rest of the work; then sold the old sheet back, close by the line drawn upon it; apply the edge to the line on the new sheet of paper, and as they lie in that position continue the last station line upon the new sheet, and also the rest of the measures, beginning at where the old sheet lest off; and so on from one sheet to another. When the work is done, the sheets are to be fastened together into one piece, and the lines in each sheet to be accurately joined together.

It must here be noted, that the faid joining lines upon the old and new shrets, must have the same inclination with regard to the points of the compass.

## 3. Of the Theodolite,

This is a brain circular ring divided into 360 degrees, with an index, with open fights, or a telefcope moveable upon the centre; also a compass to point out the bearings, &c. The whole is fixed by the centre upon a stand.

When this inftrument is used, a field-book is necessary, to note down all meatures, angles, &c. to be remembered when the plan is drawn.

In uting this inftrument, any flation may be taken as a judged most convenient, but it is best to take a flation from which most objects can be feen; and it is necessary at every new station to fix the Theodolite in the fame position by means of viewing the fore and back objects, and the compast; as in uting the plan table; registering in the field-book the number of degrees cut off by the index in viewing each object.

The

The best method of using this instrument is to draw a large circle, quarter it, and mark upon it the number of degrees cut by the index, in viewing each object; then by a parallel ruler, draw from station to station, lines parallel to the lines drawn from the centre to the respective points of the circumference.

# 4. Of the Crofs.

This instrument is only two pair of fights, fet at right angles to each other upon a staff with a starp point to stick in the ground.

The crofs is very useful to measure small and crooked pieces of ground. The method of measuring them is this: measure a base or chief line in the longest direction of the piece, from corner to corner, and, while measuring it, find the places where perpendicular lines should fall upon this line, from the several corners and bends in the piece, with the crofs, by fixing it upon such parts of the line that through one pair of the tights both ends of the line may be seen, and through the other pair of sights, the corresponding angle or angles may be seen, and then measure the length, &c.

There are also several other instruments used in surveying; as the Circumferenter, which resembles the Theodolite both in shape and use; and the semicircle used for taking angles, &c. and the Perambulator, for measuring roads and other great distances, on level ground; it has a wheel of 8½ feet in circumserence, upon which the machine turns, and the distance measured is pointed out by an index moved round by clock-work.

Levels are instruments with telescopes or other fights, used to find levels, or how much one place is higher than another.

The offset-fluit is ten links in length, and uteful for meafuring the offsets and other short distances.

There

There are also various feates used in protracting, and menforing on the paper; as plain feates, protractor, line of chords, line of equal parts, reducing tests, parallel and perpendicular rules, Sec.

But of all the inflroments used in surveying, the plain table is by much the hell, both in point of accuracy and espedition; for by planning every part immediately upon the spot, while the objects are in view, the work is more correct, and a deal of writing is faved in the field-book; it also effords an apparaunity of proving the work at every station; but there are many cales in which some of the other inflroments will be found more proper; and some cales in which no inflrament at all is necessary, but the chain itself, particularly in large open fields lying together.

In farrowing with any inflroment, except the pisin table, force fort of a field book is necessary to note down the neglet, diffunces, &cc. but in ofing the plain table, a book is not requisite, as the whole plan is drawn upon the iput.

This book every perion contrives for himfelf; I fail, however, give the form of one as it is generally used.

Form of the Field-Buok.

Officer and Remarks on the left	Bearings, and Differences	Offices and Roma ch on the right.
21 — Red House 12 Offset 20	10" <b>20</b> 0 24 50 240	Day's hedge.
A tree. A flyle 20	870" 14' 0 30 90 450	20 Brown's pond.

Here, in this fystem, the book is ruled in three columns, the middle one is for the stations, angles, bearings, distances measured, &c. and those columns on the right and lest are for the offsets on the right and lest sides, which are set against their corresponding sigures in the middle column, and also for such remarks as may be necessary to note.

Thus or in the middle column stands for the first station where the angle or bearing is 10° 20'. On the left side against 30 links is an offset of 1s links to the red house. On the left at 0, or the beginning of the principal line, is an offset of 21 links, and on the right of the same day's bedge begins; at 34 on the right an offset to the same hedge of 40 links, and at 50 the same hedge terminates, and at 340 an offset of 20 links on the left.

A line is to be drawn under the work, at the end of every station line, to prevent confusion.

Notwithstanding the field-book is in very general use, yet a more ready method is to draw by hand a rough figure resembling that which is to be measured, and write the dimensions as they are found against the corresponding parts of the figure. This method may be practised in most cases, where the survey is not exceeding large and intricate.

## PROBLEM I.

TO MEASURE A LINE, OR DISTANCE, WITH THE CHAIN.

After having fet up a picket or station-staff at the end of the line to be measured, two persons are to begin the measure at the other end of the line. One person is called the leader, and the other the follower.

The leader, having one end of the chain, proceeds forwards in a firsight line towards the fistion fiast, or object, till he has advanced the length of the whole chain: the follower all the while finding field at the beginning of the line, holding the ring, at the other end of the chain, in his hand. When

the leader has arrived to the end of the chain, he is directed by the follower waving his hand to the right, or left, till the follower less him in the fame line with the mark to be menfored to; then both of them flooping, and firetching the than, the leader the ke an arrow in the ground at the and of the chain the being provided with ten finall arrows for that purpole). The leader leaving the arrow in the ground, as a mark for the follower to come to, advances another chain forward, being directed by the follower, waving his hand as taking, and also by moving himself from fide to fide, till he trings the follower and the fift mark both in one lines having then firetilied the chain, and fluck down another arrow, as before, the follower takes up his arrow, and they both advance another chain length thus they continue to do. till all the ten arrows are in the hands of the follower. and the leader is advanced to the end of the eleventh chain without an arrow; the follower then fends or brings the ten arrows to the leader, and they proceed on as before. Thus, the arrows are changed from the one to the other at the and of every ten chains.

## PROBLEM II.

#### TO TARR AMOUND AND BEARINGS.

(See Fig. s. in Mainwellige)

Let CD be two objects, and let it be required to take the obtainings, or the angle at the Bation CL.

# 1 With the Plain Tuble

The table being covered with a paper, and fixed on its fland, plant it at the flation C, and fix a pin, in the point of the compaffes, in a point of the paper, to reprefer the point C, close by the fide of this point by the fiducial edge of the index, and turn it about, full touching the point C, till one object, D, can be been through the fights, then by the fiducial edge of the index, draw the line C.D. In the very fame

matine,

manner, draw the line C G from the object feen at C, and the angle C G D on the paper, will be equal to the angle measured.

## 2. With the Theodolite.

Turn the inftrument about till you fee the object D through the fights, and there ferew the inftrument fast: then turn the index about, till, through the fights, you fee the object C; then the degrees cut by the index upon the ring of the inftrument will show the measure of the angle.

## 3. With the Chain only.

Measure one chain length, or any other length from the angle, to both objects C and D, then measure the distance DC, and it is done. This must be transferred to paper, by making a triangle GCD, with lengths proportional to the corresponding lengths in the figure.

## PROBLEM III.

## TO SURVEY A TRIANGULAR FIELD.

# 1. By the Chain only.

Let the field to be measured be represented by the triangle ABC, (fig. 1.) then having set up marks at the corners (which is always to be done, when there are no objects to serve as marks) as you measure along the line from A to C, when you have arrived about n, where you judge a perpendicular will fall from the angle B, plant the cross, or any other at instrument; moving it from one place to another, till, through one pair of sights, you can perceive the marks AC, and through the other sights the mark B. Then measure the remainder of the line from n to C, and also the perpendicular n B; thus, having the base AC, and the perpendicular n B, the area is easily found.

Or the area may be found by measuring the three fides of the triangle, as taught in the foregoing tection.

# 2. By taking one or more Angles.

This is done by menfuring any two fides, and taking the single between them, as AB, BC, and the angle B; or, menfuring one fide, and the two adjacent angles, as AB, and the angles A and B.

## PROBLEM IV

TO SURVEY A PIRLO OF POUR SIDES BY THE CHAIR.

Let the field be represented by the four-fided figure ABCG (fig. 1.) measure from A to C, which will be a diagonal, dividing the field into two triangles, ABC, ACG. In measuring along this diagonal line, draw the perpendiculars a B, mG, as directed in the last problem; then find the areas of the two triangles ABC and AGC, and add them together for the area of the trapezium ABCG.

## PROBLEM V.

TO SURVEY A FIELD OF ANY NUMBER OF SIDES BY

Let the field be represented by the figure ABCDEFG (fig. r.) Take a view of the field, and confider how it my best be divided into triangles and trapeziums; and divided into as many trapeziums, and as few triangles as possible. Thus, this figure is divided into two trapeziums; ABCO, GDEF, and the triangle CGD. Then the areas of the two trapeziums are found by means of the diagonals AC, FD, and perpendiculars Bn, mG, Go, p K, so in the last Problem; and the area of the triangle, by the base CG, and perpendicular qD, as in Problem III. The firm of these two trapeziums, and triangle, is the area of the whole field.

Note. The measures of each line may be wrote against the corresponding sides of a similar rough figure, drawn upon paper, or in any other manner.

Figures of this fort are, in fact, divided into triangles; as each trapezium is divided into two triangles.

## PROBLEM VI.

TO SURVEY ANY FIELD WITH THE PLAIN TABLE.

Fig. s. Plant the table at any one angle, as at C, from whence all the other angles can be feen; turn the table about till the needle points to the flower de luce, and there screw it faft: make a point on the paper for C, and then lay the edge of the index to C, turning it about the point C, till through the fights you fee the mark D; and by the edge of the index draw a line DC; then measure the distance from C, where the table is fixed, to the mark D, and lay that distance down on the paper, on the line CD. Then turn the index about the point C, till the mark E can be seen through the fights, and draw the line CE, and measure the distance from the Pation C to the mark E, laving the distance down on the paper, on the line C E: in the same manner find the positions of the points A and B; and lay the lengths of these lines down on the paper, on the line CA, CB: then join the points by the lines CD, DE, EA, AB, BC.

## PROBLEM VII.

TO SURVEY A FIELD BY MEASURING ROUND IT.

Let the field be represented by figure ABCDEF (fig. 3.) Having set up marks at the angles AB, &c. plant the instrument at any point A, and turn it till the fixed index be in the direction AB, and there serew it fast; then turn the moveable index to the direction AF, and the degrees cut off will be the measure of the angle A: measure the line AB, planting the instrument at B; and there in the same manner

obtain the angle B; then menfure BC, and observe the angle C; then measure the distance CD, and take the angle D; then measure DE, and take the angle E; then measure EF, and take the angle F; and lastly, measure the distance FA.

To prove the work p-add all the inward angles ABC, &c. together; and if the work be right, the fum will be equal to twice as many right angles as the figure has fides, except four right angles; but when there is an angle that bends inwards, as at F, and you menfure the outward angles, fubtrack it from four right angles, or 360 degrees, and the remainder will be the inward angle.

# Otherwife;

Instead of taking the inward angles, you may take the outward angles, by producing one fide of each angle further out, as feen in the figure: and if the fum of all the outward angles be equal to 360 degrees, or 4 right angles, the work is right; but when one of the angles runs inwards, as F, subtract it from the sum of the rest, and the remainder will be 4 right angles.

## PROBLEM VIII.

## TO SURVEY A FIELD WITH CROOKED HERGES.

Let ABCDE be the shape of the sield, (fig. 4.) Set up marks within the field, at a b c d, dividing it into as few sides as possible. Then begin at any station, as at a, and measure along the imaginary lines a b, b c, c d, d a, taking the offset as you mensure along the lines, at a, m, u, o, p, &c. either with the offset staff, or any other instrument; which are to be added to the area of the figure. The area is found either by measuring a diagonal from b to d, with perpendiculars to a, &c. or by taking the angles at the four corners a, b, c, d, as before directed.

Note. The area of the offsets is found either by the rule for finding the area of a triangle; or taking the mean measure of the perpendiculars, for the mean distance of the hedge: thus, the offset from o to B sorms a triangle whose perpendicular is p. But that from B to D must be measured by adding the two perpendiculars together, and taking half the sum for the mean distance of the hedge from the line bc, which is to be multiplied thereby.

If the measurement be taken outside the offsets, they must then be subtracted from the area,

#### PROBLEM IX.

TO SURVEY ANY PLACE BY TWO STATIONS.

Let the place to be measured be represented by the heptagonal figures ABCDEFG (fig. 5.); plant the plain table at m, for the first station; then turn the table about, till through the fights you perceive n, the other station. Draw the line mn on the paper, along which lay the fiducial edge of the index, and then screw the table fast; turn the fights round m, to all the objects ABC, &c. successively, drawing a dry line by the edge of the index to each, as m A, m B, &c. Next, measure the distance on the ground from m, the first fation, to n, the other station, and there plant the table, and lay that distance down on the paper, on the line mn; then lay the index by the station line mn, and turn the table about, till through the fights you perceive the other station m. and there screw it fast. Lastly, direct the fights succes-Evely to all the objects ABC, &c. as before, drawing lines. from each, as n A, n B, &c. and the intersections of these lines with the former at the points ABCD, &c. give the place of the objects, or bounds of the figure.

The same method must be pursued in surveying with the theodolite, or any other instrument for taking angles; mamely, measuring the distance mn, planting the instrument first at one station, then at another; placing the fixed sights

in the direction min, and directing the movemble lights to every object, noting the degrees, cut off at each time.

Their abservations being planned, the intersection of the

lines give the bounds of the figure, as before.

It all the objects cannot be feen from two flations, then more flations may be used; always measuring the diffuser from one flation to another, placing the inflrument in the same position at every flation, and from each fistion observing every object that can be seen from it, by taking its angular position; till the place of every object be determined by the intersections of two or more lines—the more lines the better.

The flations may be taken either within the bounds of the figure, or in one fide, or at a diffrance, and without the bounds of the figure.

large effates, without entering them; or a furvey may be taken of a country, or any parts of a country, by taking two flations, on two towers or entirences.

#### Remarks.

fary, always measuring the distance from station to station in a right line. In measuring any of the station distances, mark where these lines meet with any ditches, hedges, roads, rivulets, or other remarkable objects, by measuring the distance from the station line, and where the perpendicular from it cuts that line; and as you measure along any main station line, take the offsets to the ends of all hedges, and to any pond, house, rivulet, &c. and be careful to set up marks at the intersections of all hedges with the station line, that you may know where to measure from when you come to survey these particular places. By such means all you flation lines are to be measured, and the situation of all places adjoining to them determined.

- a. The inner parts of the furvey must be determined in like manner, by new station lines; taking inner stations at those places where you have the greatest command or view. Measure these station lines as before, and note all the interfections with hedges or other objects. Thus you may furvey the adjoining fields, by taking the angles that the fides make with the station line at the intersections; and measure the distances to each corner from the intersections; for every station line will be a basis to all the future operations, the situation of all parts being entirely dependant upon them; therefore the flation lines should be as long as possible, and fhould be so contrived as to run along the hedge, or bound of some field, or to pass through some angle. These things being adjusted, you must take more inner stations, and divide and fubdivide till you come to fingle fields, repeating the fame work at the inner flations as at the outer ones; and take notice how one field lies by another, to place them properly in the draught.
- 3. When an estate is so situated that one part cannot be seen from another, it must be divided into two or more parts, and each part surveyed separately, as if they belonged to different owners; and at last join them together in the plan.
- 4. In laying the lines of distances down upon the paper, it is necessary to have a scale of a proper length. For this purpose, you must take the length of the whole estate in chains, and consider how many inches in length the map is to be, and from these you may know how many chains there must be in an inch on the scale; thus, if the length of the estate be see chains, and the map is to be so inches in length, a decimal scale should be used; and each inch on the map will contain to chains in length, a tenth of an inch, I chain, &c.
- 5. When the stations are long, a good instrument should be used for taking angles: and the plain table may be used for the inner stations, as it is a quick and ready instrument.

6. When the draught is finished, place all the trees, and every other remarkable object, in their proper fituation.

#### PROBLEM X.

#### TH BURTET A LARGE TRACT OF LANDS OR A COUNTY.

- t. In choosing your stations, let them be on the top of some eminences; as, high hills, mountains, towers, church steeples, &c. and such as command the greatest view, and can be seen from each other; and as far distant from each other as possible. Raite a beacon, or stag, of a different colour, at each, to be visible from the other stations.
- 2. Plant flugt allo at each of those places you should distinguish in your plant flxing them upon the tops of church steeples, houses, &c. and changing them to other places when necessary.
- 3. Then from one flation take all the angles between the other flation and each of those marks, observing the different colours of the flags, and note them down in the plans from the other flation take all the angles between the first flation and each of the former marks, and note them down in the plan also against the same coloured mark; if it be receitary, the angles may also be taken from a third flation, which will fixe to prove the work, if the three lines interfest each other in the same point. The informment for taking angles must be an exceeding good one. A circumstruction is the best of four or five feet radius with telescopic tights.
- 4. It is not needlary to measure every diffance, because any flationary line being exactly laid down from any teals, all the other lines will be proportional to it; but cometimes it is needlary to measure the diffance of a place in miles and in measuring long diffances, it will not be exact enough to measure along the high roads, by reason of their windings; but the best way is, to measure in a straight line, over hills and dales, and all obstacles, it possible; but where it is not possible.

pedible, such parts must be measured by the method of measuring insteadible distances. A good compass is also necessary, to show the bearing of the two stations, and to direct you to go straight when you do not see the stations.

- 5. From all your flations, and in the whole progress, he wary careful in observing all remarkable objects; as, towns, caftes, churches, windmills, rivulets, bridges, &c. &c.
- 4. Flaving taken your observations from the main stations which command the whole country, then proceed to take inper stations, as in surveying large astates; and from these new stations determine the places of as many of the remaining towars as you can; and if any remain, the situation of which you cannot take, take more inner stations; and thus proceed through all the parts, taking one station after another as long as is necessary.
- 7. Lastly, take the position of the station line, with regard to the points of the compass, by an astronomical process, as follows: hang a plumbet in the sun, over some part of the station line, and when the shadow of the plumbet line runs along the station line, at that moment take the sun's altitude; then, having his declination and the altitude of the place, the azimuth will be found by spherical trigonometry; for the azimuth is the angle which the station line makes with the meridian: and thus the meridian may be drawn through the map.

## PROBLEM NI.

## TO SURVEY A TOWN, OR CITY.

The proper instrument for this purpose is the plain table; as the distances are not very great, and every part should be laid down while in fight.

Take the first station at the meeting of two or more of the principal streets, in order to get the longest station lines, then draw the lines of direction to represent these streets having chosen objects, measure the streets, and lay the meafures down from a scale, on the lines on the paper, taking offsets with the flaff, to all bendings and windings in the flates, and to all remarkable objects; then take another fation in one of the foregoing lines, and repeat the process.

Thus, (fig. 6.) having chosen A for the first station, draw two lines in the direction of the two streets meeting there; and measure AB, marking the street on the lest, and lay the same measure down on the plan: let B be the second station, from which draw the directions of the streets meeting there measure from B to C, noting the ends of the streets at n and as you pass them; and lay the same measure down on the plan. At C, the third station, take the direction of the street meeting there, and measure from C to D. At D, the near station, do the same, and measure DE, noting the cross street p; and in the same manner take the directions of all the principal streets, laying the measures down upon the plan. Then proceed to the next smaller streets; and lastly, to the lanes, alleys, courts, &c. using the same process throughout the whole.

Note. In taking the furvey of a town there is no necessity for having objects fixed up, as there are generally mark enough to ferve as objects; fuch as the doors or windows a houses, &c.

# OF PLANNING, CASTING UP, AND DIVIDING.

## PROBLEM L

TO LAY DOWN THE PLAN OF A SURVEY.

When the furvey is taken by the plain table, a rough dra of the plan is already drawn on the paper; but where the furvey is taken with any other influment, the plan is to be drawn from the nicafures taken in the furvey; first, a roug draft is to be drawn on paper, in which all the lines at angles must be laid down in the fame order in which the

were taken in the furvey; laying down first the angles, then the lengths of the lines, with the places of the offsets; then the offsets themselves. All these should be done with dry or obscure lines; then a black line drawn through the extremities of all the lines, and the offsets will be the bounding line of the whole plan.

After the principal lines and bounds are laid down, proceed to mark the smaller objects, till every thing be laid down that is necessary.

The north fide of the map or plan is commonly placed uppermoft. And in some vacant part a scale of equal parts must be drawn. All hills must be shadowed, and all hedges coloured with different colours; all hilly grounds should be drawn like broken hills and valleys: soot-paths are represented by single dotted lines, and roads by double ones.

In taking large furveys, all oblique lines, fuch as are measured up and down hills, must be reduced to straight lines, by making a proper allowance; for which purpose there is generally a table engraved on some of the instruments.

## PROBLEM II.

#### TO CAST UP THE CONTENTS OF A FIELD.

This is no more than what has been taught in the first section of this chapter, for finding the contents of figures whether there be triangular, square, four sided, polygonical, or circular figures, by the proper rules there delivered; then, having found the area in links, after you have cut off five figures on the right hand, the remainder is acres. The five separated figures are to be multiplied by 4 for roads, and five figures cut off from this product are to be multiplied by 40 for perches.

In pieces of land bound by winding hedges, in measuring the offsets, all the parts between the offsets are accurately measured separately, like small triangles or trapezoids; but sometimes Kuneumes fuch pieces are measured by finding a mean breadth, which is done by dividing the fum of the affacts by the number of them, accounting that for one where the boundary meets the flation line, and the quotient is the mean breadth: but this last method is not very exact.

that in very large furveys, and where there are many helds, the both way of finding the contents of the whole is to make a rough plan of the whole, and duide it into feveral trapesiums and triangles, and find the area of each departely, and add them together; then, to prove the work, divide the whole ethate into as few triangles or trapesiums as publible, by drawing new lines in the plan; and if the commutatound by this last method be equal to the contents found by the former method, the work is right; but if they differ, the work must be examined and recomputed till they marrly agree.

But the chief difficulty in calling up the contents arina from the fides of the figure being curved, or of any other irregular fhape; in which case such hounds of the figure must be reduced to straight lines, in the following manner; make a finall how with a piece of horse-hair, and whalehone, or case or any other elattic substance, which will keep the horse-hair extended at full thretch; then apply the horsehold to the crooked bounds of the figure, in such a manner, that those parts of the curve which are on one fide the hair may be equal to the parts of the curve on the other tide the hair; then, by making two points, draw a thraight line in the direction of the horsehold, which will be a thraight fide to the agure, equal to the curve one. Do the same by every curve tide of the figure; thus the figure may be reduced into a right-lined figure.

#### PROBLEM III.

TH TRANSFER A PLAN FROM ONE PAPER TO ANOTHER

There are reveral methods of performing this; four of which I thall mention;

First. Rub the back of the plan over with black lead powder, and then lay the black side upon the sheet of paper on which the plan is to be copied, keeping it sleady; then with a blunt point of a tracer, trace over all the lines in the plan, pressing the tracer so, that the black lead on the back of the paper may be transferred to the clean paper; then take off the plan, and you will see all the marks on the clean paper in black lead, which must be traced over with a pen and ink, &c.

Secondly. The plan may also be transferred to another paper, by dividing both ends and sides of the plan into any convenient number of equal parts, connecting the corresponding points of division with lines; which will divide the whole plan into a number of squares, or parallelograms; then divide the paper upon which the plan is to be drawn into the same number of squares or parallelograms; next copy the parts contained in the squares of the old plan, in the corresponding squares of the new one. (See figures 40 and 41.)

Thirdly. Another method is by the instrument called a pentagraph, which will copy the plan in any fize required.

Fourthly. The best method of any is the following: fix the old plan on the front of a copying frame of glass, with the face uppermost, (which is a large square of the best window glass, set in a broad stame of wood, and constructed so as to be raised up to any angle whatever), with the clean paper on the face of the old plan being sixed to the stame by several pins; then the frame being raised up facing the window, by means of the light shining through the paper, you will perceive every line of the plan through the clean paper, which is to be drawn thereon with a pencil; having copied that part which covers the glass, the other part is to be brought over the glass, and copied as before, and so on throughout the whole.

Then

Then take them afunder, and trace the lines with pen and link; and finish the piece, writing such names as are necessary.

Thus the finest plan may be copied without the least in-

The foregoing rules will be found fully sufficient to infirmft any ordinary capacity in all the practical parts of Mensuration and Surveying.—I have avoided every thing that favours more of curiosity than real utility.

## SECT. III.

# OF SOLID MEASURE, MEASURING TIMBER, DIGGING, AND GUAGING.

## Definitions.

- 1. Solids are fuch bodies that have length, breadth, and thickness.
- 2. A prifin is a folid body whose ends are finitlar and equal plain figures, and its sides are parallelograms. It is called a triangular prism when its ends are triangles (as sig. 1. in the solids); when its ends are squares, a square prism; when pentagons, a pentagonal prism, &c.
- 3. A cube is a square prism, having fix equal square sides perpendicular to each other, (Fig. 2.)
- 4. A parallelopipedon is a figure having fix rectangular fides; each two opposite fides being equal, and parallel. (Fig. 3.)
- 5. A cylinder is a round prilm, having two equal ancles for its ends. (Fig. 4.)

- 6. A pyramid is a figure that has a right-lined figure for its base, and each of its sides is a triangle, whose vertices meet in a point at the top, which is called the vertex of the pyramid, as A (fig. 5.) The pyramid takes its name from the figure of its base, like the prism.
- 7. A cone is a round pyramid, having a circular base. (Fig. 6.)
- 8. A sphere is that solid body bounded by one continued convex surface, every part of which is equally distant from the centre. It may be supposed to be formed by the revolution of a semicircle about its diameter. (Fig. 7.)
- 9. The axis of any folid is a line drawn from the middle of one end to the middle of the opposite end. Thus the axis of a pyramid is a line drawn from the top, or vertex, to the middle of the base; and the axis of a sphere is a line drawn through the centre. When the axis is perpendicular to the base, it is a right prism, or pyramid; otherwise it is ablique.
- 10. The height or altitude of a folid is a line drawn from the vertex, or top, perpendicular to the base.
- 11. If the bale of a prifm or pyramid be a regular figure, it is called a regular prifm or pyramid; but if the bale be irregular, the prifm or pyramid is called irregular.
- 12. The fegment of a pyramid is a part cut off the top by a plane, parallel to the base, as CE, (fig. 6.)
- 13. A frustum, or trunk, is the part that remains after the fegment is cut off, as EA, (fig. 6.)
- 14. A zone of a sphere is a part intercepted between two parallel lines.
- 15. The fegment of a fphere is a fegment less than a hemisphere, or half sphere; like a cone, whose base is the same as the base of the fegment, and whose vertex passes through the centre of the sphere.
- 16. A circular spindle is formed by the revolution of the fegment of a circle, about its chord, which remains fixed. (Fig. 8.)

- 17. A regular body is a folid, contained under a certain number of equal and regular plain figures.
- 18. The faces of a folid are the plain figures under which it is contained.
- vio. There are only five folid bodies which are regular, i.e. which have each fide equal and fimilar: namely, first, the tetraedron, which is a regular pyramid, having four triangular faces. Second, the hexaedron, or cube, which has fix equal square faces. Third, the octaedron, which has eight triangular faces. Fourth, the dodecaedron, which has twelve pentagonal faces. Fifth, the icosaedron, which has twenty triangular faces.

Note. As square measure is greater than running measure, so cubic measure is greater than square measure.

## The Table of Cubic Measure.

1728	Inches make 1	Foot
27	Feet 1	Yard
. 1661	Yarda1	Pole
64000	Polea 1	Furlong
	Furlongs 1	_

#### PRØBLEM I.

# TO FIND THE SOLIDITY OF A CUBE, PARALIELOPIPEDON, PRISM, OR CYLINDER.

The folidity of any of these figures is found by the following rule:-

RULE. Find the area of one end of the figure by the rules for finding the area of a superfices in the foreging fection, and multiply such area by the length of the figure, and the product is the folid contents.

EXAMPLE

EXAMPLE 1. What is the content of a triangular prism, whose 3 sides are 3, 4, and 5 feet, and length 10 feet?

Here the three fides of the triangular end are added together, and from the half fum each fide is subtracted separately, and the remainders, and half sum multiplied continually together: then the square root of the product is the superficial content, as taught in the foregoing section; which, multiplied by the length, gives the folid content.

Cubes, parallelopipedons, and cylinders, have their folid contents found in the fame manner.

Lms. What is the folid content of a cylinder, whose length is so feet, and circumference 5\frac{1}{2} feet? Answer 48.1459.

#### PROBLEM II.

TO FIND THE SOLIDITY OF A CONE OR PYRAMID.

Rule. Multiply the area of the base by the height, and one third of the product will be the content.

EXAMPLE 1. What is the folidity of a cone, whose height C D is so feet, and diameter A B of the base 3 feet? (Fig. 6.)

Example a. What is the folid content of a pentagonal pyramid, the height whereof is in feet, and each fide of the bale a feet?

1.780477 Tab. area.

6.881908 Area base.
One third of the height.

87.587638 Answer.

## PROBLEM III.

TO FIND THE SOLIDITY OF A SPHERE OR GLOSE.

Rule. Multiply the cube of the axis by .5830.

Example 1. What is the folidity of a fighere or globe, whose axis or diameter is 18 feet?

#### PROBLEM IV.

# TO FIND THE BULDITY OR SUPERFICIES OF ANY REGULAR BODY

# 1. For the Superficies.

RULE. Multiply the tabular area taken from the follow table of furfaces by the fquare of the linear edge of the folid.

## 2. For the folid Content.

Multiply the tabular folidity by the cube of the linear edge.

Surfaces and Solidities of regular Bodies.

No. of Sides.	Names.	Surfaces,	Solidities.
4 6	Tetracdron Hexacdron	1.73205	0.11785
8	Octaedron	3.46410	0.47140
18	Dodecaedron	40.64573	7.00312
80	Icofaedron	2.00025	2.18169

EXAMPLE 1. If the linear edge of the tetracdron be 3 feet, what is its furface and folidity?

0.11785	1.73205	Square of the edge.
. 17 Cube of the edge	9	
H#495	15.58845	
<b>3570</b>		
3.18195 Aniwer.		

28.8. What are the superficies and solidity of the octaedron, whose linear side is a feet? Answer, superficies a 3.85640, and solidity 3.47120 feet.

2n. 3. What are the superficies and solidity of the icosaedron, whose linear side is a inches? Answer, superficies 10.64100, and solidity 17.45352 inches.

## PROBLEM V.

TO FIND THE CONVEX SURFACE OF A CYLINDER, OR THE UPRIGHT SURFACE OF ANY PRISM.

RULE. Multiply the circumference by the height, and the product will be the answer.

length is so feet, and dismeter a feet? Answer 125.664 feet.

## PROBLEM VI.

. THOS THOUGH A 40 BURARUS REVIOUS BHY GHIE OF

Rule. Multiply the rircumference of the bafe by the flant height, or length of one fide; and half the product will be the furface.

Example 1. If the diameter of the hale be 4 feet, and the fide of the come to feet, what is the convex furface?

3.1416	
914448	Circumference. Half of the height.
47.1240	Amheri

## PROBLEM VII.

ARDIO NO ANAROS A TO TOATROS KATAOO ARE UZIT OF

Reve. Multiply the diameter by the circumference, and the product will be the antiver.

Brancis i. What is the fireface of a globe, whole diameter is 12 inches?

In the lame manner the convex furface of any some, or fegment of a tiphere, is found a vis. by multiplying the height of the some or figment by the whole circumference of the liphere.

29. 8. What is the superficies of the earth, its diameter being 79572 miles, and the circumference \$5000 miles? Answer 198,943,750 square miles.

## PROBLEM VIII.

TO FIND THE SOLIDITY OF THE SEGMENT OF A CONE.
OR PYRAMID.

The fegment of a cone, as C & (fig. 6.) or of a pyramid, may be confidered as an entire cone or pyramid; and the folidity or superficies is found in the same manner, and therefore need not be repeated,

#### PROBLEM IX.

TO FIND THE SOLIDITY OF THE FRUSTUM OF A CONS.
OR PYRAMID.

RULE 1. Multiply the mean area of the end by the height of the frustum, and the product will be the solid content.

8. The mean area of the ends is found by one of the following rules :---

Add the areas of the two ends, and the mean proportional between them together, and one third of the fum will be the mean area.

Or, when the ends of the pyramid are regular plain figures, the mean area is found by multiplying one third of the tabular number belonging to the polygon (in the table of multipliers, in the fuperficial measure) by the fum arising by adding together the square of a side of each end, and the product of the a sides.

In the fruitum of a cone, the mean area is found by multiplying the fum of the squares of the two diameters, added to the product of the diameters, by 12618, or one third of 17854.

But

But if the circumference be taken instead of the diameter, the multiplier will be .02654.

EXAMPLE 1. What is the content of the frustum of a cone, whose height is 20 inches, and the diameters of the two ends 12 and 10 inches?

Greater diameter	12	less diameter	10	19
Square of greater diameter Square of less diameter Product of the two diameters	144 100		100	180
•	364 2618 2912 364	•		
21 72		¥.		
	20	Mean area, Height. Answer.		

EXAMPLE 2. What is the content of a pentagon frustum whose height is 50 feet, each side of the base 3, and each side of the less end 2 feet?

Mar. 3. What is the folidity of the fruffum of a cone, the height of which is 25 feet, the circumference at the greater end 20, and the less and 10 feet? Answer 464,205 feet.

20.4. What is the folidity of an hexagonal fruitum, the height being 6 feet, the fide of the greater end 18 inches, and that of the lefs 12 inches? Aufwer 24.681722.

#### PROBLEM X.

## TO FIND THE SUPERFICAL CONTENT OF A BOARD OR PLANK.

RULE. Multiply the length by the mean breadth,

Note. When the board is tapering, add the breadths of the two ends together, and take half the fum for the mean breadth.

EXAMPLE 1. What is the superficial content of a board, whose length is so feet 3 inches, and mean beadth 10 inches?

By Decimals,		$B_y D$	HOL	lecim	als.	
		Feet.		Incl	ıcs.	
80.85		80	••	3		
10				10		
18)803.50	Answer	16	••	10		6
16.875 Answer.	•		-		==	

When the board does not run regularly tapering, but is broader in some parts than others; take several breadths and add them together, and divide the sum by the number of them, and the quotient will be the mean breadth.

## PROBLEM XI.

TO FIND THE SOLID CONTENT OF SQUARE OR FOUR-SIDED TIMBER,

RULE. Multiply the mean breadth by the mean thickness, and that product by the length; and the last product will be tolid content.

Note. If the timber taper regularly from one end to the ther, the mean breadth and thickness is found either by 3 C measuring

measuring the middle of the piece, or by taking half the sum of the two ends.

But if the timber does not taper regularly, take feveral dimensions, and divide their sum by the number of them, for the mean breadth, or thickness.

EXAMPLE 1. What is the folid content of a piece of timber, the length of which is so feet 6 inches, the breadth at the greater end a feet 3 inches, and at the less end 1 foot 6 inches; and thickness at the greater end a feet, and at the less end 1 foot 9 inches?

Decimals.		Duodecimals.			s,
9.95 1.5		9 I	3		
4)9.75		2)3	Q	_	
1.475	mean breadth	1	10	-	
1.75		1	9		
2)3.75 1.875	mean thicknetic	3)1	10	7	
1.875 9.375	mean breadth	1	10	6	
13125 13125		i	6	9	_
1875		_		11	
3.515 625	length	1, 08	6	•	,\$
17 57 8145		70	., ()	9	0
74.0701 185	Answer	73	Ö	10	- i

28. 2. What is the content of a piece of timber, the length of which is 20.38 feet, and its ends unequal figures, the fide of the greater being 101, and the fide of the lets 91 feet? Antwer 29.838 feet.

## PROBLEM XII.

#### TO FIND THE SOLIDITY OF ROUND TIMBER.

The common rule, is to multiply the square of the quarter girt, or one quarter of the mean circumference, by the length; and the product will be the content.

The quarter girt is a geometrical mean proportional, between the mean breadth, and thickness; that is, the square root of their product: unskilful measurers use the arithmetical mean instead of it, that is, half their sum, but this occasions a very great error in the contents, and particularly when the breadth and depth differs much from each other.

When the round timber or tree is tapering, take the mean dimensions from the dimensions of each end, as in the foregoing problem, either by girting it in the middle for the mean girt, or half the sum of the two ends; but when the tree is irregular, find the content of each part separately.

Note. This rule gives the contents about  $\frac{1}{4}$  lefs than the true quantity, so that it makes an allowance for hewing the tree square. But when the true quantity is required, it is found by the next rule.

EXAMPLE 1. What is the content of a piece of round timber, being 9 feet 6 inches long, and its mean quarter girt 3 feet 6 inches?

Decimals.	Duodecimals.				
3.5	quarter gir	3	6		
<u>3.5</u>		10	4		•
105		I	2		•
1 <b>3.2</b> 5 9.5	length	12 9	3		•
612 5		110	3	6	
116.37 5	content	116	4	6	` •
	3 C 2				PROBLEM

#### PROBLEM XIII.

TO FIND THE CONTENT OF A TREE, OR ROUND PIECE OF TIMBER, MORE EXACTLY.

RULE. Multiply the square of  $\frac{1}{2}$  of the mean girt by twice the length, and the product will be the contents.

EXAMPLE. What is the content of a tree, the length of which is 9 feet 6 inches, and mean girt 14 feet?

Decimals.	•	Duo	deci	mals	•
2.8	of mean girt	2	9	7	
2.8		2	9	7	
22 4		5	7	2	
56		2	I	2	
			I	_7	
7.84	fquare of $\frac{1}{4}$ of mean girt - twice the length -	7	9	II	
19	_				
70 56	Answer	148	8	5	٠
784		==		=	
148.96	Answer.				

## PROBLEM XIV.

TO FIND THE DEPTH, BREADTH, OR LENGTH OF ANY VAULT, CELLAR, RESERVOIR, &C. TO BE MADE.

RULE. Divide the folid content by any one of the three dimensions (viz. length, breadth, or depth), and the quotient will be the product of the two other dimensions.

EXAMPLE. What will be the length and breadth of a fquare refervoir of water, to contain 5000 cubic feet of water, and the depth to be 20 feet?

<sup>\*</sup> The answer by duodecimals is less in this question than the truth, as all the parts could not conveniently be concluded in the operation.

Qs. 2. A bowling-green, 300 feet long and 200 feet broad, is to be raifed one foot higher by the earth to be dug out of a ditch that encompasses the green, and is 8 feet in breadth; to what depth must the ditch be dug? Answer 71 feet.

# Of Gauging.

Gauging is most commonly performed by the sliding rule, or gauging rod. But I shall here give the practice of it, as wrought by calculation of the common measures only.

By gauging is always understood the method of finding the content of any hollow vessel, and is mostly used for finding the content of casks, coppers, &c.

The rule is to find the content of the veffel in inches, and divide them by 282, if for ale gallons; and by 231 for wine gallons; because 282 cubic inches contains an ale gallon, and 231 cubic inches is a wine gallon. But if any prefer multiplication to division, when the solid content is found, it may be multiplied by .003546 for ale gallons, instead of being divided by 282; and by .004329 for wine gallons, instead of being divided by 231; for dividing by 282 or 231 is the same as multiplying by these vulgar fractions  $\frac{1}{237}$  or  $\frac{1}{237}$ ; and the above multipliers are the decimal fractions, equal to these vulgar ones.

In veffels of a circular or eliptical form, to obtain the content in inches, it is necessary to multiply by .7854, and then to reduce them to ale or wine gallons. Therefore to multiply by .7854, and then divide by 282, or 231, is the

fame as to multiply by the fraction  $\frac{(a_{11}^{4})}{2a_{11}^{4}}$  or  $\frac{(a_{11}^{4})}{2a_{11}^{4}}$ , and the decimal fraction equal to their vulgar ones are .0027851 for ale, and .00339999 for wine.

#### PROBLEM XV.

#### TO GAUGE A CASK.

There are feveral methods of gauging casks according to their shapes, or the curvature of the sides, of which there are four general forms, but the content of any of them may be found by the following general rule:

RULE. To the square of twice the middle diameter add the squares of the head and bung diameters. Multiplying the sum by  $\frac{1}{4}$  of the length, and that product multiplied or divided by the circular multipliers or divisors, will give the contents 1 or multiply the squares of the diameters by the length of the case, and that product again by .0004\$ for ale gallons, or by .0005\$ for wine gallons.

EXAMPLE 1. Required the contents of any cash, whose length is 40 inches, the bung diameter being 32, the head diameter 24, that between the bung and head 282 inches.

57.5		2 ‡		<u>.</u> ; e
57.5		5 1		1,2
28.5		gn		64
4 22 5		48		gh
2471		576		11324
1:00 27				
10.14				
5*0				
400000				
4 1				
1969 (0			10h2ço	
.000 4 i			.00054	
18,100			481240	
11.8.11			130893	
91.5811	Gallons.		111.4081	Winc.

PROBLEM:

## PROBLEM XVI.

TO FIND THE CONTENT OF ANY CASE, FROM THREE DIMENSIONS ONLY.

RULE. Add into one fum 39 times the square of the bung diameter, 25 times the square of the head diameter, and 26 times the product of the two diameters: then multiply the sum by the length, and that product by .00034, and divide the last product by 9 for wine gallons, and divide by 11 for ale gallons, or multiply by .000311 for ale.

EXAMPLE. What is the content of a cask, whose length is 40, the bung diameter 32, and head diameter 24 inches?

32	24	32
32	2 ‡	24
<del>32</del> 64	95	128
96	48	64
1024	576	768
39	25	26
9216	2880	4008
3072	1152	1536
39036	14400	19968
	39936	<u> </u>
	19968	
	74304	
	40	
	2972160	2972160
	•00034	.00003Tr
	11888640	8916480
	8916480	270196
Wine gall	9)1010.534.10	Ale 91.86676 gallons.

## PROBLEM XVII.

TO ULLAGE A STANDING CASK\*.

RULE. Add together the square of the diameter at the

<sup>\*</sup> The ullage of a cask is what it contains when only partly filled, and it is confidered in two positions; namely, either flunding on its end with its axis perpendicular to the horizon, or as lying on its side with the axis parallel to the horizon.

furface of the liquor, the square of the diameter of the nearest end, and the square of double the diameter taken in the midway between the other two; then multiply this sum by the length between the surface of the liquor and the nearest end, and multiply the product again by  $.0004\frac{3}{2}$  for ale gallons, or by  $.0005\frac{3}{2}$  for wine gallons, in the less part of the cask, whether empty or filled.

EXAMPLE. The three diameters being \$4, \$7, and \$9, what is the ullage for ten wet inches?

24 29 54 2916 24 29 54 841 96 261 216 576 48 58 270 4333 576 841 2916 10 	ne.
4,339	
•0001	
173320	
173320 28886	
Ale 20.2206	
A1C 20.2200	

#### PROBLEM XVIII.

#### TO ULLAGE A LYING CASK.

Rule. Divide the wet inches by the bung diameter, and find the quotient in the column of verfed fines in the table of circular fegments at the end of this section, taking out its correspondent fegment; then mutiply this fegment by the whole content of the cask, and the product again by 14 for the ullage required.

EXAMPLE. If the bung diameter be 32 inches, and content 92 ale gallons, what is the ullage of 8 wet inches?

32)8(.25, whose tab. seg. is .153546

92

307092

1381914

14.126232

2 is 3.531558

Answer 17.657790

ATABLE

Of the Areas of the Segments of a Circle,
Whose diameter is Unity, and supposed to be divided into
One Thousand equal Parts.

Height.	Area Seg.	Height.	Area Seg.	Height.	Area Seg.	
1001	*000042	'027	.005867	.053	-016007	
1002	000119	1028	.006194	1054	1016457	
1003	*000219	1029	.006527	.055	1016911	
1004	*000337	1030	.006865	.056	.017369	
200	.000470	'031	1007209	.057	.017831	
.000	810000	.032	1007558	.028	1018296	
1007	'000779	.033	1007913	1059	.018766	
800	120000	1034	.008273	.060	1019239	
.000	.001132	'035	.008638	100.	.019716	
'010	'001329	.036	800000	-062	.020196	
110	'001533	'037	1009383	.063	.020680	
1012	1001746	*038	.009763	.064	.021168	
*013	.001963	.039	.010148	1065	.021659	
1014	*002199	.040	.010537	.066	.022154	
.015	'002438	140	1010931	.067	.022652	
.016	1002685	'042	.011330	.068	'023154	
'017	'002940	.043	*011734	.069	.023659	
810.	.003202	1044	1012142	.070	.037108	
'019	1003471	1.045	.012554	'071	.024680	
'020	*003748	.016	.012971	'072	.025195	
120	.004031	.047	.013392	.073	.025714	
.022	'004322	.048	.013818	.074	1026236	
.023	.004618	'049	.014247	1075	.026761	
.024	1204001	.040	189410.	.076	.027289	
.025	.005230	.051	.012110	.077	.027821	
.026	.005546	1052	.015561	1078	.028356	

## THE AREAS OF THE

Height.	Area Seg.	Height.	Area Seg.	Height.	Area Seg.	
·e79	-028894	114	*049528	149	1073161	
.080	.029435	1115	1050165	.120	1073874	
180*	*029979	.116	1050804	151	.074589	
.082	1030526	1117	1051446	1152	1075306	
.083	.031076	-118	1052000	1153	1076026	
.084	1031689	*119	1052736	1154	*076747	
280.	1032186	120	285550.	1.155	1077469	
.086	1032745	-121	.054036	1156	1078194	
.087	.033307	122	.054689	157	126870	
.088	1033872	123	*055345	1158	.079649	
.089	1034441	1124	.026003	.120	.080380	
.090	110250.	1125	:056663	.160	.081113	
1001	.035585	1126	1057326	.161	.081846	
1092	1036164	127	*057991	1162	·08258a	
.093	.036741	1128	1058658	163	083380	
1094	.037323	1129	'059327	164	.084020	
'095	.037909	130	.029999	-165	1084801	
1096	.038496	.131	.060672	.166	.085544	
'097	1039087	132	.061348	167	.086289	
.008	.039680	*133	.062026	.198	.087036	
.099	.040276	*134	1062707	.169	.087785	
.100	.040872	1135	.063389	170	.088535	
101	.041476	.130	.001014	171	.089282	
102	.015020	137	.004760	*172	,000011	
103	.042682	.1.18	.062444	173	.000202	
104	*043296	139	.000140	174	'091554	
105	.013908	.140	.040833	175	.003 113	
106	.014222	.141	.067528	176	.003024	
107	.042130	.113	.068222	.177	.003836	
108	'C45759	143	068924	178	094601	
100	.040.381	.144	069625	179	.095366	
110	.011002	145	070328	.180	,000134	
111	.047632	146	1,50160.	.181	,0069003	
112	048262		147170.	182	.007674	
113	.048804	148	072450	183	098447	

## SEGMENTS OF A CIRCLE.

	<del></del>				
Height.	Area Seg.	Horekt.	Area Seg.	Height.	Arra Seg.
184	.099221	1919	127285	*254	
.184	1099997	1220	.188113		157019
1.86	100774	188	128945	·255 ·256	157890
.182	.101253	.422	129773		159636
188	108334	-263	130005	*457 *458	1160510
.180	103116	.884	131438	59	161386
.100	103900	.225	132278	-566	162863
191	104685	.326	133108	.361	163146
1293	105478	.997	133945	-868	164019
193	106661	.938	134784	.863	164899
194	107051	.289	135684	.864	165780
1.195	107843	.830	136465	.365	166663
1:06	*108636	.831	137307	.866	167546
197	100430	.838	138150	-267	168430
198	*110886	.833	138995	.268	169315
1.199	111024	·934	139841	.869	170202
.800	111893	·\$35	140688	.270	171089
108.	1112624	1236	*141537	271	171978
1606	113426	237	142387	.272	172867
.803	114830	1238	143238	*273	173758
*804	1115035	1239	144091	*874	174649
.802	115842	1240	144944	275	175542
-800	.119920	241	145799	976	176435
1.807	117460	.242	146655	277	177330
1208	118271	.843	1147518	278	178225
1809	119083	'244	148371	.279	179125
.B10	119897	1945	149830	.280	.180010
.311	120712	*846	11 50091	184	.180018
-918	.18123	'247	1150953	-282	.181812
4813	*122347	.348	1151816	1283	182718
414	123167	'249	152680	.284	183619
1.812	123988	.8 20	153546	285	*1845\$1
.816	.184810	1251	1154412	.889	185485
Z18.	185634	.323	155280	.887	186319
.318	126459	253	1156149	.888	187834

THE AREAS OF THE

Hoight.	Area Seg.	Haght.	dieabig.	Height.	Area Seg.
.880	.188140	*324	1220404	1359	1853590
.000	189947	.325	'331340	360	18 54550
1991	189955	.336	.338277	1.361	255510
1898	190864	.327	.283816	1361	1850471
1893	191775	.328	1884154	1.363	· 67433
.894	193084	.329	188 (093	164	12 58395
.295	193596	330	1226033	1365	1859357
1846	.194200	1331	.836974	106	1260380
*897	195482	332	1227915	367	*\$61884
104	1196337	'333	·ss8858	368	.epse48
.299	11978 58	334	1.829801	1.369	1.863213
.300	1.108198	.335	1230745	370	1664178
.301	1199085	1.336	.831689	.371	1265144
.308	1800003	337	1.232634	378	.200111
1303	1800038	.338	.233580	373	1967078
1.304	1.301811	'339	1234516	374	1.808042
.302	1802761	.340	235473	1375	1869013
1306	1.304683	1441	1246421	1.376	1260981
1.307	1304605	1, 142	1237369	1177	1370951
1368	1206527	1444	124-418	1.378	127 1920
.300	1.206421	1144	123,7268	1.379	· · 372890
. 110	1807 476	1.145	1.54 15118	i ilio	.37 1861
1311	1308 401	y 346	1.441160	վ⊹յենն	.774838
1312	1200227	1347	.345191	, tha	1.275803
1314	1310124	148	1243074	144	: 1276775
1114	्र :क ा 108क	1349	.3.14080	1.484	1277748
1.312	.818311	1,480	12440hi	185	. 278721
1.319	1212940	351	1245951	456	170004
1.117	1.81182T	11:353	1.246880	144	Book Bard
1318	.814HO3	1153		thii	251048
1.410	1815733	11154		1,80	1.383012
.340	1.8 1.00.00	1355	1249757	.400	-26 G02
.431	1817599	1356		7771	1284,03
1328	1.81823	1357	1251671	11/2	28,544
121	Softing.	1.358	1377011	1.494	12150521

## SEGMENTS OF A CIRCLE.

<u> </u>	<del></del>				
Height.	Area Seg.	Height.	Area Seg.	Height.	Area Seg.
*394	.287498	.430	.322928	.466	-358725
395	·s88476	'431	323918	.467	359783
.396	189453	432	1344909	468	360781
397	1890432	<b>'433</b>	12 5000	.460	361719
.398	1291411	434	326892	470	362717
'399	1993390	435	1327882	471	.363715
400	1893369	·436	1328874	.472	364713
'40I	1294349	437	1329866	473	305713
1408	1295330	+38	.330828	474	366710
.403	116968	+39	.331850	475	.367709
'404	1897898	1440	*332843	.476	1368708
1405	*298573	.441	•333836	.477	1369707
.400	.899822	.443	. 334829	.478	1370706
407	<b>'300\$38</b>	443	*3358==	479	1371705
408	1301280	144+	1336816	.480	1372704
.409	.302203	445	.337810	.481	373703
410	.303182	.446	138804	.483	374703
411	.30+121	1447	1339798	1483	175702
418	,302122	.448	.340103	.484	376702
413	.300140	*449	*341787	1485	1377701
414	*307185	1450	1342782	.486	1378701
415	,308110	.421	1343777	.482	1379700
416	,300002	.123	*344772	.488	1380700
417	1310081	453	1345768	.489	.381699
418	311068	.454	.346764	.490	.382699
419	1312054	1455	*347759	.401	*383609
'480	'313041	.456	·348755	'41)2	.384600
48,1	314029	457	1349753	*493	1385699
428	315016	.458	.350748	494	.386699
493	1316004	1459	'357745	.492	1387699
484	316992	1460	352742	1496	388699
425	1317981	.461	1953739	1497	·389699
486	'318970	.462	354736	.408	1390699
497	1319959	1463	355732	1499	.391699
428	320948	.464	.356730	.200	·39 <b>26</b> 99
1.489	.381038	.162	· 357727	·	

In this table the diameter of the circle is 1, and the whole area '785, 98; the figures in the columns of heights are the height of the fegment, or the verfed fine of half its are; and those in the columns of area segments are the areas of the circular segments, whose heights stand on the left hand in the column of heights.

The use of this table is to find the area of any segment of a circle, by the following rule:

Rule. Divide the height of the given fegment by the diameter of the circle, and the quotient is the height of the fegment; and opposite this height, in the table, is the tabular area, which is to be multiplied by the square of the diameter, and the product will be the area of the segment.

EXAMPLE. What is the area of a fegment of a circle, whose height is 5 inches, and the diameter 20 inches?

Note. In dividing the given height by the diameter, if the quotient does not terminate in three places of decimals, then the area for that fractional part ought to be propertioned for as follows:

Having found the tabular area, answering to the first three decimals of the quotient, take the difference between it and the next following tabular area; which difference, multiplied by the fractional part remaining, the product will be the correspondent proportional part, to be added to the first tabular area.

Thus in the last example the quotient is 166, and there is a remainder of \(\frac{1}{4}\), the tabular area of the segment is

.085544 .086289	
3745 248	The difference
496	3 of the difference
.086040	The true tab. area

### SECT. IV.

#### OF INSTRUMENTAL ARITHMETIC.

Infrumental arithmetic is the method of calculation by inftruments made for that purpose, for a quicker dispatch of business, and for the help of those who are deficient in common arithmetic. The most common instruments are, the carpenter's rule, Coggesball's sliding rule, Gunter's line, the gauging rule, and the diagonal rod.

- a foot in length, connected together by a joint: one fide of this rule is divided into inches, and eighths of an inch; on the fame fide are also several plane scales, divided into twelfth parts by diagonal lines, for planning dimensions in feet and inches.
- s. On the other fide of this rule, on one piece, are fet all the principal lines, which are on Coggeshall's sliding rule; namely, four lines marked A, B, C, and D respectively; the two middle ones being on a slider, which runs in a groove.

Thefe

THE STREET PROPERTY AND ADMINISTRATION OF THE SECRETARIES.

Their four lines are logarithmic lines; the three marked A, B, C are all equal; and are called double lines, because the numbers for upon them run from 1 to 10, twice 1 the boxett line D is a tough line, the numbers running from 4 to 40. It is called the girt line, from its use in easting up the contents of trees, and timber. This line also may be used for gauging; as upon it, at 17:13, is marked W.O. and at 18:03. A.O. to the wine and ale gauge points.

Upon the other part of this tide is a table of pounds, thillings, and pence, thowing the value of a load, or so subject of turber, at all prices from tispence to two thillings a foot.

In the use of those lines it must be strictly observed, that when one at the beginning of a line is accounted unity, then the time the middle of the line will stand for 10, and the to at the end of the line will stand for 10, and when the tat the beginning of the line stands for 10, the 10 in the middle of the line will stand for 100, and the 10 at the end of the line 1000, 80, and all the intermediate divisions are altered in proportion.

The edge of the rule is divided decimally, each foot being divided into an hundred equal parts: by this meature dimentions are taken in feet, and decimals of a toot, which is by much the bett way.

4. Counter's line is a line of figures, exactly the fame as the three tingle lines on the corporer's rule, and therefore needs no turther description. Its me is to multiply, or divide numbers, to perform the rule of three direct, &c. It was formedly let by itself on the carpenter's rule.

The figures 1, 4, 4, &c. tometimes thand timply for the infelies, at other times their figurify 10, 30, 30, &c. agains at other times 100, 300, &c. or 1000, 3000, &c.

4. The gauging rule terves to compute the contents of cuke, or any other vellels, after the dimensions have been taken. It is a figure rule, with log orthone lines on the fides, having this cities a function in grocers in three of the fides.

Upon the first face of this rule are three lines: two, marked A and B, for multiplying and dividing; and one, marked M D, for malt depth, as it serves to gauge malt. The middle line B is upon a stider, and is a double line, marked at each edge of the slider, like that on the carpenter's rule: these three lines are all of the same radius, or distance from 1 to 10, each line containing twice the length of the radius. A and B are numbered exactly alike, and the numbers may be increased, or decreased at pleasure: thus the first number 1 may either stand for an unit, 10, or 100, &c. or 1, or .01, or .001, &c. but whatever the first number is, the middle number will be ten times as much, and the last number 100 times as much, as on the carpenter's rule.

The 1 on the line M D is opposite \$15 on the other lines, which are the cubic inches in a malt bushel; and the divisions on this line are numbered retrograde to those of A and B.

Upon the lines A and B are feveral other marks and letters: thus, on the line A are M B, for malt bulkel, opposite the aforesaid number 2153 and A, for ale, opposite 282, the cubic inches in an ale gallon; and upon the line B, opposite 234, is W, for wine, the cubic inches in a wine gallon; also S I, for square inscribed at .707, which is the side of the square inscribed in a circle, whose diameter is 1: and S F, for square equal, at .886, being the side of a square equal to the same circle: also C, for circumsterence, at 3.1416, which is the circumsterence of the same circle.

Upon the fecond face, which is that opposite the first, are a slider, and four lines marked D, C, D, E, at one end, and at the other end marked root, figures, root, cubic; the lines C and E, containing respectively the squares, and cubes of the opposite numbers of the lines D, D; the radius of the line D is double to that of C, and triple to that of E; so that whatever the first one on D denotes, the first on C is the square of it, and the first on E the cube of it; thus, it D begins with 1, C and E will begin with 10, which is the square of 10, and E with 1000, the

cube of 10, and so on. Upon the line C, at .0796, is marked a c for the area of a circle, whose circumference is 1; and a d at .7854, for the area of a circle, whose diameter is 1. Also upon the line D are W G for wine gauge, at 17.15, and A G for ale gauge, at 18.95; and M R for malt round, at 52.32; these three being the gauge points of round and circular measure, and are found by dividing the square roots of \$31.282, and \$150.4 by the square root of .7854; also M S for malt square is marked at 46.37, the malt gauge point for square measure, being the square root of \$150.4.

Upon the third face of this rule are three lines, one marked N upon the slider; and two upon the stock, marked S S and S L, for fegment standing and segment lying, which serve to ullage standing and lying casks.

Upon the fourth face are a scale of inches, and three other scales, marked first variety, jecond variety, and third variety; the scale for the fourth variety being on the inside of the slider on the third face; the use of these lines is to find the mean diameter of casks of each of the sour different forms or shapes of the sides.

Befides those lines, there are two others on the infide of the two first sliders, being continued from one slider to the other; one of these is the scale of inches, from 12\frac{1}{2} to 36, and the other a scale of ale gallons between the corresponding numbers 435 and 3.61, which forms a table to show, in ale gallons, the contents of all cylinders, whose diameters are from 12\frac{1}{2} to 36 inches, their common altitude being 1 inch-

5. The diagonal rod is a square rule, commonly sour feet long, and solding together by joints; this instrument is used both for gauging casks, and computing their contents; and this is performed by taking one dimension only; namely, the diagonal of the cask, that is, the length from the middle of the bung hole to the meeting of the head of the cask, with the stave opposite the bung hole; and is the longest line within the cask from the middle of the bung. On one face of this rule is a scale of inches to take this diagonal by, opposite.

which are placed the areas, in ale gallons, of circles to the corresponding diameters, in like manner as the lines on the under fide of the three sliders in the sliding rule.

On the opposite face are the scales of ale and wine gallons, to show the contents of casks, from having the diagonal. All the other lines on this infirument are the same as those on the sliding rule, and to be used in the same manner.

## The Use of the Carpenter's Rule.

#### PROBLEM I.

#### TO MULTIPLY NUMBERS TOGETHER.

Suppose the two numbers 24 and 12; draw the slider out, till 1 on the line B is opposite to 12 on the line A; then against 24 on the line B stands 288 on the line A, which is the product of the two numbers.

Note. In any operations, when a number runs beyond the end of the line, feek it on the other radius, that is, the other part of the line, which will be the tenth part of the required number.

#### PROBLEM II.

#### TO DIVIDE NUMBERS.

To divide 312 by 24; draw out the slider till the divisor 24 on B be opposite to the dividend 312 on A, then against 2 on B stands 13, the quotient on A.

#### PROBLEM III.

TO SQUARE ANY NUMBER.

Suppose to square 12: set 1 on the line B to 12 on A, then against 12 on B stands 144 on A.

#### PROBLEM IV.

#### TO EXTRACT THE SQUARE ROOT.

Set 1 or 100, &c. on C to 1 or 10, &c. on D; then against every number found on C stands its square root on D.

PROBLEM



Next, let 100 on B to the referved number on A, and against the whole content on B will be found the ullage on A.

There are many folid figures besides the foregoing, the contents of which cannot be found by any actual dimensions taken on the figure, such as slatues, &c. The contents of such bodies are found by immersing them in water, and measuring the rise of the water occasioned by such immersion.

## SECT. V.

#### A VIEW OF THE FIVE ORDERS OF ARCHITECTURE.

The origin of architecture is almost contemporary with that of civil society. When mankind felt the inclemencies of the weather, and, consequently, found the necessity of creeting habitations for shelter, case and convenience soon improved itself into ornament and grandeur. A few trees perhaps growing round in a circle, and leaning together at the top, afforded the first habitations, being interwoven with twigs, and plaistered over with mud. This gave rise, in after ages, to the idea of columns.

It is probable that the inconvenience of these habitations rendered their owners desirous of inventing such, that should answer every purpose of the former fort, and possess several advantages above those: this improvement naturally gave rise to the invention of the cross beams to support the roof; for this purpose, they had, no doubt, recounse to the trunks of trees: thus columns were at once introduced.

which one cone, LON, has its vertex O in one point of an object; and the other cone, LFN, has its vertex F in that point of the object. The middle line OF is called the axis of that pencil, (fig. 5.)

## SECT. L.

#### OF VISION.

Direct vision is the faculty of fight, and is occasioned by the rays of light proceeding from an object, and passing through the humours of the eye, where they form the image of the object on the back part, or bottom of the eye. In order to understand which, it will be necessary to explain the figure and construction of the human eye.

ABCE is the eye. It is of a spherical figure, by which means it is easily moved any way in its socket, by muscles appointed for that purpose; the fore part at A (fig. 1) is more convex than any other part. The eye is enclosed in three membranes: the outermost is called the Sclerotica; the second, the Tunica Choroides; the fore part of which is called the Iris, which consists of many fibres, like so many radii: the third membrane, or innermost coat, is called the Retina, which is nothing but the optic nerve, spread over the bottom of the eye: upon this membrane the images of visible objects are formed.

In these three membranes are contained the three humours of the eye; the sirst, HAI, is called the aqueous humour,

humour, which is a thin watery liquor; the fecond, FGO, is the cryfalline, in the form of a double convex lens, and more convex in the back part: behind this is the vitreous humour KL.

The cryfialline is more dense than the vitreous, and the vitreous more dense than the aqueous humour: the three humours together form a compound lens, which refracts the rays of light, iffuing from an object PR, to the bottom of the eye; and there paints its image pr, upon the retina, in an inverted position.

The aqueous humour is in the form of a menifcus; as is also the vitreous humour. The fore part of that membrane called the sclerotica is called the cornea, as at A, and that part adjoining is called the white of the eye. Within the cornea is that coat called the wora; in the middle of this is a hole O called the pupil, to let in the rays of light: this pupil is contracted or dilated by several muscular fibres, in order to let in more or less light, as found convenient.

D is the optic nerve, which, coming from the common fenforium in the brain, is expanded all over the concave back furface of the eye, and thus forms the retina. This nerve is not fituated in the middle of the eye, but lies nearer the fide E, in that part next the nose.

The crystalline FG has a ring of fibres round its edge, by which means it can be drawn more or less convex, and the distance AC is thereby made greater or less, in order to form the image pr, upon the retina, for distinct vision. This ring of fibres is called the Ligamentum Ciliare, the back part of which is black, in order to stille the rays which fall upon it. The eye is moved in the head by several muscles in the sclerotica.

If the image of an object do not fall upon the retina at pr, the vision will be confused; if it fall short, or nearer F G, as is the case with short-sighted people, then a concave lens that makes the rays more diverging will bring it to the retina.

If the rays of light do not unite, so as to form the image of the object, till they get beyond the retina, as is the sase with most old people, then a common convex lens of a proper form will make them converge sooner, and so form the image upon the retina; therefore long-sighted people must use convex glasses; and short-sighted people concave ones.

The ray of light P p, flowing from the point of the object P, and the ray R r, flowing from the point R, crofs each other at O, and proceeding in the same straight lines, point the image of the object P R on the retina, in an inverted position, as p r.

Note. Though the rays of light are in the figure reprefented by fingle lines, yet it must be observed that every visible point of the object sends forth a pencil of rays, which cross each other at O, and paint the image of the object on the retins.

There are many experiments made by philosophers to demonftrate the truth of this theory of vision; the most common of which is the following:—take a bullock's eye, while it is fresh, from a newly killed beast, and having out off the three coats from the back part, quite to the vitreous humour, put a piece of paper behind that part, and hold the front of the eye towards any bright object, and there will be an inverted image of the object upon the white paper; which in this case serves as a retina to the eye.

Though the image of the object is inverted in the bottom of the eye, yet we judge it to be creet, being always used to that position of the object. By an attentive perusal of the figure, the position of the object, with regard to that of the mage, may be easily accounted for. Thus, to view that point of the object P, the pupil of the eye at O must be turned upwards towards A, in order that the ray P p may fall on the axis of the eye, opposite C, where alone distinct vision is performed. And to view that point of the object R, the pupil of the eye must be turned downwards, to take

in the rays of light R r, fo that r may fall on the axis of the eye at C.

The diameters of objects are proportioned to the diameters of the images at the bottom of the eye: thus, the angle POR is equal to the angle pOr.

Some of the most common properties of the eye are the following:

- 1. The eye co only see a very small part of an object distinctly at once; therefore the eye must be turned successively to the several parts of the object, that each part may fall in or near the axis of the eye.
- a. When an object is feen diffinelly with both eyes, the axis of both eyes are directed to that point; thus the object appears fingle, though it be feen by both eyes at once; but if the fixes of both eyes are not directed to the fame point of the object, it will appear double.
- 3. Few eyes can diffinguish a particle of matter, that subtends, at the eye, an angle less than half a minute; and very few can distinguish it when it subtends a minute. If the distance of two stars in the heavens be not greater than this, they will appear as one.
- 4. The eyes of young people are more convex than those of old people; and this is the reason the former can see an object nigher than the latter.
- 5. The eyes of fhort-fighted people are too convex to admit of diffinct vition, when the object is placed at the diffunce of fix or eight inches, which is the common diffunce of an object for diffinct vition. And the eyes of long-fighted people are not convex enough to admit of diffinct vition at that diffunce. In the former case, the rays of light converging from an object through the humours of the eye, unite too soon, and before they reach the retina: to remedy which concave glasses are used, which render the rays more diverging. And in the latter case the rays of light do not unite soon enough, in their passage through the eye, to paint the image on the retina: the remedy of which is the convex glasses.

- 14. The REFLECTION of rays is their regrets, or returning from the turface of such bodies, on which they fall, and cannot enter: thus, the rays AB falling on the surface CD, is reflected or turned back again in the direction E. (Fig. 6.)
- 15. Minnons, or Speculums, are those bodies whose furfaces are so very smooth, as to be impervious to the rays of light which fall on them; and which, therefore, they reflect, so as to represent the images of the objects exposed to them; they are generally made of metal, highly polithed, or of glass polithed on one tide, and silvered on the other; and are either plain, convex, or concave.
- 16. PLAIN MIRRORS are those whose surfaces are perfect planes, and whose section is a right line, as CD (sig. 6); these are vulgarly called looking glasses.
- 17. Convex Merrors are those whose surfaces do every way equally rise above the plane of their bases; the section of these fort of mirrors is a curve, and is either circular, eliptical, parabolical, or hyperbolical. ACD (sg. 4.) is a circular section; and the mirror is the segment of a globe, or spherical surface, which is that mostly used.
- 18. Concave Mirrors are those whose surfaces sink down with an uniform hollowness below the upper parts; whose section also is a curve, as various as the convex; but the circular form is the most common.
- 19. REFRACTION of rays is their being bent, or turned out of their course, in passing out of one medium into another: as the ray BC (fig. 2), in passing into the dense medium AIHD, is refracted, or turned out of its natural course CK, in the direction CE, which is called the retracted ray.
- eo. The Incident RAY is that which comes from any object, and falls on the refracting or reflecting furface, as BC (fig. s), or AB (fig. c).

the space within two miles of it, every way, with luminous rays of light, before the tenth part of a grain of its matter is consumed.

The velocity with which the rays of light proceed from the furface of a body is surprising. The method by which the swiftness of the rays of light was determined first, was by an observation on the eclipses of Jupiter's satellites. These eclipses appear to us about seven minutes sooner than the precise time, when the earth is situated in that part of its orbit, between the sun and Jupiter; and the eclipse appears about seven minutes later, when the sun is between him and us: from which it is plain, that the rays of light require about seven minutes to pass through a space equal to the distance between the sun and us; that is, about ninety-sive million of miles.

The rays of light proceeding from a visible body, as they proceed in all directions, and extend themselves upwards and downwards, as well as sideways, must necessarily become thinner and thinner; and that they do, in proportion to the squares of their diameters from the luminous body; that is, at the distance of twice a certain space they are four times thinner than at the distance of one such space; and at the distance of three times such a space, nine times thinner; and so on.

## Of Refraction.

All light proceeding from any luminous body, without being reflected from any opaque substance, or instected by passing very near one, is always found to proceed in straight lines. But if the rays pass obliquely from one medium to another, they always leave the direction they had before, and assume a new one; and this change of direction is called their rafraction: and after having suffered this refraction, they again proceed in straight lines, till they meet with a different medium, when they are again turned out of their course.

The phenomena of refraction are occationed by an attractive power in the medium, through which the light passes.

When When a ray of light passes out of a rarer into a dealer medium (if the latter has a greater attractive some than the former, which is mostly the case) the ray, just before to entrance into the dealer medium, will begin to be attracted towards it; and this attraction will continue to act upon the ray rill some time after it has antered the medium. When a ray enters the dealer medium obliquely, its direction will also become less oblique to the surface of the medium; and approach nearer to a perpendicular, drawn through the forface of the medium.

But when the ray of light paffer from a denfer into a race medium ubdapally, its direction will be made, more oblique to the furface of the rarer medium; and depart furface from a perpendicular drawn through the furface of the carer medium.

the air into the dinfer medica. ADHI; at entering the dinfer medium at the point C, it will begin to be attracted towards that medium, which attraction will change its course from the direction C K to that of C F. Let FG be a perpendicular drawn through the denter medium; then L will be the fine of the angle of refraction, and M N the fine of the angle of incidence is always proportionate to the fine of the angle of refraction in the fame medium.

From this property of reheafting rays of light arifes the magnifying power of the glass lends used in optical influences. For the rays of light proceeding from any object are too diverging to admit of dainer vision at a less diffunce than from 6 to 8 inches; it, therefore, by interpoling a glass lens between the eye and the object, the object can be viewed at a less diffunce, the rays of light, proceeding from the object, will be made to converge to a point fooder, and by that means the object will be feen under a larger angle.

Thus,

Thus, let O (fig. 10) be an up of ct to be viewed by the eye at F; which object, to be viewed by the naked eye, must be removed to the distance of fix inches at least from the eye. But by interposing a lens, whose focal distance is an loch and an half, the eye will have distinct vision of the object at the distance FO; consequently the object will appear magnified four times in diameter, to what it would do to the naked eye. And the object appears under the angle IFM.

If an object AB (fig. 9) be placed in one focus of the lens DE, and the eve in the other focus F, the eye will fee just to much of the object as is equal to the diameter of the lens: for the rays AD and BE, which go from the extremaies of the object to the extremities of the lens D E, and are united at the focus F, must necessarily proceed from the abled to the lens, parallel to the axis FC, and to each other; therefore, the part of the object AB, from by the rays DF, E. F., will be equal to the diameter of the lens. If only one part de of the lens be open, then only so much of the object AB as is equal thereto, will be feen by the eye. Now as AB is equal to DE, or ab to de: the angle DFE, or If e, is the optic angle; that is, the angle under which the part of the object A B, or ab, appears to the eye at F; and as GF is supposed but half the distance of CF; the angle DFE, or dFe, is double to that under which the part AB, or ab, would appear to the naked eve at the distance F C; thus the eye fees the object twice as large in diameter through the lens, as it would do without it.

If it be required to see a part of an object larger than the lens, the eye must be placed nearer the lens than its focus. Let the lens be D (sig. 8) its two soci F and C. In the focus C, let there be an object AB larger than the lens: suppose the rays AD and B proceed from the extremities of the object to those of the lens, then by the lens they will be converged into the point K, between the lens and its focus F:

then, if the eye be placed at K, it will fee all the object A B. which is larger than the lens.

But if the eye be placed further from the lens than its real focus, it can never fee any object, or part of an object, at once, near so large as the lens, but always smaller. Let the eye be placed at 1, beyond the focus F; it will then only see the part of the object G H, which is less than the lens.

Thus it is evident that the nature of a convex lens is fuch, as will render an object diffinctly visible to the eye at the diffance of its focus. The reason why these lenses are used as microscopes is exceeding plain; for if the diffance FI (fig. 10) be fix inches, which is the least diffance an object can be seen by the naked eye, and the focal diffance of the lens c F two inches, then the object O will appear three times magnified in length, as I M; and if it were the surface, it would be magnified nine times; and the solidity or bulk twenty-seven times.

If the focal distance F c of the lens be one fourth part of an inch, then will that be but one twenty-fourth part of six inches, the distance of naked sight: and so the length of an object feen through such a lens will be magnified twenty-four times; the surface sive hundred and seventy-fix times; and the solidity this teen thousand seven hundred and twenty-four times; for those are the square and cube numbers of twenty-four.

## To find the principal Focus of any Lens.

Hold the lens perpendicularly against the rays of the sun, or a candle; hold a white paper behind it, to receive the refracted rays, which will make a round white spot upon the paper; move the paper backwards or forwards, till this spot, which is the image of the sun or candle, be the least possible, there six the paper; then the distance of the paper from the lens is the focal distance required, or the burning point.

Or, fecondly. Cover the fide of a lens with a paper, having feveral small holes made in it with a pin; and placing the lens directly against the beams of the sun, or a candle, and the light passing through the holes will form so many white spots upon the paper held behind it. Move the paper backwards and forwards, till all the spots coincide in one. That point is the socus; and the distance of the paper from the glass is the focal distance.

I shall here give some of the most general propositions and properties in the science of optics, leaving the process and demonstration for the exercise of the reader.

- 1. Wherever the rays, which come from all the points of an object, meet again in so many other points, to which they converge by refraction, there they will make a picture of the object upon any white body on which they fall.
- s. Rays flowing from all points of an object, and passing through a lens, paint the image of the object in the real focus of the lens, and may be seen there upon a white paper: or without the paper, the image may be seen hanging pendulous in the air, by an eye placed six or eight inches behind the focus.
- 3. The object, and its image made by a lens, subtend equal angles at the lens.
- 4. The length of an object is to the length of the image made by a lens, as the distance of the object from the centre of the lens is to the distance of the image from it.
- 5. A convex lens magnifies an object, when it is nearer than twice the principal focal distance; but if further off, it lesses it.
  - 6. A concave lens always diminishes an object.
- 7. The apparent magnitude of an object is the angle under which the object appears to the eye.
- 8. If the object and its image be both on the same fide of, the lens, the image will be erect; but if they be on different sides, the image will be inverted.

- 9. When the object and its image are on different fides of the lens, as the object approaches the lens, the image recedes from it; or, if the object recedes from the lens, the image approaches it.
- 10. It the object and image be both on one fide of the lone, and the object move towards the lone, the image also moves towards the lone; and if the object moves from it, the image also moves from it.
- 11. In a convex lone, if the object be further off than the principal focus, its image will be on the other fide of the glass, inverted. But if the object be nearer than the principal focus, the image will be on the same side of the glass, erect.
- 12. In a concave lens, the image and object are always on one fide of the lens.
- 13. If an object be placed in the principal focus of a lens, its apparent magnitude at any place whatever, beyond the lens, will be invariably the fame 1 and equal to the apparent magnitude, when feen from the centre of the lens, with the naked eye.
- 14. The apparent magnitude of a body, placed in the principal focus, will always continue the fame, however the eye is moved backward or forward, from the lens.
- 15. The nearer the eye is to the lens, the more of the object appears, and the tarther off the eye is from the lens, the lefs of the object is from.
- 16. If the object he nearer than the principal tocus, its apparent magnitude becomes lefs, in going from the glaffitut if the object he further than the focus, the apparent magnitude will increase, in going from it.
- 17. If the eye be fixed in the principal focus, the apparent magnitude of an object will be invariably the fame, wherever the object is placed before the glass.
- 18. If the eye and object be fixed, and a convex lens be moved from the object to the eye, the apparent mag-

mende

nitude of the object increases to the middle, and then decreases to the eye. When it comes into such a position that the eye and object are conjugate foci, the object is infinitely confused.

- 19. If the eye and object be fixed, and a concave lens be moved from either of them to the other; the apparent magnitude of the object will decrease to the middle, and then increase again. The apparent distance is reciprocally as the apparent magnitude; and, in general, we judge the apparent distance of an object to be the very same, as we suppose the real distance of an object to be, from which the rays come to our eyes, with the same degree of confusion.
- so. Converging rays are made more converging by a convex lens: and diverging rays are made more diverging by a concave.
- at. Parallel rays falling on one fide of a convex lens will be refracted to the focus on the other fide. But parallel rays falling on a concave lens will, by retraction, diverge from the focus on the fame fide.
- as. In a convex lens, rays diverging from the focus will emerge parallel on the other fide.
- \$3. In a concave lens, rays converging to the focus will emerge parallel, going out of the lens on the fame fide.
- s4. In a double convex lens of equal radii, the principal focus is distant from the lens, the radius of the iphero, of which the lens is a fegment.
- as. When the lens is a perfect sphere, the principal focus is distant from the lens half the radius.
- a6. When the lens is an hemisphere, the principal focus is distant four thirds of the radius, when the convex side is exposed to the rays; and twice the radius, when the plane side is exposed.
- s7. When the lens is a plano-convex, the distance of the focus is equal to the diameter, or twice the radius of the sphere when the plane side is exposed to the rays. But when

the convex fide is exposed to the rays, the focus is distant twice the radius, except two fifths of the thickness.

- 28. In double concaves of equal radii, the principal focus is distant the radius of the sphere; and it is virtual.
- so. In a plano-concave, the principal focus is distant twice the radius; and is virtual.
- 30. If the radiant point and the focus be equidifiant from a lene, they will each of them be distant twice the principal focal distance.
- 31. If the radiant point be nearer the lens than the principal focus, the rays after refraction will diverge; but if the radiant point be in the principal focus, they will after refraction emerge parallel; and if the point be farther off than the focus, the rays will converge after refraction.
- 33. The distance of the radiant point and its focus, made by a convex lens, is the least possible, when they are equidistant from the lens.
- 33. If a convex lens be held directly to the rays of the fun, and a combustible body be held in the principal focus; the heat of the rays of the fun, converging to a point in the focus, will fet the body on fire.
- 34. The heat of the focus of the lens is, to the fun's direct heat, as the area of the glass to the area of the image in the focus.
- 35. The degrees of heat in the foci of different lenfes are as the fquares of the diameter directly: and the fquares of the focal diffances reciprocally.

The foregoing propositions contain all the phenomens of refracting lenses; and may be proved for the most part by actual experiments.

It is necessary just to observe, for the sake of those who may use lenses of a different medium, that different mediums have different refracting powers: I shall, therefore, give a table of the refracting power, as given by Sir Isaac Newton, and proved by many later experiments.

In the first column are the names of the bodies; in the fecond column, the sines of incidence and refraction; in the third column, the refracting power; in the fourth column, their density, or specific gravity; in the fitth column, the ratio.

Bodies.	Sines of I and Ref		Refialling Power.	Deafigy.	Ratio.
Pieudo topaz	23	:4	1.699	4. 27	0. 39
Air	3201		0. 000025	0.0012	. 52
Glass antimony	17	9	2. 568	ζ. 28	.48
A felenitis	6 i	41	1.213	2.252	. 54
Glais	3 t	20	1.4025	2. 58	. 54
Rock crystal	25	16	1.445	2.05	. 54
Island crystal	Š	3	1. 778	2. ;3	. 65
Sal gemma	17		1.388	2. 143	. 64
Alum	35	2+	1. 1267	1.714	.65
Botax	22	15	1. 1511	1.714	.67
Nitre	38	2:	1.345	1.9	. 70
Vitriol	303	200	1.295	1.715	.75
Oil vitriol	10	7	1.041	1.7	.61
Rain water	520	396	0.7845	1.	. 78
Gum Arabic	31	<b>`2</b> 1	1. 179	1. 375	.85
Spirit wine	100	73	0.8765	o. 866	1.01
Camphire	3	2	1.25	0. 996	1.25
Oil olive	22	15	1. 1511	0.913	1.26
Linfeed oil	40	27	1. 1948	0. 932	1.28
Spirit turpentine	25	17	1. 1626	0.874	11. 32
Amber	14	9	1.42	1.01	1. 36
Diamond	100	41	4.049	3.4	1.45

From this Table it appears, that those bodies which contain oily sulphurous particles differ from the constant ratio, and have a greater refractive power.

#### SECT. II.

#### OF SINGLE AND COMPOUND MICROSCOPES.

SINGLE microscopes are such that have but one lens; and may be constructed in an infinite variety of ways. I shall give the forms of a few of the most useful.

A (fig. 10, plate () is a circular piece of wood, metal, or ivory, in the middle of which is a finall hole, c. Upon this hole is fixed, by means of a wire, a glass spherical lens, of one tenth of an inch radius, whose focal distance is cD. At the focus D is a pair of plyers DE, fixed upon a fliding screw B. and which opens by means of the two ftuds a, e: these plyers ferve to hold any small object O, which is to be viewed through the lens by the eye, placed in the other focus F: and according to the focal distance of the lens, the object will be more or less magnified, as before described: thus, in a lens of this radius: viz. one tenth of an inch, the focal distance of which is a radius and an half from the centre thereof, as described in the foregoing propositions; the length of an object, by fuch a lens, will be magnified forty times; the furface, one thousand fix hundred; and folidity, fixty-four thousand times. For a radius and an half of such a sphere, or zo of an inch, is only the fortieth part of fix inches, (the least distance of naked vision;) the square of 40 is 1600, and the cube of 40 64000. This infirument, from its fize and portability, is very convenient. The best lenses for these single microscopes are, however, those whose focal distance is three tenths, or four tenths of an inch.

Again, when the diameter of a spherical lens is only one twentieth of an inch, the object will subtend an angle at the eye as great as if it were only three eightieths of an inch, (which is the one hundred and fixtieth part of fix inches) diffant: therefore, the length of an object feen through fuch a lens will be magnified one hundred and fixty times; the furface, twenty-five thousand fix hundred times; and the folidity, four million and ninety-fix thousand times; which is so great a magnifying power as to surpass conception.

But spherule lenses, of so small a diameter as the latter, are of no use but in viewing transparent objects; for if an opake object were to be viewed by such a lens, the eye must be applied almost close to the surface of the lens, by which the lens and object would be so over-shadowed, as to render an opake object too obscure to be viewed.

These spherule lenses were used by the samous Mr. Leeuwenhock, by which he made such wonderful discoveries in the minuter parts of nature. And it must be by a proper arrangement of these, that the particles of matter are to be discovered, if ever they can, which Sir Isaac Newton thought was possible.

But there are great difficulties attending the use of these very small spherules: first, the difficulty of making very good ones, of a very small diameter. Secondly, the prejudice done to the eyes in using them. Thirdly, the trouble of placing objects at the proper socus. And lastly, the very small part of the object, which can be seen at one time. These inconveniences render this fort of microscopes of very little service for common use; they have therefore been superfeded by others, particularly by the following; in which both transparent and opake objects may be viewed with less trouble.

In this instrument (fig. 11) F is a piece of brass turning round in a socket, at the end of which is a small spring tube moving upon a rivet, through which there runs a steel wire, terminated at one end by a sharp point, G, and the other end hath a pair of plyers, H. The point and plyers are to shrust into, or take up any object. Either of them may be

sumed operards, sowards O. I is a ring of brais with a female forces within it a this ripp is fixed upon a piece of brule which turns round on a river near D, that is may be fet to the proper diffame, when the truth rengaliters are ufed. K. (fig. 12) is a concave speculum, or mirror, generally of filver, polithed very high, to the centre of which a double convex tens is placed, with a prepar sperture, an look through it; on the lark of this fpeculum is a male ferew L, which is made to fixew into the female forew I (fig. 113).

There are generally four of these reacave specula, with different leafes of different magnifying powers, for different otpode. The greatest magnifiers must always have the lead

D is a not adapted to the force B : one end of this force is fallened to the fide C, and by turning the not D, the two files A and C are gradually brought together, or separated, being beld flood, by the first spring In P is the handle of the influencest

La me this a flam ent, the Germann K is to be firewed non the bear income, the magniful gilters being fift backing the freculum. Then place it object either on the needle G. in the places H, on the exception M. Contral, or in the Forts had O regularly and to treat convenient; then holding up the influence to the doctors to I, look through the nogrations less directions were to the high panel by the mit D. mages an with the result for the conserver, the object may be the state of the following of the secretarial forthe from the of the Wards See a factor the true focus, and the eight is thought with a dispensity from the speculums by Calenging to all a will be a very cally and difficulty. The highest reamine will be a say well as doy-light, for the 111 (f - 111 - 11<sup>1</sup> )

On the court is a facility trade box, with neglige on cach fide to continuously living object, in order to by examined; it forms up in the needle G, be and a s of a finall pipe at bottom.

M (fig. 13) is a round object plate, black on one fide, and white on the other. N, a freel spring, tuning down on each fide, to hold any object fast. A dark coloured object is to be placed on the white side; and a light coloured object on the black side, to render them more distinct. This plate also has a small pipe to screw on the needle G (fig. 11).

This microscope is of late invention: and by means of the polified mirror, any opake object may be viewed with a very small magnifier. Transparent objects may also be viewed by it: but in this case, it will not be proper to throw on the object all the light reflected from the speculum; less the light transmitted through the object, meeting the reflected light, peroduce too great a glare. For this purpose, a bit of paper may be interposed between the object and some part of the speculum. A listle practice will enable a person to know how to regulate the light.

As opake objects are more numerous than others, very great discoveries may be made in such objects.

# A Microscope on a Stand, which will answer all the Ends of the large Double Reflecting Microscope.

B (fig. 17) is a round frame of wood, on which is fixed the brass scroll A for the purpose of holding the microscope fleady. C is a brass screw that passes through a hole in the scroll, into the microscope D, and serves to screw it sail to the scroll.

E is a concave looking-glass, or speculum, of metal, set in a brass box, and hanging in the arch G by two small screws: at the bottom of this arch is a small brass pin h, which goes through the stand of the arch into the wooden frame B, by which means the arch is turned round in an horizontal direction; and the mirror swings in a vertical direction. By these two motions the speculum may be so adjusted as to restent the light directly upwards, through the body of the microinge D, which is fixed perpendicularly over it.

The

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The body of the microscope may also be fixed in an horisontal direction, and objects viewed either by the light of a candle, or the common day-light.

To use this microscope, the object is fixed in a slider, which is thrust in between the plates, through a slit on one side of the microscope.

This microscope may be used in a variety of ways. One method I shall mention:—Take a slip of glass, place one end through the slit of the microscope where the sliders go; and on the other end, which extends to some distance, any object may be placed that cannot be placed in the sliders; then place over the object, upon the slip of glass, a magnifying lens, screwed into a brass ring, (having several lenses sixed in brass rings for that purpose, and in such a manner that the ring of brass may extend as tar as the focal distance of the lens,) and bring the speculum to restect the light up to the object.

Microscopes of this fort are the most easy and pleasant for use, of any extant; and will serve to view very minute objects; such as the animalcules and falts in fluids, the farina in vegetables, the circulation of the blood in small infects, &c. If the object have any degree of transparency, this microscope is likely to make more discoveries in it than any other.

## Of Double or Compound Microfcopes.

Double or compound microscopes are those which have two glatles, or lenfes: that next the object is called the object glats; and that next the eye, the eye glats.

The object a bi (fig. 16) is placed at a little greater distance from the object glass than its focus; to that the rive flowing from the different points of the object, and pairing through the object grass, if, will converge to grand is where they form the image of the object. This image is viewed by the eye at Githin igh the eye grass exist which is to places, that the image gives in its focus, and the eye in the focus.

also, but on the other side; thus, the rays of each pencil will converge at the eye k, where they cross each other, and after passing through the humours of the eye, they will form the large inverted image A B on the retina.

This image, feen by fuch a microscope, will be inverted with regard to direct vision: for the object ab lies in the same direction as the image AB on the retina, as seen in the figure; which is not the case when the object is seen by the naked eye, or by a single microscope.

To calculate the magnifying power of these double microscopes, we reckon how many times the object is magnified by the object glass, and then how many times the image of this object is magnified by the eye glass: thus, if the object ab be reagnified six times in length by the object glass cd, as it will when the image gb is six times the distance from the object glass, as the object ab is: and if the eye glass af be only of half an inch focus, the image gb can be viewed at half an inch distance, which as it is only the twelfth part of six inches, the image gb will be magnified twelve times in length to what it will appear to the naked eye without the eye glass: and the image gb being six times the length of the object ab, the object ab is therefore magnified in length seventy-two times, and the superficies and folidity in proportion.

The field of view is very small in a microscope of this fort; therefore, there are generally two eye glasses used, which are placed sometimes close together, and sometimes an inch or more afunder: by which means the visible area is much enlarged, and a larger field of view is obtained, though the object appears somewhat less magnified.

## A Compound Microscope.

A (fig. 18) is the body of the microscope, which is moveable up or down in the external case CD, which is fixed on the foot of the instrument I, by three pillars. F is a plate fixed horizontally to the three pillars, and is called the stage. In the centre of which is a hole, on which a piece of glass,

3 I 2

OL



an angle, from the perpendicular to the furface of the mirror, as they fall upon it, with regard to the perpendicular, but on the other fide thereof. Thus, let C be the centre of the mirror's concavity. Draw the lines  $C_gA_p$ ,  $C_mI_p$ , and  $C_bc_p$ , from the centre C to the mirror. These lines will be each perpendicular to the mirror, as they proceed therefrom like so many radii. Make the angle  $C_bc_p$  A equal to the angle  $C_bc_p$  And draw the line  $C_bc_p$  which will be the direction of the ray  $C_bc_p$  after reflection; so that the angle of incidence  $C_bc_p$  A.

In the same manner the angle of restection mec may be proved equal to the angle of incidence Cee. The ray Cm / passing through the centre of the mirror's concavity, and talling upon it at  $I_r$  is therefore restected back from it in the same line. All these restected rays meet in the point m, and there paint the image of the body, from which the parallel rays proceed.

This point, as before observed, is half the distance of IC.

The rays which proceed from any celeftial object may always be effected parallel: and therefore the images of fuch objects, on a reflected speculum, will be formed at half the distance of the centre of the mirror's concavity.

But the rays which proceed from any diffant terreftrial object do not come quite parallel to the mirror; but come diverging to it in feparate pencils; therefore they will not be converged to a point at the diffance of half the radius of the concavity of the mirror, but at a little greater diffance from the nurror, and in feparate points. And the nearer the object is to the mirror, the farther these points will be removed from it; and an inverted image of the object will there be formed, which will feem to hang pendulous in the air, by an eye placed beyond it.

Let AB be a mirror, whose centre of concavity is C (fig. 3), DE is an upright object placed beyond the centre C; from the upper end D, of which flows a pencil of diverging rays to every point of the concave furface of the mirror AB.

From the centre C, draw CA, Cc, CB, touching the mirror in the same points where the pencils of rays touch it, which slow from D. These three lines drawn from C to the mirror will be perpendicular to the surface of the mirror. Make the angle CA d equal to the angle DAC; and draw the right line Ad for the restection of the ray DA. Make the angle CB d equal to the angle DBC, and draw the right line cd for the course of the incident ray Dc. Make the angle CBd equal to the angle DBC, and draw the right line Bd, for the course of the incident ray DB; all these restected rays will meet in the point d, where they will form the extremity D of the image DE.

If the pencils of rays be drawn from the other point of the object  $E_i$  in the direction  $E_i$ ,  $E_i$ ,  $E_i$ , and be continued to the furface of the mirror, they will be reflected back from the mirror to the other end of the object  $d_i$  and their angles of reflection will be equal to their incident angles: thus, they form an inverted image of the object, at the point  $A_i$ 

Though I have only drawn three lines in the figure, to reprefent rays flowing from the point D; yet it must be observed, that this point, as well as every other point in the object, sends forth a pencil of rays to every part of the mirror; and the rays of each pencil are reflected back, and meet in all the intermediate points of the object d, as had been shown, with regard to the point D.

When the object is farther from the mirror than its contract, the image will be less than the object, and will be between the object and the mirror; but when the object is nearer than the centre of concavity, the image will be further off, and bigger than the object.

If the radius of the mirror's concavity, and the distance of the object from the mirror be known, the distance of the image from the mirror may be found by this rule:—

Divide the product of the diffunce, multiplied by the radius, by double the diffunce made less by the radius; and the quotient is the diffunce required.

If a man place himself directly before a concave mirror, but at a further distance from it than the centre, he will see an inverted image of himself in the air, between him and the mirror, and less than himself in size. And when he holds his hand out towards the mirror, the hand of the image will also approach towards his hand; and if his hand be in the centre of the mirror, the hand of the image will coincide with his hand; and an inexperienced observer will fancy that he may thake hands with his own image. If he extend his hand forward further towards the mirror, the hand of the image will pais by his hand, and come between his hand and his body: if he move his hand to either fide. the hand of the image will move the contrary way. But a person standing at a distance, and on one side of the mirror. will fee nothing of the image, because none of the restected rays enter his eye.

It is necessary that the reader perfectly understand what is here demonstrated concerning reflection, that he may perceive how the image is formed in the large concave mirror of the reflecting telescope.

Again, if a concave mirror be placed against a wall opposite a fire in a chamber, and a mahogany table highly polished, placed in the focus of the mirror; a person standing facing the mirror, but not directly between that and the sure, will see a large, bright, creek image of the fire upon the table; and to a casual observer, just entering the room, it will appear in all respects like a real sire. But the room should be made quite dark for this purpose, that the sire may app ar more bright. But to a person who stands on one

fide the table, nothing will appear but a long beam of light.

If, instead of a fire, a large candle be placed opposite the mirror, a person standing by the candle will see the appear-] ance of a large bright star over the table: thus, by fixing a large candle in a frame, with a small wax taper to turn round it, in a circle, an appearance will be made in the focus of the glass, representing a bright planet, and its satellite; the satellite performing a revolution round the planet.

#### The Refracting Telescope.

The first form of refracting telescopes, that I shall mention, is that which consists of two lenses only. The object glass must be convex; but the eye glass may be either convex or concave.

Let cd (fig. 4) be a convex object glass, in a long tube. and have its focus at E. AB is a remote object: from the extremity A flows a pencil of rays ghi, which will be so refracted by passing through the glass cal, as to meet in the point f; and the pencil of rays k/m, flowing from the other point of the object B, by passing through the lens will be refracted so as to unite in the point e; thus the points A and B of the object will be formed by refraction in the points fee and all the intermediate points of the object fend forth pencils of rays, which form corresponding points in the small figure fe, the inverted image of the object. But as this image is small, a concave glass nc is placed at the end next i the eye, so that its virtual focus may be at F. Then as the rays of the pencils come to the concave glass converging, they will converge less after passing through it, as hath been demonstrated: and they will proceed to b and a before they unite, which is on the retina, and there form the large image ab.

The only inconvenience attending the use of this telescope is, that the field of view is very small, by reason of the rays, 3 K diverging

diverging to much, after passing through the concave

For, from a view of the figure, it is evident that when the telescope lies directly towards the object, none of the rays which flow from the extremities A and B can enter the pupil of the eye; but fall upon the iris, above and below the pupil. So that, to view the different parts of an object, the telescope must be moved upwards or downwards, unless the object be a very remote one; and then it is but indistinctly feen.

Therefore, to remedy this inconvenience, a convex eye glass is used instead of a concave, as ab (sig. 5), which is placed so, that its focus may be coincident with the focus of the object glass cd, whose focus is at E. Then the rays of the pencils flowing from the object AB, and passing through the object glass cd, will meet in its focus, and form the small inverted image mp. And as the image is formed in the focus of the eye glass ab, the rays of each pencil, after passing through this glass, will be parallel, but the pencils themselves will converge to each other, and cross each other in the focus of the glass at e: the pupil of the eye being in this focus, the image will be viewed through the eye glass, under the angle D e C.

This telescope also has an inconvenience, which is, that is inverts the object with respect to it, when seen by the naked eye: that is, the image is painted in the eye in the same position in which the object lies; we therefore judge it to be inverted. This telescope is, therefore, only sit for viewing celestial bodies, in many of which their position is immaterial. But it must be observed, in the use of this telescope, that whatever way the object seems to move, the telescope must be moved the contrary way; for as the object is inverted, so will be the motion.

The magnifying power in this telescope, is as the focal distance of the object glass is to the focal distance of the everglass. Therefore, if the former be divided by the latter, the quotient will express the magnifying power.

Therefore,

Therefore, this telescope can be constructed so, as to magnify in any proportion, provided it be of a sufficient length: for the greater the focal distance of the object glass is, the less may the focal distance of the eye glass be. Thus, an object glass of ten feet focal distance will admit of an eye glass, whose focal distance is little above two inches and a half, which will magnify the length of an object near forty-eight times, and its surface and solidity will be magnified in proportion; as in the microscope.

Thus, if the focal distance of the object glass be equal to the focal distance of the eye glass, the telescope would not magnify the object in the least.

Again, if the focal distance of the object glass be twenty inches, and the focal distance of the eye glass one inch, the length of an object seen by such a telescope will be magnified twenty times, its surface four hundred times, and its solidity eight thousand times.

To remedy the inconveniences of both the former kinds of telescopes, the following one is generally used for terrestrial objects, which gives a larger field of view than that with the concave eye glass, and shows the object in its natural posture, as seen by the naked eye. In this telescope there is one object glais ed (fig. 6), and three eye glasses, ef. They are so placed, that the distance between every two glasses, which are next each other, may be equal to the fum of their focal distances; thus, the focus of one glass is coincident with the focus of the next glass. faci of the two glasses ed and ef, meet at F; those of the two glasses of, gb, meet at I; and those of gb and ik, at m; and that of ik at n, where the pupil of the eye is Then it is evident, from the figure, that the pencils of rays which flow from the object A B will pass through the object glass cd, where they cross each other, and meet, and form an inverted image, in the focus of the glass at CFD; . this image being also in the focus of the next glass of, the rays of the pencils, which flow from the image CFD, will

become parallel after passing through this glass, and cross each other at l, which is the focus of the next glass  $g \neq g$  therefore, the rays proceeding from this focus and passing through the next glass  $g \neq g$ , are converged to the focus of this glass, where they form the erect image EF of the object AB; and as this image is in the focus of the eye glass  $i \neq g$ , and the eye on the opposite side of the glass in the other focus, the image is viewed through the eye glass in this telescope, in the same manner as in the former one, but in a contrary position; that is, in the same position as when seen by the unked eye. The object also appears under the angle  $i \neq g$ .

The three eye glaffes have generally all their focal distances equal. The magnifying power of this telescope is found in the same manner as that of the last: viz. by dividing the focal distance of the object glass by the focal distance of any one of the eye glaffes, as the three latter are all equal.

Objects feen through such a telescope appear coloured about the edges, the reason of which is, that the rays of light coming from the object are unequally refracted through the glass lens, and particularly those rays which pass through a convex glass near its edges. These rays, being unequally refracted, do not all meet again in the fame points exactly. Therefore, in this teletcope, there must be a plate with a finall round hole in the middle, fixed at m, parallel to By this plate, the wandering rays about the the glaffes. edges of the glaffes will be intercepted, and prevented from coming to the eye; and none admitted, but those which come through the middle of the glaffes, or, at leaft, at a good distance from the edges. But this formewhat lessens the field of view, which would be much larger if the plate could be difpenfed with.

The Binocular, or Double Telefcope.

The binocular, or double telefcope, is only two telefcopes of an equal magnifying power, fixed in a frame, parallel to each

each other, and adjusted by the means of screws, so as to be at the same distance from each other as the pupils of the two eyes. Then by looking through them both at once, through one with each eye, the object will be seen by both eyes, and appear brighter, and more distinct than through a single telescope.

#### The Reflecting Telescope.

Refracting telescopes require to be of a considerable length, to magnify to any great degree, and the great length of some of them has rendered them very inconvenient. Sir Isaac Newton, therefore, invented the first telescope of the reflecting kind, and which has received considerable improvements since his time. Since the invention of these, refracting telescopes are very little used for celestial objects 5 for a reflecting telescope, of only six seet in length, can be brought to magnify the object as much as one of the other fort of a hundred seet in length.

They are generally confirmated now in the following manmer: TTTT (fg. 7) is a large tube, at the houson of
which is placed a large concave mirror, DUVF, whole
principal focus is at m. In the middle of this speculium is a
mount hole P, opposite which is placed the fund mirror L,
concave nowands the great solvers, and fixed on the use M,
by which it may be knought neares to the great mirror, or
mount further off, having a long forew on the outlide of the
millies with that of the great mirror; six. Power In thing the
millims with that of the great mirror; six. Power In thing the
millims with that of the great mirror; six. Power In thing the
millims with that of the great mirror; six. Power In thing the
millims with that of the great mirror; six powers and paralle is
established that is defined, which is the transport in the surface of the
mirror.

Land I be the diffiant stopeth, from visite two conservations. Show the parallel of rays I and I, which we wrise impose generally the rays I. Isling these the great region of I, are from themse otherwise in the conservation. I. I.

and by crofling at I, the point of convergence, and the principal focus of the mirror, they form the upper extremicy I, of the image IK, fimilar to the lower extremity B. of the object All; and then they pass on to the finall concave mirror, whose focus is at s. They full upon this finall concave mirror at a, and are from thence reflected, converging in the direction gN; because gm is longer than gm; and palling through the hole P, in the large mirror, they would pale on to r before they meet, and there form the lower extremity d of the creft image ed, fimilar to the lower extremity B. of the object AB. But passing through the plane convex glass R, they form that extremity of the image In the fame manner the rays E, which come from the extremity of the object A. and fall parallel upon the great mirror at F. are from thence reflected to its focus, where they form the lower extremity K. on the image I K. fimilar to the upper extremity A, of the object AB; and from thence they pals on to the finall mirror L, and fall upon it at h; from whence they are reflected, converging in the direction &O, and palling through the hole P of the great mirror, they would meet at q, and form the upper extren ity e, of the image ed, fimilar to the extremity A, of the object AB, but pulling through the convex glass R, they meet, and crofs fooner, as at a, where that point of the image is formed. In the fame manner pencils of rays flow from every intermediate part of the object A.B. to the great morror DUVF, and are from thence reflected to the focus of the nervor 44, where they form an inverted image of the object. And failly, the rays patting from the image at. through the eye glass, and through a fmall hole e, in the end of the leffer tube to, they enter the eye f, where they cross cach other in the pupil, and paint the image of the object on the ection in its natural position, and the image is feen by the eye under the large angle code

To find the magnitying power of this telefcope, the rule is, to multiply the focal diffance of the great mirror, by the diffance

distance of the small mirror from the image which is next the eye; and multiply the focal distance of the small mirror, by the focal distance of the eye glass; then divide the product of the former multiplication, by the product of the latter, and the quotient will be the magnifying power.

When the first image IK is formed a little further from the great mirror than its principal focus, as at a; the focus of the great mirror is never coincident with that of the small one; therefore the rays of the pencils resected from the small mirror will not be parallel, but rather converging, so as to meet in the points qer, where they would form a larger erect image than ab, if the glass R was not in the way. This image might then be viewed by means of a single eye glass, properly placed; but in that case, the field of view would be less; therefore, the glass R is used to enlarge the view.

The adjusting screw, to which the small mirror L is fixed, renders this telescope applicable to every sight, as the small mirror may be brought either nearer to the eye, or removed farther from it; by which means the rays may be made to diverge a little, for short-sighted eyes; or to converge, for persons of a long sight.

In the use of this telescope, it must be observed, that the nearer an object is, the more the pencils of rays will diverge before they fall upon the great mirror; and consequently they will be the longer before they meet after restriction; therefore, the first image IK will be formed at a greater distance from the large mirror. But this image must always be formed further from the small mirror than its principal focus s; therefore, the small mirror must be fet at a greater distance from the large one in viewing a near object than when viewing an object more remote; this is easily performed by turning the adjusting screw.

The reflecting telescope will admit of an eye glass, of a much shorter focal distance (and consequently of a greater magnifying magnifying power) than a refracting telescope will; therefore, those telescopes magnify to a greater power. And the rays of light are not coloured by the reflections of the concave mirror, if it be ground to a true figure, as they are by passing through a convex glass, though it be ground ever so true.

In these reflecting telescopes, the observer never sees the object itself, but only the image of it, which is formed next the eye. This will be demonstrated by the following experiment:

If the observer fix a stick across the mouth of the telescope before the object glass, it will not hide any part of the object from his view, unless it covers the whole mouth of the telescope; but it will only make the object appear dimmer, by intercepting part of the rays. But if he place only a piece of wire across the inside of the tube, between the eye glass and his eye, it will hide part of the object, which he thinks he ices; which proves, that it is not the real object, but the image which is perceived. This is evident, from the small mirror L, which is made of opake metal, and stands directly between the eye and the object, and would hide the whole object from the eye, if the two glasses R and S were taken out of the tube.

#### The Solar Telefcope,

The folia teleflope is the most useful instrument for viewing the face of the tun of any hitherto invented. It is formed of a felliptile ball and focket, which is fastened against a hole in the window-shutter of a darkened room; in the evhindrical hole of which is placed the end of a common refracting telescope, which is to be drawn out to its proper (legth; then the ball and telescope are moved about till the

rays of the fun fall perpendicularly on the object glass, through the hole of the ball i the tube which contains the eye glass is then to be adjusted, by drawing it in, or out, till the image of the fun be formed on a white paper, in the focus of the telescope, very distinctly and large.

By this telescope, the face of the fun may be represented in almost any size, which affords the mathematician an opportunity of viewing all the phenomena to be feen in that planet: fuch us the foots on the fun's dife, which are feldom feen when viewed through finall telescopes, in the common way. But they may here be feen in all their different appearances; as their increase, division, union, beginning and end, &c. also the solar college may be seen to a great advantage. And the transits of Mercury, and Venus over the face of the fun are most delightfully exhibited by this instrument; as the planets here appear truly round, and very black; their comparative diameters to that of the fun may be taken, with the true direction of their motions, their ingress, egress, &c. The circle of the fun's dife may be divided by lines and circles, that the quantity and time of the eclipse may be exactly determined.

The belieflate was the invention of Dr. Gravefand: by this excellent invention, the motion of the telefcope, in viewing the folar light, is greatly taken off. It confifts of two parts first, a plain metallic speculum, supported on a stand; and a clock, which directs the speculum according to the motion of the earth, and thereby preserves the image of the sun in the same point of view.

#### The Acromatic Telefcope.

This telefcope has a double, and fometimes treble object glafs, to correct the aberration of the rays of light; for all rays of light palling through a fingle lens will be fomewhat decompounded, and divided into feparate colours, which renders the object coloured; to remedy which, the double

object glass is used. This confetts of a double concave lens of white flint glass, and a double convex of crown glass. The two parts of the lenge, which are on the fame fide of the centre, have the same effect on the rays of light as two triangular prisms, which refract the rays of light in a contrary duction to each other; therefore, if the excess of refraction in the crown glass destroy the divergency of colours oceastoned by the flint glass, the incident ray will be refracted without any foreign colour; thus, the image formed in the focus of this compound object glass, will be of the same colour as the object. For the rays flowing upon these slaffes from distant radiant objects will pass through them in such a manner, that the aberration, caused by the first glass, is so far corrected by the second, that the rays emerging from it are nearly parallel, and converged to one focus. from may, therefore, have a much larger sperture, and a greater magnifying power, than the common refracting telefempe can. And if the telescope be fluort, the leaste should be very convex : and it flould then have three lenfes for the object glass; a concave one of white fint, between two convex ones of crown glass.

#### The Camera Obscura.

The camera obscura is only a convex glass CD (fig. 9) sixed in a hole of a window-shutter. In the focus of this glass will be seen, on a sheet of white paper placed parallel to the glass, as at GH, the images of all the objects outside of the window, as trees, men, cattle, &c. which affords a most beautiful piece of landscape, or perspective, particularly it the sun shines upon the objects: but the images appear inverted. The room for this purpose should be so darkened, that no light can enter, but what comes through the lens.

To represent the image horizontally, the convex glass CD must be placed in a tube in the fide of a square box, within which is the plane mirror EF, leaning backwards

in an angle of forty-five degrees from the perpendicular Ig; then the pencils of rays flowing from the outward objects, and passing through the convex glass to the plane mirror, will be reflected from it upwards, and meet in points, and form the image I K, of the object A B, which is at the fame distance from the mirror EF, as the image GH, which image they would have formed if no mirror had been in the way. This image I K will be formed on an oiled paper, stretched horizontally in the direction I K. On this paper the outlines of the images may be drawn with a black lead pencil, and then copied on a clean sheet; but it is usual to place a plain unpolished glass in the direction I K to receive the images of the outer objects; and their outlines may be traced upon this, as on the paper.

The tube in which the glass CD is fixed must be moveable, that it may be drawn out to adjust the distance of the glass-lene, from the plane mirror, in proportion to the distance of the focus. For this purpose, the tube must be moved backward or forward, till the images appear distinctly on the horizontal glass IK.

If the mirror EF be reclined in the opposite direction; that is, leaning forwards towards the lens, in an angle of forty-five degrees, the images of the objects will then appear in an horizontal position, but below the lox; and inverted with respect to the image IK.

To form an horizontal image, as IK of an upright object AB, it is necessary that the mirror be reclined from a perpendicular, in an angle of forty-five degrees. Then the rays of the pencils abc flowing from the point A of the object AB, will fall upon the mirror at the points kfg, and from thence will be reflected in the lines kI, fI, gI, and form the point A of the object AB, at the point I in the image IK. And the rays of the pencils qrs, flowing from the point B, and passing through the convex lens CD, will fall upon the mirror at the point m/k, from whence they will be reflected to the point K, where they form the image

of the point of the object B. The fame may be demonstrated of the pencils of rays, which flow from every intermediate point of the object AB. This horizontal reflection depends upon the rays of incidence, (which fall upon the mirror, after passing through the convex lens CD.) making angles, with a perpendicular drawn to the furface of the mirror, equal to the angles formed by the reflected rays, and the faid perpendicular; thus, if we suppose a perpendicular drawn to the furface of the mirror at the point k, where the ray A & C r falls upon it, that ray will be reflected upwards in the line k d I, which will make an angle with the aforefaid perpendicular, and on the other fide thereof, equal to the angle formed by the perpendicular, and the incident ray C k: and if a perpendicular be drawn to the point fof the plane mirror, where the ray A &f falls upon it, that ray will be seffected upwards in the direction fb 1, which will also make an angle with the last perpendicular, equal to the angle formed by the incident ray Abf, and the same perpendicular. Tho iums may be demonstrated of every other pencil of rays which flow from the object AB.

The flat plano-convex glafs, vulgarly called the multiplying glafs, is used to multiply an object. It is formed of a plano-convex glafs, the convex fide of which is ground into feveral flat furfaces. An object feen through fuch a glafs will appear multiplied into as many different objects as the glass contains plane furfaces. Let AD (fig. 8) be fuch a glass, the flat furfaces of which are bb, bld, dk; then the inys which flow from the object C to all parts of the glafs will be refracted by the plane furfaces to the eye at II. ray gH falling perpendicularly on the middle furface, will pals through the glals without any refraction, and flow the object C in its true place; but the ray a l., flowing from the tame object, and falling obliquely on the plane furface blo will be refracted in the direction (II: by which the object will appear as at E. And the ray eth, flowing from the object  $C_{ij}$ , and falling obliquely on the flat furface  $dk_{ij}$  will be refracted

fracted in the direction fH; by which the object will appear in the line fm, as if it were at D. If the glass be turned round the axis III<sub>K</sub>, the object C will remain in the same place, but the other objects D and E will appear to go round C; because the planes on which the oblique rays fall, will be turned round by the motion of the glass.

From what has been faid of the properties of different lenfes, the intelligent reader may be able to form a combination of them, for any ordinary optical purpose; but it may be necessary to say a few words more, concerning the reflecting telescope.

The great mirror of the reflecting telescope, as invented by Sir Isaac New Ton, was truly spherical; and which telescopes are of effential fervice at this day, particularly in the minutiae of aftronomy, when finall apertures and long foci are used. Dr. Herschell uses a reflector of this form, in his feven feet reflecting telescope. And the highest power that a telescope of a spherical metal will bear with perfect distinctness, may be found, by multiplying the diameter of the great mirror by feventy-four. Thus, in Dr. Herschell's seven feet reflector, the aperture or diameter of the great mirror is 6.25 inches, which, multiplied by 74, gives 46s the magnifying power; and the focal distance of the single eye glass may be found, by dividing the focal distance of the great mirror by the magnifying power; thus, 7 feet, the focal diffance, multiplied by 18, and divided by 46s, quotes 0,18s of an inch. the focal distance of the eye glass.

But the concave furface of the great mirror, in common reflecting telefcopes, is of a parabolic form; which form Sir Masc Newton was unable to give to his metal, though he recommended it; and imagined it might be effected by mechanical devices.

#### A TABLE

#### OF THE

# Final Diffunity, Apertures, and magnifying Powers or the NEWTONIAN REFLECTORS.

friend Definance of the concases Mend.	Agenties of the concess Metal.	SelfancNew vm/s Numbers	Focus Difference of the fingle Byr Galds.	The magnifying Power.	
Non.	In the. 0. 80	100	In Dec. 0. 167	36	
1	1.44	168	0, 100	6a	
	2.45	alle	0.236	108	
3	3.31	,183	0. 161	1,18	
4	4. 10	470	188.0	171	
	4. 85	gha	0. 207	808	
6	4. 57	641	P. 111	848	
7	6. 44	5.6	11. 121	400	
	n. Ny	Reser	Ox. 1.14	4117	
0	7.51	W.	0.114	114	
10	P. 10	010	0.451	440	
11	R. 40	20 14	17: 10.4	406	
14	0. 10	11.154	w. 107	100	
11	0.04		1.127	414	
14	10. 10		11. 184	400	
12	with	Sir.	4. 101	484	
16	11.10	1144	05 107	500	
3.5	12.11	10 1	0.404	448	
18	14.67	1 2 4	0.400	110	
10	10.00	1501	65, 4413	153	
ørs.	14:71	1401	01.446	107	
01	14-01	1	0.440	614	
44	14 1		25414	615	
11	19:1	Loke	12. 110	nin	

#### A TABLE

#### OF THE

Dimensions and magnifying Powers of the Gregorian Restering Telescopes,

As confiructed by

#### Ma. SHORT.

Magnifying Power.	Diffunce between the two Glaffes.	Focal Diffusion of the Glafs next the Eye.	Focal Diffunce of the Claris next tite Metals.	Diffusive between the little Speculum, and the first Eye Glads.	Breadth of the Hole in the great Speculium.	Focus of the lathe Speculam.	Breach of the great Mirror.	Focal Diffance of the great Mirror.
39	In. Dec. 1. 68 2. 08	1.04	3.13	8. 54	. 39	1.10	1. 54 2. 30	9.60
165	3.41 4.28	1.71	5. 12	41. 16 68. 17		3.43		15.50 30.00 60.00

Since the invention of these reflecting telescopes, the refracting ones are very little used for celestial observations. For a refracting telescope, even of a thousand seet focus, (supposing it possible to be used,) could not be made to magnify more than one thousand times; whereas a reflecting telescope, not exceeding ten seet, will magnify twelve hundred times. Mr. Short, of Edinburgh, was the first who brought the Gregorian reflectors to perfection, by giving them the true parabolic form, whereby they will admit of a much larger aperture.

To the same ingenious gentleman we are also indebted for that excellent contrivance, the equatorial telescope, or, as he himself calls it, a portable objervatory; by which most of the flars of the first and second magnitude, as also the planets Mercury. Venus, and Jupiter, may be feen at mid-day. even while the fun flines bright. By this inffrument, colesial objects may be viewed with very little trouble. It confifts of a piece of machinery, by the help of which the mounted telescope may be turned in any direction, and directed to any degree of right afcention, or declination. And any object may be callly kept in view, or recovered when loft from fight. without moving the eye from its fituation. The particular effect of this telescope depends upon its excluding almost all the light, except what comes from the object itself. But any other telescope of the same magnifying power, and in the fame fituation, will have the fame effect. From a fimilar cause, the stars are visible in day-time, from the bottom of a deep pit.

Mr. Ramiden has also lately invented a portable observatory, which, it is expected, will excel Mr. Short's.

To render the fixed stars visible in day-time, it is only necessary to exclude the extraneous light as much as possible.

A comet, or any other beavenly body, may be seen through this telescope; its machinery directing it to the proper place in the heavens.

The principal advantages of microscopes and telescopes depend—first, upon their property of magnifying the minute parts of the object, so that they can be seen more distinctly than by the naked eye; and, secondly, upon their throwing more light into the pupil of the eye than what would flow from the object itself. The magnifying power

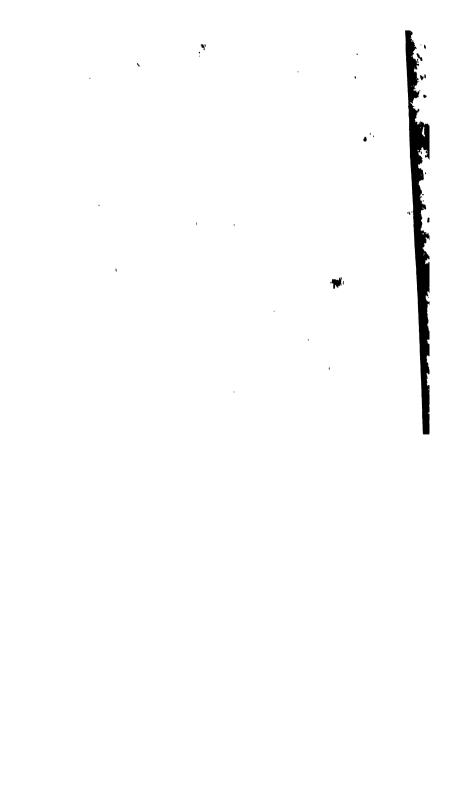
of the glass would be of little service. if this latter property of transmitting the light be wanting; for the same quantity of light, spread over a larger surface, becomes proportionably diminished in force; and though the objects may appear bigger, they would appear proportionably dimmer, without an increase of light, as well as magnitude. Thus, though a glass flould magnify the furface of an object an hundred times. vet if the focal distance of the glass were only eight inches (if this be possible), and its dismeter only the fize of the pupil of the eye, the object will appear an hundred times more dim through the glass, than to the naked eye; even though the glass transmitted all the light which fell upon it, which no glass can do. But if the focal distance of the glass be four inches, and the diameter the fame as before: the object will appear far more bright, because the glass could be placed twice as near the object, as before, and confequently would receive four times as many rays of light from the object. as in the former case. Thus, diminishing the focal distance of the glass, and keeping its diameter as large as possible, we should perceive the object more and more magnified, and at the same time very distinct and bright.

With regard to the comparative merit of telefoopes, for terrestrial objects, those of the refracting kind have evidently the advantage of all others, where the aperture is equal, and the aberrations of the rays are corrected according to Mr. Dollond's method: because the image is more perfect; and a greater quantity of light is transmitted, than can be reslected from the best materials hitherto known. And a telescope for terrestrial objects should never magnify above an hundred times; if it do, the vapours arising from the earth will be so magnified, as to render vision very obscure and imperfect.

However, the imperfections in every kind of glass, very much retard the improvement of these telescopes, in which there are five eye glasses; so that they cannot be made above three feet and an half long.

Upon the whole, therefore, the reflecting telescopes are the 2 M best



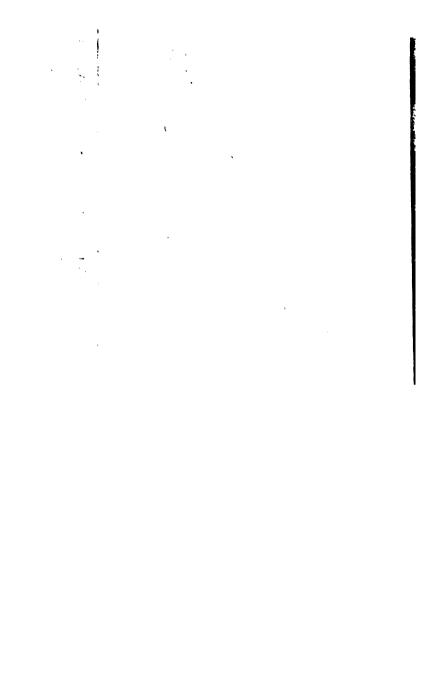


telescope must be kept constantly directed to the same point of the object: for if the telescope be moved gently from its position, the object will seem to move in the same, or in the opposite direction, according as the telescope shows the image inverted, or erect.

If the inftrument shake ever so little, it makes the object dance before our eyes; and causes an indistinctness in the vision. In the Gregorian telescopes it is hardly possible to prevent this quivering motion of the small speculum, as it is fixed to the tube by one arm only. And though the tube of the instrument be fixed ever so motionless this speculum will retain a tremulous motion, particularly if the telescope has . A great magnifying power. This motion is an imperceptible tremor, like that of an harpsichord wire, while it is founding, and produces a fimilar effect to the fight. A person walking in the room, where the inftrument is fixed, prevents us from seeing the object distinctly; or even the pulsation in the body of the observer agitates the ground enough to produce this effect. The more rapid this motion is, the greater is the optical indistinctness; or the object appears more confused. Therefore, the more firm, classic, and well bound together, the frame work and apertures of the telescope are, the more hurtful will be the confequences. Just as it is to a rider on a wheel carriage—the more firmly the carriage is fixed on the wheels, the more violent will be the motion to the rider. A telescope, therefore, mounted with lead (if it were practicable), would be preferable to one mounted on either wood, This is the principal cause of that indistinctiron, or brafa. nels of vision in the very best restocting telescopes. Refracting telescopes have not this inconvenience.

From hence we may easily judge of the merits of any particular apparatus, for the support of a telescope: and in general, all forms where the tube is supported only in or near the middle, or where it remotely depends upon one joint, are very destructive of distinctues of vision.

The



#### To use the Solar Microscope, (Fig 4.)

Make a round hole in the window-shutter, a little larger than the circular plate abc: pass the mirror ONP through this hole, and apply the square plate to the shutter, screwing it thereto by the two milled forews de: the forews are to pass through the shutter into their nuts in the microscope, and thereby to hold the body of the microscope sirm. Screw the conical tube ABCD to the circular plate abc; and then flide the tube G of the opake box into the cylindrical plate CDEF, if opake objects are to be viewed; but if transparent objects are to be viewed, place the tube Y. (fig. 5.) in the cylindrical tube. (fig. 4.) should be made as dark as possible, and no light suffered to enter, but what comes through the body of the microscope: for, on this circumstance, together with the brightness of the fun-shine, the distinctness of the object, in a great measure, depends. The mirror NOP is to be then so adjusted by means of the two screws Q and R, as to reflect all the sun's light through the lens, at A B, in the body of the microscope; the mirror is to be so adjusted, till you have formed a clear round spot of light upon a screen, or sheet of white paper, placed at some distance.

In viewing an opake object, place the object between the plates at H: open the door ik of the opake box, and adjust the small mirror M, till the object is strongly illuminated. If this cannot be effected by the screw S, you must move the two screws Q and R, in order to get light reflected strongly from the great mirror NOP, to the small one M. object being strongly illuminated, shut the door ik, and a diffinct image of the object will foon be obtained on the screen, by adjusting the tubes V and X. In the northern latitudes a clear large spot of light cannot always be obtained, nor when the fun is perpendicular to the front of the room; as the light then falls upon the back of the mirror.

And Note. As the fun is continually changing its place, it will be necessary to change the position of the mirror, by the the two ferows Quad B, to order to type the their repr contionally direct shrough the suit of the hillramous.

#### To view transparent Objects.

Fix the fingle microscope (fig. 5.) in the cylindrical tube R.F. (fig. 4.) put the flider (fig. 6.) into its place at a (fig. 5.) and the flider with the object between the two plates at m, and adjust the large mirror NOP. (fig. 4.) as before directed in opake objects, and regulate the focus of the magnifier of the fingle microscope. (fig. 5.) by the screw O. The most pleasant magnifiers for common use, are those marked number 4 and 5 in the flider, (fig. 6.) The fize of the object may be increased or diminished, by altering the diffusee of the screen from the microscope. That distance which shows the object most diffuse, is about five or fix seet.

To examine transparent Objects of a larger Size by the Megalastope.

Take out the flider, (fig. 5,) from its place, in fig. 5, and forew the button, (fig. 7,) into the hole at P, (fig. 51) then remove the glafs which is under the plate at w, and regulate the focus as before.

At the end of the tube G, (fig. 4.) there is a lem for increasing the density of the rays; which ferves to burn any combustible substance, or melt any susple one. In using this microscope, this lens must generally be taken out, less the object thould be burnt by the intensity of the best.

This microscope affords the greatest entertainment of any, on account of its wonderful magnifying power, and the ease with which feveral persons may view each single object, at the same time. It was formerly used only for transparent octions; but in the year 1774, Mr. B. Martin improved this instrument so far, as to render it applicable to opake objects. He speaks of it thus: "With this instrument all opake objects, whether of the animal, vegetable, or mineral kingdom.

thiguom, may be exhibited in great perfection, in all their mative beauty; the lights and shades, the prominences and bevition, and all the varieties of different hues, tints, and colours, heightened by the reflection of the folar rays condenied unon them."

#### \*\* The improved lucernal Microfcope.

The lucernal microscope is represented, (fig. 1,) where BCDE, is a large mahogany pyramidical box, which is the body of the microscope; and supported on the brass pullar P.G. by the focket H, and the curved piece. M.N and two tubes, one within the other: to the inner tube A fixed the vertical piece M L, which is a guide to the eye, to direct it to the axis of the instrument. This piece may be raifed, or depressed, pulled further out, or pushed further in, to adjust it to the focus of the glasses, and make it coincide with the centre of the field of view. The tubes M N are fixed to the box in a dovetailed piece of brass. OP is a mall tube which carries the magnifiers; O is one of the magnifiers ferewed into the end of the tube. QRSTVX is a long fquare bar, passing through the sockets Y, Z, and Turvey to hold the stage for the objects: this bar may be moved backward or forward, by means of the pinion a, and the handles to, in order to adjust the stage to the focus. is a brais bar to support the curved piece IK, and keep the body of the microscope firm and steady. fgrsis the stage for hold the fliders with the opake objects; it flides upon the bat QRS by means of the focket bi, by which means it is brought nearer to, or removed farther from, the magnifying The objects are placed in the front fide of the stage, next the tube of the microscope, between four small brass plates, (which cannot be shewn in the figure,) the edges of wo of the plates are feen at kl; the two upper plates are moveable, and are preffed together by a spiral spring. to confine the flider with the objects: these two plates may be

raifed 3 N .

raifed higher, or moved lower, by the small nut . The upper part of the stage fgrs, may be taken out, and the stage for transparent objects (sig. 3.) inferted in its place. At the lower part of the stage, there is a semicircular glass lamp at w. to receive the light from the lighted lamp, and throw it upon the concave mirror I, from whence leas reflected on the object.

Fig. 2, is the flage for transparent objects: the two legs 5 and 6, fit into the top of the under part of the flage 7 a, (fig. 3,) is the part that holds the fliders? Q' and 10, the tube that holds the magnifiers: within this tube, there is another, which may be placed at any distance from the object by the pin 11. When this stage is used by itself, as a single microscope, the magnifiers must be screwed into the hole 12, and to be adjusted to the focus, by the nut 13. At the end of the wooden box ABC, (fig. 1,) is a slider A, represented as partly drawn out; when this slider is taken out, there will be perceived three grooves, one of which contains the board that forms the end of the box; the next contains a frame, with a gray glass; the third, or the instruction, contains two large convex lenses.

#### To examine opake Objects, by this Microfcope, .

The inftrument, (fig. 1.) is ready mounted, for this purpole. Take out the wooden flider A, and lift out the court, and the gray glafs from their groover, under the flider B, and the grade for the eye L.M.N being put into its place, and the focket at the bottom of the opake flage on the har Q.X.T., fo that the concave mirror I, may be next the end D.F. of the wooden body. Screw the tube P.O into the end D.F., with the magnificers, and the handle I, or nelled nut, (fig. 2.) placed on the end of the pinion a; place the lighted lamp before the glaft lamp at n, and the object to be examined between the tpring places of the flage; and the nuthrament is really for infe.

#### To examine transparent Objects.

For this purpose, the upper part of the opake stage fgrs, (sig. 1,) must be removed; and the stage for transparent objects, (sig. 3,) inserted in its place, with the end 9 and 10 next the lamp. Place the gray glass in its groove at the end AB, (sig. 1,) and the objects to be viewed in the slider-holder at the front of the stage; then transinit as strong a light as possible on the object, by raising or lowering the lamp; and the object will be beautifully depictured on the gray glass, being regulated to the socus of the magnifier by turning the pinion a.

If the gray glass be taken out of the microscope, the image of the object may be received on a paper skreen.

There is no inftrument invented by the art of man capable of affording fo great entertainment as the microscope.

By this inftrument we can pry into the minutest recesses of pature; and discover truths which have lain hidden from the creation of the world. It is from the use of this instrument that we can considently affert, that there is hardly any part of nature which is not the abode of animal existence. By it we discover thousands of living creatures in a single drop of water; and whole nations of animated beings in the bloom which surrounds a plum, a pear, and most other fruit; not to mention numberless insects in every part of nature, so small, that a thousand of them might be crushed by a single grain of sand.

From the discovery of these truths, the philosophic mind is led to make still further improvements: thus, in the formation of a mite, we can see the same proportion and symmetry in the structure of his limbs, as in those of any of the larger quadrupeds; as free a circulation of blood in the one as in the other; as many members adapted to different purposes; as numerous veins, muscles, arteries, sinews, &c. &c. with a proboscis to take in its food, like that of the elephant.

And

And if we defeed to infects, of a yet finaller fize, we shall always find in each, all the properties and attributes essential to animal life; if we descend to those infects, whose bulk, compared to that of a mite, is as that of the mite to the elephant.

Others are of fo fmall a fize, as to be beyond the reach of any magnifying power; and whose whole existence is circumscribed within the space of a few hours, or a summer's day at the most. Myriads there are in the vegetable world, to whom the morning gives birth, and who expire with the tetting sum, besides numberless others who have their habitations on the bodies of other animals, such as the ichneumon, whose peculiar habitation is on the body of the caterpillar.

In fhort, there is no part of nature which does not afford to the microscopical observer an abundant source of wonder and admiration, and display the attributes of that Supremo Being, whose wisdom is as conspicuous in the construction of the smallest atom, to be discovered by our affisted sight, as his power is evident in the formation of the planetary systems.

But there are some objects which have more immediately engaged the attention of the curious observer: such as, what is called the filver tree; and the crystallization of talts. The filver tree is formed by diffolying a little filver in a fmall quantity of aqua fortis; and then adding to it twice the quantity of common water. Drop a little of this upon a piece of plain glafs, and put upon it a fmall piece of brats wire; and immediately the wire is put upon the mixture, trees will appear to grow, and difplay their branches, which will be extended, as far as the liquor extends on the glafs; and has all the appearance of real trees, but of a filver caft. To observe the cryflallization of falts, diflo've a little fal-ammoniae in common water, drop a little of this mixture on a piece of glats, as in the former cafe, and when viewing it through the mierofcope, hold an hot iron near it, to make it evaporate the quicker. As foon as the evaporation takes place, it will

rife up in a round cylindrical form like the trunks of trees, and divide and fubdivide, so as to represent branches and boughs: and has a truly wonderful and beautiful appearance. And every different kind of salt forms a different figure.

There are several other objects, which I must recommend to the attention of the young observer: as, 1. The common F/1, the vibration of whose wings is repeated several hundred times in a fecond of time. The great quantity of eyes with which this animal is favoured renders it worthy of notice. each having a distinct optic nerve. 2. The Louie. 3. Mises in cheefe. 4. The cuticular Pores in the human skin, so close and numerous, that a fingle grain of fand will cover hundreds of them. c. The construction of the Scales of Files. 6. The Animakules in several forts of infusions and 7. The construction of common Feathers. Q. The Sting of a Bee, with the form of its barbs. 10. The Configuration of Wood. 11. The common Milder, which displays a numerous group of vegetable substances. 12. Small regetable Seeds. And several other articles.

I shall close this chapter with a few words concerning the method of making small spherule lenses for microscopes, as recommended by the late celebrated Mr. George Adams. And also the method of mixing the metals for the great speculum in the reflecting telescope.

To make the small spherule lenses, a piece of window glass is to be cut into slips, about an eighth of an inch in breadth. Then, holding one of these slips of glass at each end in the slame of a lamp, as the glass begins to melt, it is to be drawn by each hand into a sine thread, and at length it will break. Then one end of this thread being held in the slame of the lamp, it will run up into a small globule, which is to be taken off; and is a small spherule lens. Several of these lenses are to be made, and examined; and those that are the best, are to be preserved for use. For some will always prove faulty, though every precaution be taken.

In this process, the lamp is to be supplied with spirits of wine instead of oil, and the stame is to be blown in an horisomal direction by a blow-pipe, or a pair of bellows for that purpose; and the glass held in the whitest part of the stame, left the sinoke fully the glass.

The social for the speculum of the reflecting telescope, is generally somed of copper and grain ting and in the proportion of two pounds of Swedish copper, to fourteen ounces and an half of grain ting and this mixture is to be melted twice over, before it be call into the mould.

When the metal is cast into a concave mirror, it is ground upon, what is called, the rough grinder, or even a common grind-stone, of the same radius as the concavity of the metal, to take off the rough sace. Then it is ground on a body convex grinder, to give a true spherical figures and lastly, upon a convex bed of hones, which is to perfect that figure, and give the metal a fine smooth sace. Then the concave sace of the metal is to be possibled by a convex tool, covered with pitch. And, lastly, it is to be brought into the parabolic form by a merely mechanical method of grinding it on the possible in a different direction.

But the left metal for speculums, is that proposed by the Rev. Mr. Indeande, and which was proved by Dr. Maskelyne, to exect, in brightness and diffinitions of the inerge, every other metal then known. It confills of thirty-two conness of copper, with filtern or fixteen conness of grain (in (according to the purity of the copper), with one conness of brafs, one counce of filter, and one counce of arterie. I once was prefer to the cutting of a speculum of this metal; and, when finithed, at reflected more light than any speculum I have ever teen.

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and by erolling at I, the point of convergence, and the paincipal forms of the mirror, they form the upper extraunity L, of the issues I K, fimilar to the lower extremity B, of the eligible A it; and then they puls on to the femal concave micror, whole focus is at a. They fall upon this fruit concave mirror at g, and are from thence reflected, converging in the direction gN; because gw is longer than gw; and palling through the bale P, in the large mirror, they would puls on to s before they meet, and there form the lower extremity of of the creft image ed, familiar to the lower extremity B, of the object A B. But palling through the plane convex glaft R, they form that extremity of the image at 5. In the fame manner the rays E, which come from the extremity of the object A, and fall parallel upon the great polyror at P, are from thence reflected to its focus, where a cost new r., on the artige IK, fimler The second of the state of the AB; and from grammation of the arm of Land fall upon it no from when rightly are reflected, converging in the die chan I On this pathog traceigh the hole P of the great notion, they would need at a, and form the upper extremay a of the concernal, find a to the extremity A, of the chief AB, but putting through the convex glass R, they me to and so to be very a large where that point of the mage the contribution matter pencils of rays flow from a section and the part of the object A B, to the great normalist & hyperbore from their eneflected to the focus as a commercial where they form an inverted image of the c) etc. And I fly, the rays paling from the image ab, theory's the everyouts by and through a fmall hole e, in the end of the letter tulezz, they enter the eye f where they end eith other in the papil, and paint the image of the object on the return in its natural polition, and the image is feet, by the eye under the large angle cod.

To find the an agentying power of this telescope, the rule is, to multiply the focal distance of the great mirror, by the distance

chance of the linal mirror from the image which is near the eye; and multiply the local diffrance of the final mirror, by the fecal diffrance of the eye girls; their divide the product of the further multiplication, by the product of the latter, and the quotient will be the magnifying power

When the fifth image II. a former a little factor from the great mirror than its principal local, as at a , the figure of the great mirror is never considered with that of the final one; therefore the tays of the penalt between a first the mail mirror will not be parallely but rather converging. It as no meet in the points query where they would form a larger meet image than a 6, if the gial, I was not at the way. This image might then be viewed a mean of a large eye glass, property pasced but in that case the face of view would be less; therefore, the gials I is nicely a strong the view.

The adjusting forest, to which the head morrow is find a rendere this telefrope applicable it every figure as the final mirror may be brought esture heaver to the eye or removed farther from it; by which means the easy may or made as diverge a little. For faort-ligance eyes, to be converge and sections of a long figure.

In the use of the reselvope a unit or colorace that the measure an object it the more the penche of my are discussionable they fall upon the great mirror and consequently they will be the mager orders they need alone electron therefore, the first image IF will be formed an appending diffusive from the range more but the mager will alone as formed further from the male mirror bank is principle, focus as therefore, the male mirror than is principle distance from the male mirror main or for a considered finance from the male once a victorial man object than which mission as object more remote, this is called personned by turning the adjusting is over.

The reflecting tenticope will make of an eye glade, of a much femiliar than the tention of a greater magazinary



and we will be a single or the designate & The state of the state of the angles of the state of the The second second . . . April 10 Page 15 . . . . Property of the second and the second . . 

rife up in a round exchanged from like the trunks of trees, and divide and fabilities, in as to represent branches and bangus: and has a train wonderful and beautiful appearance. And every different kind of fait forms a different figure.

There are leveral tries strictles, which I must resonance to the areaton of the young diserver; as, t. The manner Fig., the vibration of whole wings is repeated leveral hundred times in a femore of time. The great quantity of eyes with which this minute is hundred; centers it wor by of nonce, each having a diffinite optic nerve. z. The Land. z. Most in cheese. z. The minutes optic nerve. z. The Land. z. Most in cheese. z. The minutes of includes in the human kin, to done and numerous, that a length grain of land will cover hundreds of them. z. The can bricken of includes and liquids. z. The designatures in leveral large of includious and liquids. z. The designation of amount Figure 1. The Configuration of Wasa. z. t. The common Manner, which displays a mannerous group of vegetable facilitations. zz. Small regretable Senie. And develop other articles.

I final code and shapter with a few words contenting the method of making final innervie lends for microhopes, as recommended by the sate colerated Mr. Garge Manual Acid alin the method of mixing the method for the great speculation in the reducing telescope.

To make the final innerse enters a piece of window glars is its be cut into it is, about an eighth of in inch at areadiffs. Then, holding one of mede figs if guils it enter ent in the fame of a lamp, is the guils begins to ment it is to be drawn by each hand ment after mental and it longth it will break. Then one end of this thread on agreed it the final of the hump, it will but a price a line, good, it, where is to be used off; and is a final injustrals easy. Several of their leaves to be made, and each miner, and their true are the tenh, are to be preferred for the. Fire some volumes are the perferred for the colors of the preferred for the colors.

In this process, the lamp is to be supplied with spirits of wine instead of oil, and the same is to be blown in an hotizental direction by a blow-pipe, or a pair of bellows for that purpose; and the glass held in the whitest part of the same, lest the source fully the glass.

The metal for the speculum of the reflecting telescope, is generally sound of copper and grain ting and in the proportion of two pounds of Swedish copper, to sources and so half of grain ting and this mixture is to be melted twice over, before it be cast into the mould.

the metal is called the rough ginder or every a common grad done, of the inner ratios the concepts of the form of the concept and give the metal is to be polithed by a convex tool, covered with patch. And, faitly, it is to be brought into the parabolic form by a merely mechanical method of grinding it on the posither in a different direction.

But the best metal for speculums, is that proposed by the Res. Mr. Edwards, and which was proved by Dr. Miskeling, to exact, in Liephine's and distinctness of the image, every other metal then known. It consists of therty-two ounces of copper, with sincen on a term ounce, of grain tim (according to the purity of the copper), with one ounce of brass, one ounce of silver, and one cunce of arfenic. I once was present at the copper of a speculum of this metal; and, when finalled, at reflect 1 more light than any speculum I have ever seen.

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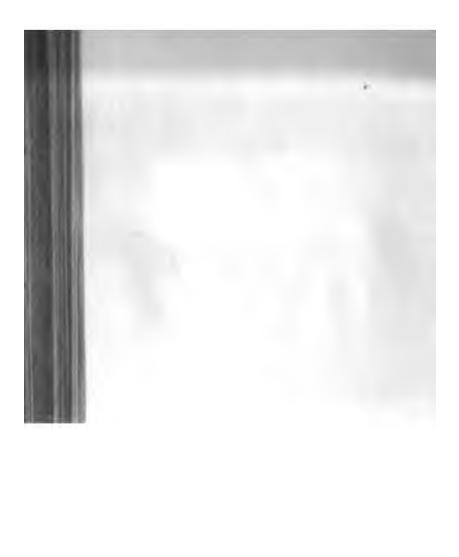
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